

## Solution to Midterm 2005

### Question 1a)

- The integer  $X$  has the value 5, and the array  $Y$  initially contains the following values: {2, 4, 6, 8, 10}. Only one of the following Boolean expressions evaluates to true. Circle the letter corresponding to the expression that evaluates to true.
  - a)  $(X < 5) \text{ OR } (Y[Y[1]] = 8)$
  - b)  $(Y[4] \div 2 = X) \text{ AND } (X \text{ MOD } 2 = Y[1] \text{ MOD } 2)$
  - c)  $(X > Y[2]) \text{ AND } (X \leq Y[3])$
  - d)  $Y[Y[0]] \times 2 = (2 \times X + X \text{ MOD } 3)$
  - e)  $X \times X \leq Y[1] \times Y[2]$

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a)  $(X < 5) \text{ OR } (Y[Y[1]] = 8)$

F OR  $Y[4] = 8$

F OR  $10 = 8$

F OR F

F

## Question 1a)

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b)  $(Y[4] \div 2 = X) \text{ AND } (X \text{ MOD } 2 = Y[1] \text{ MOD } 2)$

$10 \div 2 = 5$  AND  $(5 \text{ MOD } 2 = 4 \text{ MOD } 2)$

$5 = 5$  AND  $(1 = 0)$

T AND F

F

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c)  $(X > Y[2]) \text{ AND } (X \leq Y[3])$

5 > 6    AND    5 ≤ 8  
F            AND    T  
                  F

## Question 1a)

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d)  $Y[Y[0]] \times 2 = (2 \times X + X \text{ MOD } 3)$

$Y[2] \times 2 = (2 \times 5 + 5 \text{ MOD } 3)$

$6 \times 2 = (10 + 2)$

12 = 12

T

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e)  $X \times X \leq Y[1] \times Y[2]$

$$5 \times 5 \leq 4 \times 6$$

$$25 \leq 24$$

F

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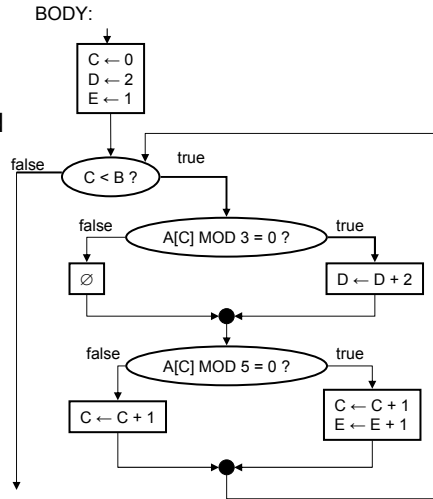
d)  $Y[Y[0]] \times 2 = (2 \times X + X \text{ MOD } 3)$

e)  $X \times X \leq Y[1] \times Y[2]$

## Question 1b)

What would be the values of D and E after the following algorithm executes, if A has the value { 6, 15, 8, 20, 14, 10 } and B has the value 6?

GIVENS: A, B  
 RESULTS: D, E  
 HEADER ( D,E )  $\leftarrow$  AnAlgorithm( A, B )  
 INTERMEDIATE: C



## Trace of algorithm

	A	B	C	D	E
Initial values	{ 6, 15, 8, 20, 14, 10 }	6	?	?	?
C ← 0			0		
D ← 2				2	
E ← 1					1
C < B : true					
A[C] MOD 3 = 0 : true					
D ← D + 2				4	
A[C] MOD 5 = 0 : false					
C ← C + 1			1		
C < B : true					
A[C] MOD 3 = 0 : true					

## Trace of algorithm

	A	B	C	D	E
from previous page	{ 6, 15, 8, 20, 14, 10 }	6	1	4	1
$D \leftarrow D + 2$				6	
$A[C] \text{ MOD } 5 = 0 : \text{true}$					
$C \leftarrow C + 1$			2		
$E \leftarrow E + 1$					2
$C < B : \text{true}$					
$A[C] \text{ MOD } 3 = 0 : \text{false}$					
$\emptyset$					
$A[C] \text{ MOD } 5 = 0 : \text{false}$					
$C \leftarrow C + 1$			3		
$C < B : \text{true}$					
$A[C] \text{ MOD } 3 = 0 : \text{false}$					

