### **Modulation Process**

- Modulation: transforming an information-carrying signal m(t) (lowpass) into a narrowband signal x(t). m(t) is also called the <u>modulating signal</u> or <u>message</u>.
- Start with a sinusoidal signal (carrier)  $x(t) = A\cos(2\pi f t + \varphi_0)$
- Varying A = A(t) according to m(t) amplitude modulation (AM)
- Varying  $\varphi = \varphi(t)$  according to m(t) phase modulation (PM)
- Varying f = f(t) according to m(t) frequency modulation (FM)
- FM and PM can be viewed as angle modulation.
- General form of a modulated signal:

$$x(t) = A(t)\cos\left(\omega_{c}t + \int_{0}^{t} \Delta\omega(\tau)d\tau + \varphi(t)\right)$$

### Amplitude Modulation (AM)

- Information-bearing signal m(t) is impressed onto the carrier amplitude.
- Four types of AM:
  - conventional,
  - double sideband suppressed carrier (DSB-SC)
  - single sideband (SSB); can be lower or upper (LSB/USB)
  - vestigial sideband (VSB)
- Spectral characteristics & bandwidth
- Modulation index
- Power efficiency



L.W. Couch II, Digital and Analog Communication Systems, Prentice Hall, 2001.

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# Conventional AM: Sinusoidal Modulation

- Modulated signal:  $x(t) = A_c [1 + a\cos(2\pi Ft)]\cos(2\pi f_c t + \phi_c)$
- Minimum & maximum carrier amplitudes: A.
- Modulation index:

$$M = \frac{A_{\max} - A_{\min}}{2A_c} \le 1$$

$$A_{\min} = A_c [1-a]$$
$$A_{\max} = A_c [1+a]$$

• **x(t) spectrum:**  $x(t) = A_c \cos\left[2\pi f_c t + \phi_c\right] + \frac{A_c a}{2} \cos\left[2\pi (f_c - F)t + \phi_c\right]$ 



### **Conventional AM: Sinusoidal Modulation**

• Signal power  $P_x = \lim_{T \to \infty} \frac{1}{2T} \int_T^t x^2(t) dt = \overline{x^2(t)} = \frac{A_c^2}{2} + \frac{a^2 A_c^2}{4}$ (average): carrier sidebands • Power efficiency:  $\left| \eta = \frac{P_{SB}}{P_{tot}} = \frac{a^2}{2 + a^2} \right|$ Power efficiency of AM 40 Bandwidth:  $\Delta f = 2F$ efficiency, % 30 • Peak power:  $\left| P_{peak} = \frac{\left[ A_c(1+a) \right]^2}{2} \right|$ 20 10 In general: (no DC in m(t))  $\eta = \frac{P_m}{1 + P_m}$ 0 0.2 0.4 0.6 0.8 0 1 а What is the best power efficiency? 

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### Conventional AM: General Case

- General form:  $x(t) = A_c [1 + m(t)] \cos(2\pi f_c t + \phi_c)$
- Modulated signal spectrum:

$$S_{x}(f) = \frac{A_{c}}{2} \left[ \delta(f - f_{c})e^{j\phi_{c}} + \delta(f + f_{c})e^{-j\phi_{c}} + S_{m}(f - f_{c})e^{j\phi_{c}} + S_{m}(f + f_{c})e^{-j\phi_{c}} \right]$$

$$2 \left| S_{x}^{+}(f) \right| = A_{c} \left[ \delta(f - f_{c}) + \left| S_{m}(f - f_{c}) \right| \right]$$
Power ?
Power efficiency?

• Measured by spectrum analyzer: no inf. height for delta function in practice,  $\delta(f - f_c) \leftrightarrow \Delta(f - f_c)$  Bandwidth???



### Example

 Conventional AM signal with a sinusoidal message has the following parameters:

 $A_c = 10, M = 0.5, f_c = 1MHz, F = 1kHz$ 

- 1. Find time-domain expression x(t) of the signal
- 2. Find its Fourier transform
- 3. Sketch its spectrum as it appears on the spectrum analyzer
- 4. Find the signal power, peak power and the power efficiency
- 5. Find the signal bandwidth

## **Generation of Conventional AM**

Power-law modulator:



Using variable-gain amplifier (modulator):



### **Generation of Conventional AM**

### Switching modulator: $A_c \cos 2\pi f_c t$ $v_2(t) = \begin{cases} v_1(t), v_1(t) \ge 0\\ 0, v_1(t) < 0 \end{cases}$ $v_0(t)$ + BPF m(t)at f<sub>c</sub> $v_1$ $\overline{x(t)} = \operatorname{BPF}\left\{\left(m(t) + A_c \cos 2\pi f_c t\right) s(t)\right\}$ $=\frac{A_{c}}{2}\left[1+\frac{4}{\pi A_{c}}m(t)\right]\cos 2\pi f_{c}t \qquad s(t)=\frac{1}{2}+\frac{2}{\pi}\sum_{n=1}^{\infty}\frac{(-1)^{n-1}}{2n-1}\cos\left[2\pi f_{c}t(2n-1)\right]$ $T_{c}$ 0 $-T_{c}$

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### Examples of Modulators for Conventional AM



For more info, see e.g.

