## Operational Amplifiers

- Introduction of Operational Amplifier (Op-Amp)
- Characteristics of an Op-Amp
- Comparison of ideal and Non-ideal Op-Amp
- Feedback and Non-Feedback
- Configurations
- Gain; Input Impedance; Output Impedance
- Analysis of ideal Op-Amp Circuits.


## What is an Operational Amplifier?

- Operational amplifier is an amplifier whose output voltage is proportional to the negative of its input voltage and that boosts the amplitude of an input signal, many times, i.e., has a very high gain.High-gain amplifiers.
- They were developed to be used in synthesizing mathematical operations in early analog computers, hence their name.
- Typified by the series 741 (The integrated circuit contains 8 -pin miniDIP, 20 transistors and 11 resistors).
- Used for amplifications, as switches, as filters, as rectifiers, and in digital circuits.
- Take advantage of large open-loop gain.
- It is usually connected so that part of the output is fed back to the input.
- Can be used with positive feedback to produce oscillation.


## Basics of Differential Amplifier Model



Op Amp is represented by:
$A=$ open-circuit voltage gain
$v_{i d}=\left(v^{+}-v^{-}\right)=$differential input signal voltage
$R_{i d}=$ amplifier input resistance
$R_{o}=$ amplifier output resistance
The output signal of the amplifier is in phase with the signal applied at the + input (non-inverting).
The output signal of the amplifier is $180^{\circ}$ out of phase with the signal applied at the

- input (inverting) terminal.


## Characteristics of Operational Amplifier

- Very high differential gain
- High input impedance
- Low output impedance
- Wide range of applications: oscillators, filters and instrumentation

- Accumulate a very high gain by cascading multiple stages.

$$
V_{o}=G_{d} V_{d}
$$

$G_{d}$ : differenti al gain normally
vey large, say more than $10^{5}$

## Op-Amp: Power Supply Connections

Positive power supply terminal

- Commonly used: dual power supplies
- Common values:

$$
\begin{aligned}
& -+15 \mathrm{~V}(+\mathrm{V} \text { or } \mathrm{V}+) \\
& --15 \mathrm{~V}(-\mathrm{V} \text { or } \mathrm{V}-)
\end{aligned}
$$

- All output loads connected between output terminal and common ground point
- Usually power supply connections are omitted for ease


Negative power supply terminal

## The ideal Op-Amp

- Infinite Voltage Gain
- a voltage difference at the two inputs is magnified infinitely
- something like 200,000, means difference between + terminal and - terminal is amplified by 200,000 !
- Infinite Input Impedance
- no current flows into both inputs
- about $10^{12} \Omega$ for FET input op-amps
- Zero Output Impedance
- rock-solid independent of load
- roughly to current maximum (usually 5-25 mA)
- Infinitely Fast (Infinite Bandwidth)
- limited to few MHz range
- slew rate limited to $0.5-20 \mathrm{~V} / \mu \mathrm{s}$

A Voltage Amplifier

## Simple Voltage Amplifier Model


Source Amplifier Load

$$
\begin{aligned}
& v_{\text {in }}=\frac{R_{i n}}{R_{S}+R_{i n}} v_{S} ; v_{L}=A v_{\text {in }} \frac{R_{L}}{R_{\text {out }}+R_{L}} \\
& v_{L}=\left(A \frac{R_{\text {in }}}{R_{S}+R_{i n}} \frac{R_{L}}{R_{\text {out }}+R_{L}}\right) v_{S} ; v_{\text {in }} \approx v_{S} ; v_{L}=A v_{\text {in }}
\end{aligned}
$$

## Op-Amp as an Integrated Circuit

- The integrated circuit operational amplifier evolved soon after development of the first bipolar integrated circuit.
- The $\mu \mathrm{A}-709$ was introduced by Fairchild Semiconductor in 1965.
- Since then, a vast array of op-amps with improved characteristics, using both bipolar and MOS technologies, have been designed.
- Most op amps are inexpensive (less than a dollar) and available from a wide range of suppliers.
- There are usually 20 to 30 transistors that make up an op-amp circuit.
- From a signal point of view, the op-amp has two input terminals and one output terminal as shown in the following figures.
- The ideal op-amp senses the difference between two input signals and amplifies the difference to produce an output signal.
- Ideally, the input impedance is infinite, which means that the input current is zero. The output impedance is zero.


