

## ELG4152: DGD Solution (Chapter 13)

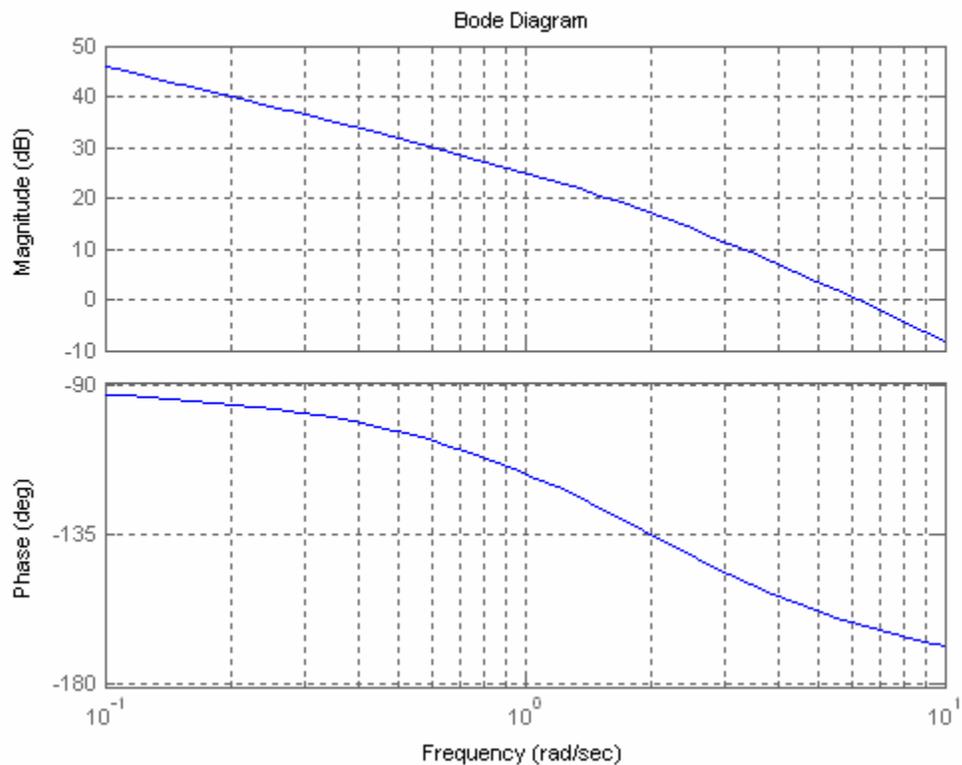
### E13.6

Design for a Phase-lag network on the Bode diagram with phase margin  $45^\circ$ , desired  $K_v=20$ ;

1 Obtain the Bode diagram of the uncompensated system with the gain adjusted for the desired error constant,

Uncompensated transfer function 
$$G(j\omega) = \frac{20}{j\omega(0.5j\omega + 1)}$$

Plot the Bode diagram



2 Determine the phase margin of the uncompensated system  
ensure 5 degree addition phase lag

$$\phi_{pm} = 50^\circ$$

3 Determine the frequency where the phase margin requirement would be satisfied

$$\phi(\omega) = -130^\circ, \omega'_c = 1.5$$

The attenuation necessary to cause  $\omega'_c = 1.5$  to be new crossover frequency is equal to 20dB

Then we find that  $20\text{dB} = 20\log\alpha$ , or,  $\alpha = 10$ . Therefore, the zero is one decade below the crossover,  $\omega_z = \omega'_c / 10 = 1.5 / 10 = 0.15$ , the pole is at  $\omega_p = \omega_z / \alpha = 0.015$ .

The transfer function of the phase-lag network is

$$G_c(s) = \frac{s/0.15 + 1}{s/0.015 + 1} = 0.1 \frac{s + 0.15}{s + 0.015} = K \frac{s + a}{s + b}$$

$$a = 0.15, b = 0.015; \quad K = 0.1;$$

The compensated system is then

$$133.3 s + 20$$

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$$33.33 s^3 + 67.17 s^2 + s$$

As a final check, the phase margin is  $\phi_{pm} = 45^\circ$ ,  $\omega_c' = 1.5$

(b)

$$T = 0.001;$$

We use the relationships

$$a = 0.15, b = 0.015; \quad K = 0.1; T = 0.001$$

$$A = e^{-aT}, B = e^{-bT} \text{ and } C \frac{1-A}{1-B} = K \frac{a}{b}$$

to compute

$$D(z) = C \frac{z-A}{z-B} = 0.1 \frac{z-0.99985}{z-0.999985}$$

### P13.11

Design for a Phase-lag network on the Bode diagram :

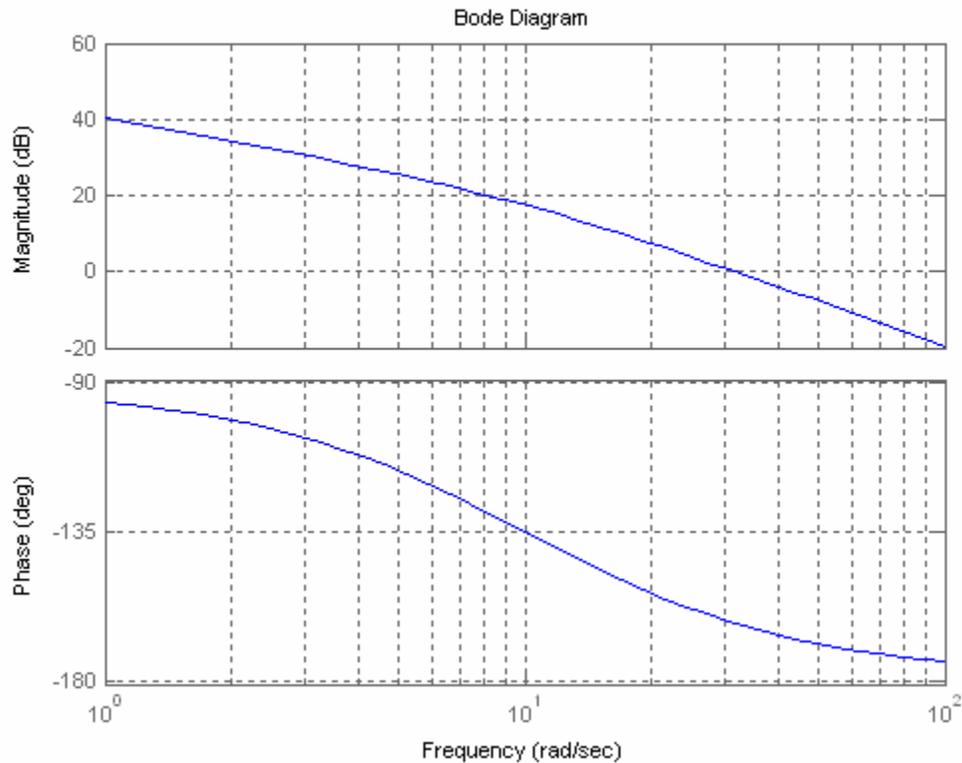
1 Obtain the Bode diagram of the uncompensated system with the gain adjusted for the desired error constant

$$e_{ss} = \frac{10}{K} \leq 0.01, \quad K \geq 1000$$

select  $K=1050$ ,

$$\text{Uncompensated transfer function } G(s) = \frac{1050}{s(s+10)}$$

Plot the Bode diagram



2 Determine the phase margin of the uncompensated system

$\xi = 0.45$ , overshoot is 20%, (Table 5.2)

$$\phi_{pm} = \frac{\xi}{0.01} = 45^\circ$$

ensure 5 degree addition phase lag

$$\phi_{pm} = 50^\circ$$

3 Determine the frequency where the phase margin requirement would be satisfied

$$\phi(\omega) = -130^\circ, \omega'_c = 8$$

The attenuation necessary to cause  $\omega'_c = 8$  to be new crossover frequency is equal to 20dB

Then we find that  $20\text{dB} = 20\log\alpha$ , or,  $\alpha = 10$ . Therefore, the zero is one decade below the crossover,  $\omega_z = \omega'_c / 10 = 8/10 = 0.8$ , the pole is at  $\omega_p = \omega_z / \alpha = 0.08$ .

The transfer function of the phase-lag network is

$$G_c(s) = 1050 \frac{s/0.8 + 1}{s/0.08 + 1} = 105 \frac{s + 0.8}{s + 0.08} = K \frac{s + a}{s + b}$$

$$a = 0.8, b = 0.08; \quad K = 105;$$

The compensated system is then

$$1313 s + 1050$$

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$$12.5 s^3 + 126 s^2 + 10 s$$

As a final check, the phase margin is  $\phi_{pm} = 45^\circ$ ,  $\omega_c' = 8$

Overshoot is 26.4%,  $e_{ss} < 0.01$

(b)  $T=0.1$

We use the relationships

$$a = 0.8, b = 0.08; \quad K = 105; T = 0.1$$

$$A = e^{-aT}, B = e^{-bT} \text{ and } \quad C \frac{1-A}{1-B} = K \frac{a}{b}$$

to compute

$$D(z) = C \frac{z-A}{z-B} = 109 \frac{z-0.9231}{z-0.992}$$

(e)  $T=0.01$ ;

We use the relationships

$$a = 0.8, b = 0.08; \quad K = 105; T = 0.01$$

$$A = e^{-aT}, B = e^{-bT} \text{ and } \quad C \frac{1-A}{1-B} = K \frac{a}{b}$$

to compute

$$D(z) = C \frac{z-A}{z-B} = 105 \frac{z-0.992}{z-0.9992}$$