## Trace of algorithm

	A	B	C	D	E
from previous page	{ 6, 15, 8, 20, 14, 10 }	6	3	6	2
$\emptyset$					
$A[C] \text{ MOD } 5 = 0 : \text{true}$					
$C \leftarrow C + 1$			4		
$E \leftarrow E + 1$					3
$C < B : \text{true}$					
$A[C] \text{ MOD } 3 = 0 : \text{false}$					
$\emptyset$					
$A[C] \text{ MOD } 5 = 0 : \text{false}$					
$C \leftarrow C + 1$			5		
$C < B : \text{true}$					
$A[C] \text{ MOD } 3 = 0 : \text{false}$					

## Trace of algorithm

	A	B	C	D	E
from previous page	{ 6, 15, 8, 20, 14, 10 }	6	5	6	3
∅					
A[C] MOD 5 = 0 : true					
C ← C + 1			6		
E ← E + 1					4
C < B : false					

Answer: D = 6, E = 4

## Question 2a)

- The following program attempts to extract a sub-array from an array input by the user. The new **subArray** contains only the elements of the input array that have odd indices (**anArray[1], anArray[3]...**). However, two errors were made when producing this program. One error is a syntax error, while the other error is a logic error in the algorithm.
- The first error is that there were **3** errors in the program ☹.
  - Software engineering advice: Changes made at the last minute are often the most error-prone.

```

public static void main ( String[] args )
{
    // DECLARE VARIABLES / DATA DICTIONARY
    int[] anArray;      // GIVEN: an array of values
    int anArrayLength; // GIVEN: number of values in anArray
    int subArrayLength; // INTERMEDIATE: size of a sub-array
    int index;         // INTERMEDIATE: position in an array
    int[] subArray;    // RESULT: new sub-array
    // READ IN GIVENS
    System.out.print( "Enter an array of integers: " );
    anArray = ITI1220.readIntLine( );
    anArrayLength = anArray.length;
    // ALGORITHM BODY
    subArrayLength = anArrayLength / 2;
    subArray = int[subArrayLength]; // create array
    index = 0;
    while (index < anArrayLength)
    {
        subArray[index] = anArray[index*2+1];
        index = index + 2;
    }
    // PRINT RESULTS AND MODIFIEDS
    index = 0;
    while (index < subArrayLength)
    {
        System.out.print(subArray[index] + " ");
        index = index + 1;
    }
}

```

Annotations in the image:

- A box labeled "syntax: missing new" points to the line `subArray = int[subArrayLength];`.
- A box labeled "logic: index < subArrayLength" points to the condition `index < anArrayLength` in the first `while` loop.
- A box labeled "logic: add 1, not 2" points to the line `index = index + 2;`.

## Question 2b)

```

int [] x;
int r;
int i;

/* 1 */ x = new int[] {2, 3, 4, 5, 6};
/* 2 */ r = 1;
/* 3 */ i = x.length-1;
/* 4 */ while ( i > 0 )
{
    /* 5 */ r = r * x[i];
    /* 6 */ if (r > 100)
    {
        /* 7 */ i = i - 1;
    }
    else
    {
        /* 8 */; // do nothing
    }
    /* 9 */ i = i - 1;
}
/* 10 */ System.out.println( r );

```

What does this program print?

- a) 720
- b) 360
- c) 144
- d) 120
- e) 60
- f) There is a run-time error

## Trace of program

#		x	r	i
	Initial values	?	?	?
1	x = new int[] {2, 3, 4, 5, 6};	{2, 3, 4, 5, 6}		
2	r = 1		1	
3	i = x.length-1			4
4	while ( i > 0 ) : true			
5	r = r * x[i]		6	
6	if ( r > 100 ) : false			
8	; // do nothing			
9	i = i - 1			3
4	while ( i > 0 ) : true			
5	r = r * x[i]		30	

## Trace of program

#		x	r	i
	From previous page	{2, 3, 4, 5, 6}	30	3
6	if ( r > 100 ) : false			
8	; // do nothing			
9	i = i - 1			2
4	while ( i > 0 ) : true			
5	r = r * x[i]		120	
6	if ( r > 100 ) : true			
7	i = i - 1			1
9	i = i - 1			0
4	while ( i > 0 ) : false			
10	System.out.println(r)			

## Question 2b)

```
int [] x;  
int r;  
int i;  
  
/* 1 */ x = new int[] {2, 3, 4, 5, 6};  
/* 2 */ r = 1;  
/* 3 */ i = x.length-1;  
/* 4 */ while ( i > 0 )  
{  
    /* 5 */ r = r * x[i];  
    /* 6 */ if ( r > 100 )  
    {  
        /* 7 */ i = i - 1;  
    }  
    else  
    {  
        /* 8 */; // do nothing  
    }  
    /* 9 */ i = i - 1;  
}  
/* 10 */ System.out.println( r );
```

What does this program print?