## Operational Amplifier Model Symbols and Circuit Diagram



## Op-Amp Stages with Pin-outs of IC741



## Ideal Versus Real Op-Amps

| Characteristics | Ideal Op-Amp | Typical Op-Amp |
| :---: | :---: | :---: |
| Input Resistance | Infinity | $\begin{gathered} 10^{6} \Omega \text { (bipolar) } \\ 10^{9} \Omega-10^{12} \Omega \text { (FET) } \end{gathered}$ |
| Input Current | 0 | $10^{-12}-10^{-8} \mathrm{~A}$ |
| Output Resistance | 0 | 100-1000 $\Omega$ |
| Operational Gain | Infinity | $10^{5}-10^{9}$ |
| Common Mode Gain | 0 | $10^{-5}$ |
| Bandwidth | Infinity | Attenuates and phases at high frequencies (depends on slew rate) |
| Temperature | Independent | Bandwidth and gain |

http://hyperphysics.phy-astr.gsu.edu/hbase/electronic/opampcon.html\#c1

## Single Inputs Op-Amp



-     + Terminal : Source
-     - Terminal : Ground
- $0^{\circ}$ Phase change
-+ Terminal : Ground
-     - Terminal : Source
- $180^{\circ}$ Phase change


## Double Inputs Op Amp


$V_{\mathrm{o}}$ Queation: What $V_{\mathrm{o}}$ should be if,


Ans: (A or B)?

## Distortion / Saturation



- The output voltage never exceeds the DC voltage supply of the Op-Amp.
- Practical Op Amps have limited output voltage and current ranges.
- Voltage: Usually limited to a few volts less than power supply span.
- Current: Limited by additional circuits (to limit power dissipation or protect against accidental short circuits).


## A Practical Application: Why Feedback

- Self-balancing mechanism, which allows the amplifier to preserve zero potential difference between its input terminals.
- A practical example that illustrates a common application of negative feedback is the thermostat. This simple temperature control system operates by comparing the desired ambient temperature and the temperature measured by the thermometer and turning a heat source on and off to maintain the difference between actual and desired temperature as close to zero as possible.


## Impedances



- The amplifier measures voltage across $\mathrm{R}_{\mathrm{IN}}$, then generates a voltage which is larger by a factor $\mathbf{A}$
- This voltage generator, in series with the output resistance $\mathrm{R}_{\text {OUT }}$, is connected to the output port.
- A should be a constant (gain is linear)


## Impedances

Add an input - a source voltage $V_{S}$ plus source impedance $R_{S}$


Note the voltage divider $\mathrm{R}_{\mathrm{S}}+\mathrm{R}_{\mathrm{IN}}$.

$$
\mathrm{V}_{\mathrm{IN}}=\mathrm{V}_{\mathrm{S}}\left(\mathrm{R}_{\mathrm{IN}} /\left(\mathrm{R}_{\mathrm{IN}}+\mathrm{R}_{\mathrm{S}}\right)\right.
$$

We want $\mathrm{V}_{\mathrm{IN}}=\mathrm{V}_{\mathrm{S}}$ regardless of source impedance So want $\mathrm{R}_{\mathrm{IN}}$ to be large.

The ideal amplifier has an infinite input impedance!

## Impedances

Add a load - an output circuit with a resistance $\mathrm{R}_{\mathrm{L}}$


Note the voltage divider $\mathrm{R}_{\mathrm{OUT}}+\mathrm{R}_{\mathrm{L}}$.

$$
\mathrm{V}_{\text {OUT }}=\mathrm{AV}_{\mathrm{IN}}\left(\mathrm{R}_{\mathrm{L}} /\left(\mathrm{R}_{\mathrm{L}}+\mathrm{R}_{\text {OUT }}\right)\right)
$$

Want $V_{\text {OUT }}=A V_{\text {IN }}$ regardless of load
We want $\mathrm{R}_{\text {OUT }}$ to be small.
The ideal amplifier has zero output impedance!

## Feedback

Feedback refers to connecting the output of the amplifier to its input



Positive Feedback


Negative Feedback

## Op-Amps for Math

- Inverting
- Non-Inverting
- Summing
- Differencing
- Integrating
- Differentiating


## Common Op-Amp Configurations

## Inverting Amplifier

$$
\begin{aligned}
& i_{S}+i_{F}=i_{\text {in }} \\
& i_{S}=\frac{v_{S}-v^{-}}{R_{S}} ; i_{F}=\frac{v_{\text {out }}-v^{-}}{R_{F}} ; i_{\text {in }}=0 \\
& i_{S}=-i_{F} ; i_{\text {in }}=0 ; v^{-}=v^{+} \\
& \frac{v_{S}}{R_{S}}+\frac{v_{\text {out }}}{A_{v} R_{S}}=-\frac{v_{\text {out }}}{R_{F}}-\frac{v_{\text {out }}}{A_{v} R_{F}} \\
& v_{\text {out }}=-\frac{R_{F}}{R_{S}} v_{S}
\end{aligned}
$$



## Voltage Gain of Inverting Amplifier



$$
\mathrm{v}_{\mathrm{s}}-\mathrm{i}_{\mathrm{s}} R_{1}-\mathrm{i}_{2} R_{2}-\mathrm{v}_{\mathrm{o}}=0
$$

But $\mathrm{i}_{\mathrm{s}}=\mathrm{i}_{2}$ and $\mathrm{v}_{-}=0\left(\right.$ since $\left.\mathrm{v}_{\mathrm{id}}=\mathrm{v}_{+}-\mathrm{v}_{-}=0\right)$
$\therefore \mathrm{i}_{\mathrm{S}}=\frac{\mathrm{v}_{\mathrm{S}}}{R_{1}}$ and $A_{v}=\frac{\mathrm{v}_{\mathrm{O}}}{\mathrm{v}_{\mathrm{S}}}=-\frac{R_{2}}{R_{1}}$

- The negative voltage gain implies that there is a $180^{\circ}$ phase shift between both dc and sinusoidal input and output signals.
- The gain magnitude can be greater than 1 if $R_{2}>R_{1}$
- The gain magnitude can be less than 1 if $R_{I}>R_{2}$
-The inverting input of the Op Amp is at ground potential (although it is physically connected to ground) and is said to be at virtual ground.


## Input and Output Resistances



## Inverting Amplifier: An Example

- Problem: Design an inverting amplifier for
- Given Data: $A_{v}=20 \mathrm{~dB}, R_{i n}=20 \mathrm{k} \Omega$,
- Assumptions: Ideal op amp
- Analysis: Input resistance is controlled by $R_{l}$ and voltage gain is set by $R_{2} / R_{l}$.

$$
A_{v}(d B)=20 \log _{10}\left(\left|A_{v}\right|\right), \therefore\left|A_{v}\right|=10^{40 \mathrm{~dB} / 20 \mathrm{~dB}}=100 \quad \text { and } A_{v}=-100
$$

A minus sign is added since the amplifier is inverting.

$$
\begin{gathered}
R_{1}=R_{\text {in }}=20 \mathrm{k} \Omega \\
A_{v}=-\frac{R_{2}}{R_{1}} \Rightarrow R_{2}=100 R_{1}=2 M \Omega
\end{gathered}
$$