- B. Razavi, RF Microelectronics, Prentice Hall, 2012.
- U.L. Rohde, D.P. Newkirk, RF/Microwave Circuit Design for Wireless Applications, Wiley, 2000.
- B. Leung, VLSI for Wireless Communications, Prentice Hall, 2002.

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### Examples of Modulators for Conventional AM



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### **Demodulation of Conventional AM**



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## Demodulation of Conventional AM

• Product detector:



• What happens if  $\theta \neq 0$  ?

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### **Multiplier Implementation**

#### more realistic

AD534: A Four-Quadrant Translinear Multiplier





Adopted from "Considering Multipliers " by B. Gilbert

#### simplified

## <u>Advantages/Disadvantages of</u> <u>Conventional AM</u>

- Advantages
  - Very simple demodulation (envelope detector)
  - "Linear" modulation\*
- Disadvantages
  - Low power efficiency
  - Doubles the baseband bandwidth

### \*Q.: is the conventional AM modulator an LTI system?

### Double-Sided AM: Suppressed Carrier (DSB-SC)

- How to increase power efficiency?
- **DSB-SC signal:**  $x(t) = A_c m(t) \cos(2\pi f_c t)$
- Example: sinusoidal modulation,

 $(f_c - F) f_c (f_c + F)$ 

 $2|S_x^+(f)|$ 

$$x(t) = A_c a \cos(2\pi F t) \cos(2\pi f_c t)$$

• Spectrum: 
$$x(t) = \frac{aA_c}{2} \left[ \cos\left(2\pi(f_c - F)t\right) + \cos\left(2\pi(f_c + F)t\right) \right]$$

Bandwidth??? Geometrical representation??? Power efficiency??? Modulation index???

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### **DSB-SC: General Case**

• DSB-SC signal:  $x(t) = A_c m(t) \cos(2\pi f_c t)$ 

• Spectrum: 
$$S_x(f) = \frac{A_c}{2} \left[ S_m(f - f_c) + S_m(f + f_c) \right]$$

- What do you see on a spectrum analyzer?
- Bandwidth ? Power efficiency? PSD?



## **Generation of DSB-SC**

- Generation:
  - Multiplier
  - Switch (digital)
- Balanced modulator:



J.Proakis, M.Salehi, Communications Systems Engineering, Prentice Hall, 2002

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### **Generation of DSB-SC**

### **Ring modulator** + BPF at f<sub>c</sub> D<sub>1</sub>, $D_3$ m(t)Vout $D_4$ $D_2$ $DC\left[m(t)\right] = 0$ Carrier is suppressed here Square-wave carrier at $f = f_c$ $\frac{v_{out}(t) = BPF\{m(t)s(t)\}}{= \frac{2A_c}{\pi}m(t)\cos 2\pi f_c t} \leq s(t) = A_c \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{2n-1} \cos\left[2\pi f_c t(2n-1)\right]$

Large-amplitude sinusoidal signal may be used instead of the square wave

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# **Demodulation of DSB-SC**

Why will the envelope detector not work?



### **Demodulation of DSB-SC**

• Product detector:



• What happens if  $\theta \neq 0$  ?

# **Demodulation of DSB-SC**

### Demodulation - Costas loop:



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### **Demodulation of DSB-SC**

Product detector + squaring carrier recovery loop:



## Advantages/Disadvantages of DSB-SC

- Advantages
  - High power efficiency
  - If message m(t)>0, envelope detection is possible
- Disadvantages
  - Doubles the baseband bandwidth
  - More complex modulation/demodulation (some form of carrier recovery is required)
  - Pilot tone may be required to simplify demodulation

## Summary of Disadvantages of AM

- Low power efficiency (of conv. AM)
  - solved via DSB-SC
- Low noise immunity
  - via FM or digital
- Low spectral efficiency (double bandwidth)
   ???

### <u>Summary</u>

- Modulation process. Types of analog modulation.
- Conventional AM. Time-domain & frequency-domain representations. Power efficiency & bandwidth.
- Generation (modulation) & demodulation of conv. AM.
- Double sideband suppressed carrier (DSB-SC). Spectrum.
   Bandwidth. Generation & demodulation of DSB-SC.
- Advantages/disadvantages of conventional & DSB-SC AM.
- <u>Homework</u>: Reading: Couch, 5.1-5.4, 4.4., 4.11-4.13. Study carefully all the examples, make sure you understand them and can solve them with the book closed.
- Do some end-of-chapter problems. Students' solution manual provides solutions for many of them.