- a) 720
- b) 360
- c) 144
- d) 120
- e) 60
- f) There is a run-time error

## Question 3) Translate to Java

GIVENS:	A	(An array of integers)
	N	(Number of values in the array A)
RESULT:	Duplicates	(Boolean: True if A contains duplicate values)
HEADER:	Duplicates ← HasDuplicates( A, N )	
INTERMEDIATES:	CheckIndex	(Index of left comparison value)
	DupIndex	(Index of right comparison value)

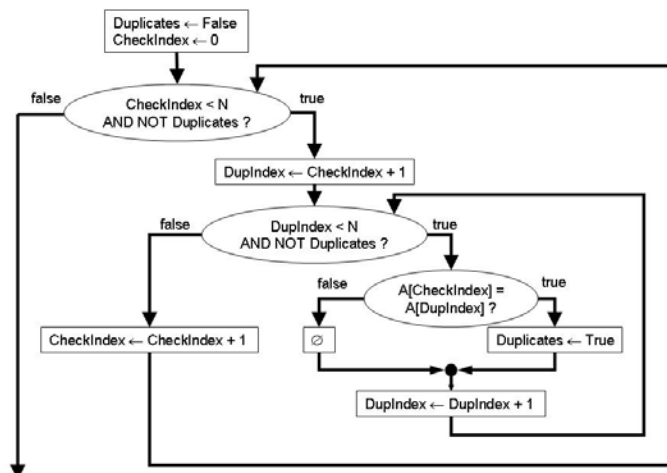
## Question 3 (first part)

```
public static void main( String[] args )
{
    // DECLARE VARIABLES / DATA DICTIONARY

    int [] a;           // GIVEN: array of integers
    int n;              // GIVEN: number of values in the
                       // array A
    boolean duplicates; // RESULT: true if a contains
                       // duplicate values
    int checkIndex;    // INTERMEDIATE: index of left
                       // comparison value
    int dupIndex;      // INTERMEDIATE: index of right
                       // comparison value
}
```

## Question 3 (second part)

BODY:



## Question 3 (second part)

```
// BODY OF ALGORITHM
duplicates = false;
checkIndex = 0;
while ( checkIndex < n && ! duplicates )
{
    dupIndex = checkIndex + 1;
    while ( dupIndex < n && ! duplicates )
    {
        if ( a[checkIndex] == a[dupIndex] )
        {
            duplicates = true;
        }
        else
        {
            ; // do nothing
        }
        dupIndex = dupIndex + 1;
    }
    checkIndex = checkIndex + 1;
}
```

## Question 4: Algorithm

- Suppose that you have an array `BoltSizes` containing the measured lengths, in millimetres, of various bolts after they have been manufactured. There are `N` values in this array. The bolts are intended to have the measured length `CorrectSize`, but the size is permitted to vary, plus or minus, up to and including the amount `Tolerance` to be acceptable
- Design an algorithm to count the number of bolts that should be rejected.
- For example, if the bolt sizes are 50.03, 50.02, 49.97, 50.04, 50.01, 50.00, and 49.99, the correct size is 50.0, and the tolerance is 0.02, the algorithm would return 3.

## Question 4)

GIVENS: BoltSizes (Array of bolt sizes, in mm)  
N (Number of values in array)  
CorrectSize (Correct size for a bolt, in mm)  
Tolerance (Allowed variance in size, in mm)

RESULT: Count (Number of bolts to reject)

HEADER:  $Count \leftarrow \text{CountRejectedBolts}(\text{BoltSizes}, N, \text{CorrectSize}, \text{Tolerance})$

INTERMEDIATES: Index (Index for the array)

## Question 4)

BODY:

