



## Chapter 15: CFG = PDA

- I. Theory of Automata
- II. Theory of Formal Languages
- III. Theory of Turing Machines ...



## Chapter 15: CFG = PDA



- Theorem1. Given a CFG that generates the language L, there is a PDA that accepts the language L.
- Theorem2. Given a PDA that accepts the language L, there is a CFG that generates the language L.



## Chapter 15: CFG = PDA

Example:

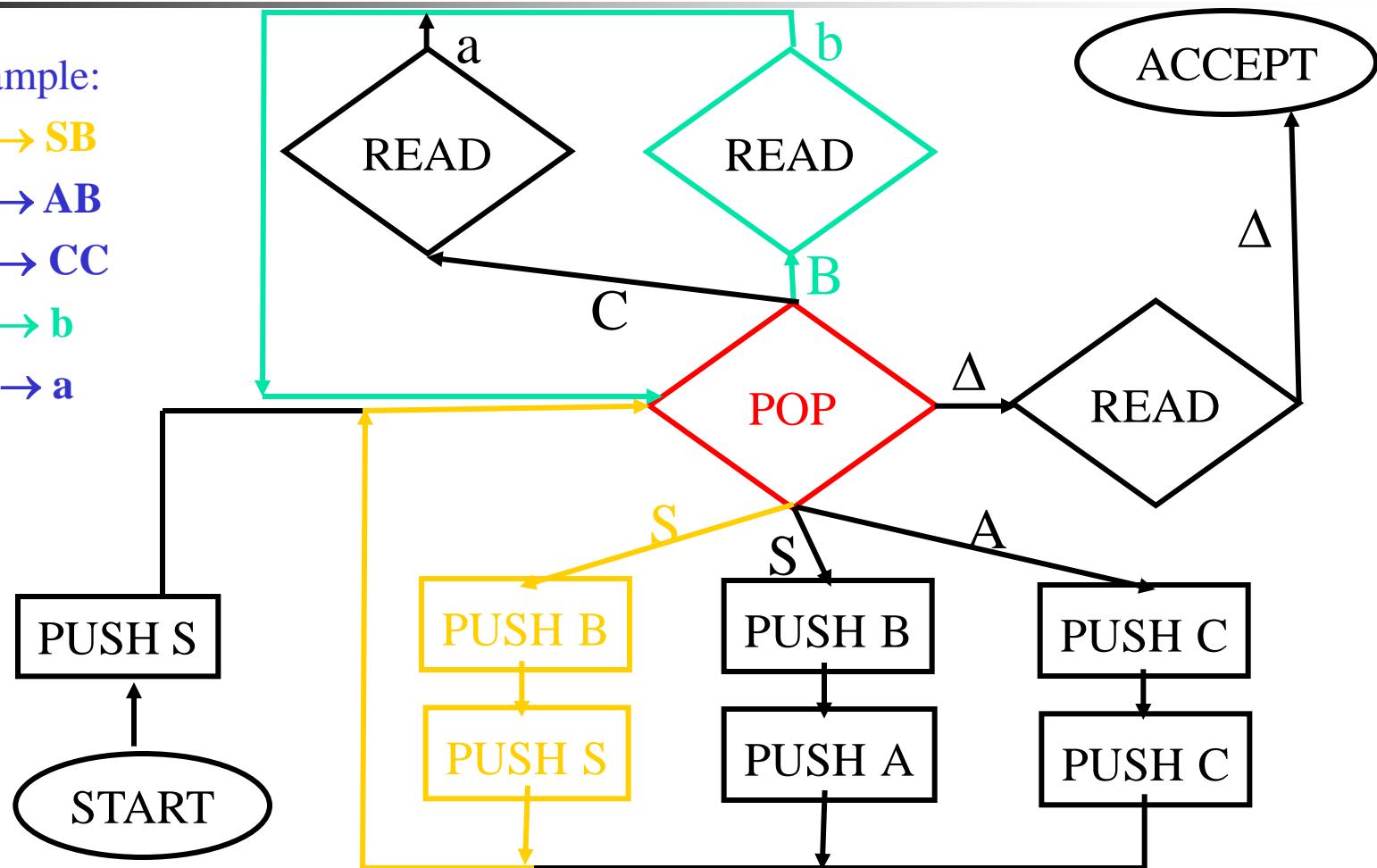
$S \rightarrow SB$

$S \rightarrow AB$

$A \rightarrow CC$

$B \rightarrow b$

$C \rightarrow a$





## Chapter 15: CFG = PDA



- Proof: by constructive algorithm

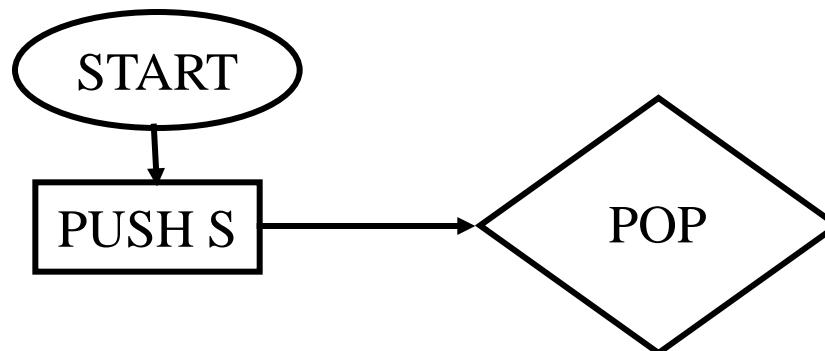
(CFG → PDA)