Design Example: Design an inverting amplifier with a closed loop voltage of $\mathrm{A}_{\mathrm{v}}=-5$. Assume the op-amp is driven by a sinusoidal soorce, $v_{\mathrm{s}}$ $=0.1 \sin \omega t$ volts, which has a source resistance of $R_{s r}=1 \mathrm{k} \Omega$ and which supply a maximum current of $5 \mu \mathrm{~A}$. Assume that the frequency is low.
$i_{S}=\frac{v_{S}}{R_{S}}\left(R_{S}\right.$ in thisexample means two resistances : $R_{S}=R_{1}+R_{S r}$.
$R_{S r}$ represents the source resistance. Therefore $i_{S}=\frac{v_{S}}{R_{S r}+R 1}$
If $i_{S}(\max )=5 \mu \mathrm{~A}$, then we write $R_{1}(\min )+R_{S r}=\frac{v_{S}(\max )}{i_{S}(\max )}=\frac{0.1}{5 \times 10^{-6}}=20 \mathrm{k} \Omega$
$R_{1}$ should be $19 \mathrm{k} \Omega$ and $A_{v}=\frac{-R_{2}}{R_{S r}+R_{1}}=-5$.
Accordingly $R_{2}=5\left(R_{S r}+R_{1}\right)=5 \times 20=100 \mathrm{k} \Omega$

## To Solve Ideal Op-Amp Circuit

- If the noninverting terminal of the op-amp is at ground potential, then the inverting terminal is at virtual ground. Sum currents at this point, assuming zero current enters the op-amp itself.
- If the noninverting terminal of the op-amp is not at ground potential, then the inverting terminal voltage is equal to that at the noninverting terminal. Sum currents at the inverting terminal node, assuming zero current enters the op-amp itself.
- For an ideal op-amp circuit, the output voltage is determined from either step 1 or step 2 above and is independent of any load connected to the output terminal.


## Inverting Amplifier with a T-Network



Combing the above equations we get

$$
A_{v}=\frac{v_{O}}{v_{S}}=-\frac{R_{2}}{R_{1}}\left(1+\frac{R_{3}}{R_{4}}+\frac{R_{3}}{R_{2}}\right)
$$

Design Example: An op-amp with a T-network is to be used as a preamplifier for a microphone. The maximum microphone output voltage is 12 mV (rms) and the microphone has an output resistance of $1 \mathrm{k} \Omega$. The op-amp circuit is to be designed such that the maximum output voltage is 1.2 V (rms). The input amplifier resistance should be fairly large but all resistance values should be less than $500 \mathrm{k} \Omega$.
$\left|A_{\nu}\right|=\frac{1.2}{0.012}=100$
$A_{v}=-\frac{R_{2}}{R_{1}}\left(1+\frac{R_{3}}{R_{4}}\right)-\frac{R_{3}}{R_{1}}$
If we choose $\frac{R_{2}}{R_{1}}=\frac{R_{3}}{R_{1}}=8$
$-100=-8\left(1+\frac{R_{3}}{R_{4}}\right)-8 ; \frac{R_{3}}{R_{4}}=10.5$
We should include the value of the source resistance in the calculation
If we set $R_{1}=49 \mathrm{k} \Omega$ and $R_{\mathrm{Sr}}=1 \mathrm{k} \Omega$ then the total resistance ( $R_{1}$ effective ) will be $50 \mathrm{k} \Omega$
$R_{2}=R_{3}=400 \mathrm{k} \Omega$ and $\mathrm{R}_{4}=38.1 \mathrm{k} \Omega$

## Summing Amplifier

$$
\begin{aligned}
& i_{1}+i_{2}+\ldots+i_{N}=-i_{F} \\
& i_{n}=\frac{v_{S_{n}}}{R_{S_{n}}} \ldots . . n=1,2, \ldots N \\
& i_{F}=\frac{v_{\text {out }}}{R_{F}} \\
& v_{\text {out }}=-\sum_{n=1}^{N} \frac{R_{F}}{R_{S_{n}}} v_{S_{n}}
\end{aligned}
$$



## Non-inverting Amplifier


$\frac{v_{\text {out }}}{v_{S}}=1+\frac{R_{F}}{R_{S}}$

## Voltage Follower



$$
7 \mathrm{~N}_{\sim} \text { OUt }
$$

## Non-inverting Amplifier



The input signal is applied to the non-inverting input terminal.
A portion of the output signal is fed back to the negative input terminal. Analysis is conducted by relating the voltage at $v_{1}$ to input voltage $v_{s}$ and output voltage $v_{o}$.

## Non-inverting Amplifier

Voltage Gain, Input Resistance and Output Resistance

Since $i=0$

But $v_{i d}=0$

$$
\mathrm{v}_{1}=\mathrm{v}_{\mathrm{o}} \frac{R_{1}}{R_{1}+R_{2}} \text { and }
$$

$$
\therefore \mathrm{v}_{\mathrm{S}}=\mathrm{v}_{1}
$$

$$
\mathrm{v}_{\mathrm{O}}=\mathrm{v}_{\mathrm{s}} \frac{R_{1}+R_{2}}{R_{1}}
$$

Since $i_{+}=0$

$$
R_{i n}=\frac{\mathrm{v}_{\mathrm{S}}}{\mathrm{i}_{+}}=\infty
$$

$$
\mathrm{v}_{\mathrm{s}}-\mathrm{v}_{\mathrm{id}}=\mathrm{v}_{1}
$$

$$
\therefore A_{v}=\frac{\mathrm{v}_{\mathrm{O}}}{\mathrm{v}_{\mathrm{S}}}=\frac{R_{1}+R_{2}}{R_{1}}=1+\frac{R_{2}}{R_{1}}
$$



Equivalent circuit model

$R_{\text {out }}$ is found by applying a test current source to the amplifier output after setting $\mathrm{v}_{\mathrm{s}}=0$. It is identical to the output resistance of the inverting amplifier i.e. $R_{o u t}=0$.

## Non-inverting Amplifier: An Example

- Problem: Determine the output voltage and current for the given noninverting amplifier.
- Given Data: $R_{l}=3 \mathrm{k} \Omega, R_{2}=43 \mathrm{k} \Omega, v_{s}=+0.1 \mathrm{~V}$
- Assumptions: Ideal op amp
- Analysis:

$$
\begin{aligned}
& A_{v}=1+\frac{R_{2}}{R_{1}}=1+\frac{43 \mathrm{k} \Omega}{3 \mathrm{k} \Omega}=15.3 \\
& \mathrm{v}_{\mathrm{O}}=A_{v} \mathrm{v}_{\mathrm{S}}=(15.3)(0.1 \mathrm{~V})=1.53 \mathrm{~V}
\end{aligned}
$$

Since $i_{-}=0$,

$$
\mathrm{i}_{\mathrm{O}}=\frac{\mathrm{v}_{\mathrm{O}}}{R_{2}+R_{1}}=\frac{1.53 \mathrm{~V}}{43 \mathrm{k} \Omega+3 \mathrm{k} \Omega}=33.3 \mu \mathrm{~A}
$$

Design Example: Design a noninverting amplifier with a closed loop gain of $A_{v}=5$. The output voltage is limited to $-10 \mathrm{~V} \leq v_{o} \leq+10 \mathrm{~V}$ and the maximum current in any resistor is limited to $50 \mu \mathrm{~A}$

Answer: $R_{1}=40 \mathrm{k} \Omega, R_{2}=160 \mathrm{k} \Omega$

## The Unity Gain Amplifier or "The Buffer"



Buffer is a special case of the non-inverting amplifier with infinite $R_{l}$ and zero $R_{2}$. Hence $A_{v}=1$.

It provides an excellent electrical isolation while maintaining the signal voltage level. The ideal buffer requires no input current and can drive any desired load resistance without loss of signal voltage.

Buffer is used in many data acquisition system applications.