1. First, transform the grammar to one in Chomsky normal form. All productions are of the form:

$$X_i \rightarrow X_j X_k$$

$$X_i \rightarrow x$$

2. Add

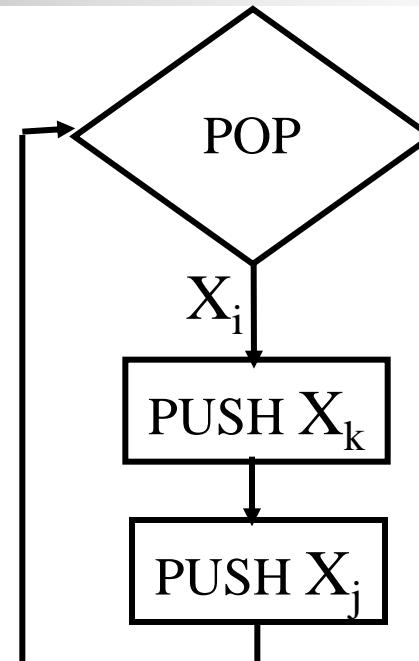
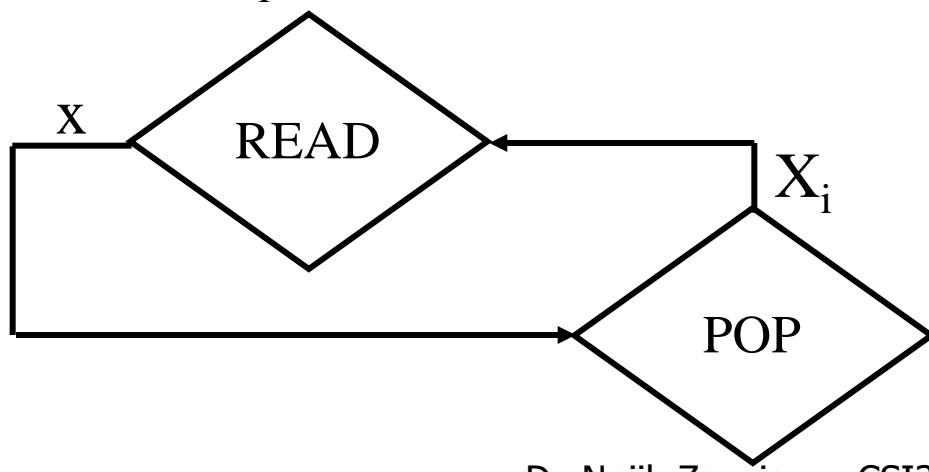




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3. For each production of the form  $X_i \rightarrow X_j X_k$  add:
4. For each production of the form  $X_i \rightarrow x$  add:

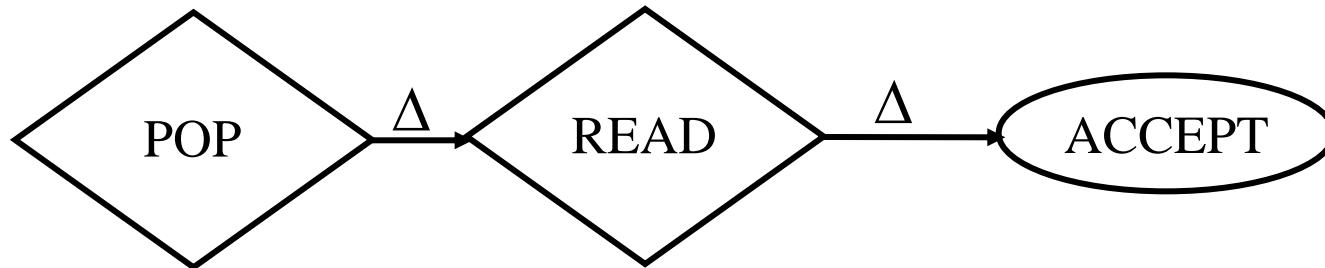




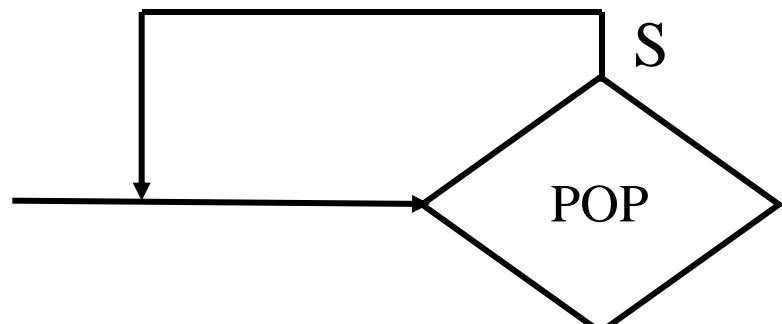
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5. Add:

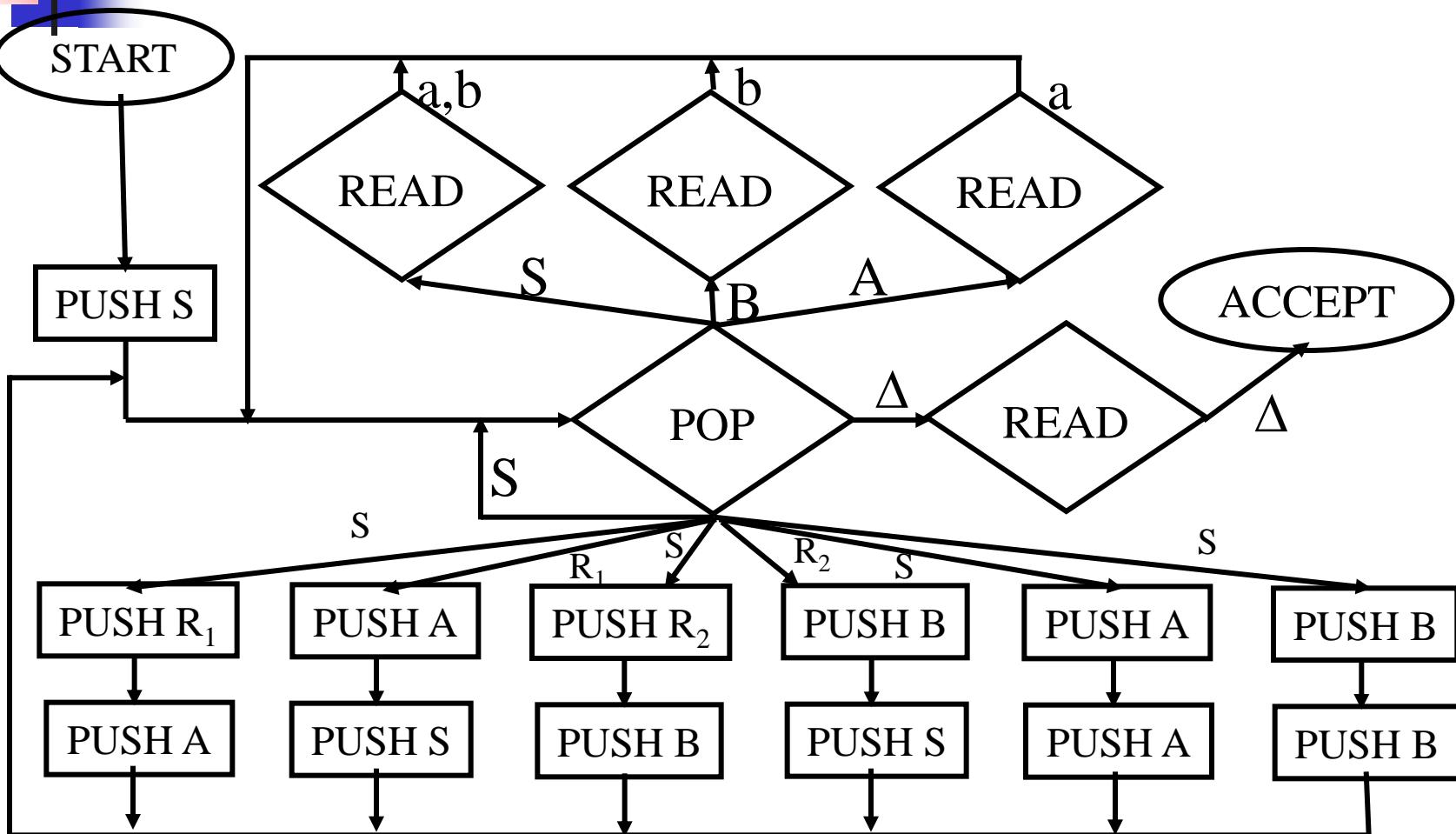


6. If  $\Lambda \in L (S \rightarrow \Lambda)$ , add:





$S \rightarrow AR_1 | BR_2 | AA | BB | a | b | \Lambda$   
 $A \rightarrow a \quad B \rightarrow b \quad R_1 \rightarrow SA \quad R_2 \rightarrow SB$





## Chapter 15: CFG = PDA



- Theorem. Given a PDA that accepts the language L, there is a CFG that generates the language L.
  - See the book for the proof

PDA and CFG are equivalent