## Differential Amplifier



## Differential Amplifier Using Op-Amp



## Differential Amplifier Using Op-Amp

$$
\begin{gathered}
\frac{v_{1}-\frac{R_{2}}{R_{1}+R_{2}} v_{2}}{R_{1}}=\frac{\frac{R_{2}}{R_{1}+R_{2}} v_{2}-v_{0}}{R_{2}} \\
v_{0}=-\frac{R_{2}}{R_{1}} v_{1}+\frac{R_{2}}{R_{1}+R_{2}} v_{2}+\frac{R_{2}^{2}}{R_{1}\left(R_{1}+R_{2}\right)} v_{2} \\
v_{0}=-\frac{R_{2}}{R_{1}} v_{1}+\frac{R_{2}}{R_{1}+R_{2}}\left(1+\frac{R_{2}}{R_{1}}\right) v_{2} \\
v_{0}=\frac{R_{2}}{R_{1}}\left(v_{2}-v_{1}\right)
\end{gathered}
$$

## Differential Amplifier Applications

- Very useful if you have two inputs corrupted with the same noise
- Subtract one from the other to remove noise, remainder is signal
- Applications: Electrocardiagram to measure the potential difference between two points on the body
http://www.picotech.com/applications/ecg.html



The AD624AD is an instrumentation amplifier - this is a high gain, dc coupled differential amplifier with a high input impedance and high CMRR (the chip actually contains a few Op Amps)

## Difference Amplifier: An Example

- Problem: Determine $v_{o}$
- Given Data: $R_{l}=10 \mathrm{k} \Omega, R_{2}=100 \mathrm{k} \Omega, v_{l}=5 \mathrm{~V}, v_{2}=3 \mathrm{~V}$
- Assumptions: Ideal op amp. Hence, $v_{-}=v_{+}$and $i_{-}=i_{+}=0$.
- Analysis: Using dc values,

$$
\begin{aligned}
& A_{d m}=-\frac{R_{2}}{R_{1}}=-\frac{100 \mathrm{k} \Omega}{10 \mathrm{k} \Omega}=-10 \\
& V_{o}=A_{d m}\left(V_{1}-V_{2}\right)=-10(5-3) \\
& V_{o}=-20.0 \mathrm{~V}
\end{aligned}
$$

Here $A_{d m}$ is called the "differential mode voltage gain" of the difference amplifier.

## Finite Common-Mode Rejection Ratio (CMRR)



A real amplifier responds to signal common to both inputs, called the common-mode input voltage ( $v_{i c}$ ). In general,
$v_{o}=A_{d m}\left(v_{1}-v_{2}\right)+A_{c m}\left(\frac{v_{1}+v_{2}}{2}\right)$
$v_{o}=A_{d m}\left(v_{i d}\right)+A_{c m}\left(v_{i c}\right)$
$A\left(\right.$ or $\left.A_{d m}\right)=$ differential-mode gain
$A_{c m}=$ common-mode gain
$v_{i d}=$ differential-mode input voltage
$v_{i c}=$ common-mode input voltage

$$
v_{1}=v_{i c}+\frac{v_{i d}}{2} \quad v_{2}=v_{i c}-\frac{v_{i d}}{2}
$$

An ideal amplifier has $A_{c m}=0$, but for a real amplifier,
$v_{o}=A_{d m}\left(v_{i d}+\frac{A_{c m} v_{i c}}{A_{d m}}\right)=A_{d m}\left(v_{i d}+\frac{v_{i c}}{\mathrm{CMRR}}\right)$
$\mathrm{CMRR}=\left|\frac{A_{d m}}{A_{c m}}\right|$
and $\operatorname{CMRR}(\mathrm{dB})=20 \log _{10}(\mathrm{CMRR})$

## Finite CMRR: An Example

- Problem: Find output voltage error introduced by finite CMRR.
- Given Data: $A_{d m}=2500, \mathrm{CMRR}=80 \mathrm{~dB}, v_{1}=5.001 \mathrm{~V}, v_{2}=4.999 \mathrm{~V}$
- Assumptions: Op amp is ideal, except for CMRR. A CMRR in dB of 80 dB corresponds to a CMRR of $10^{4}$.
- Analysis: $v_{i d}=5.001 \mathrm{~V}-4.999 \mathrm{~V}$

$$
\begin{aligned}
& v_{i c}=\frac{5.001 \mathrm{~V}+4.999 \mathrm{~V}}{2}=5.000 \mathrm{~V} \\
& v_{o}=A_{d m}\left(v_{i d}^{+} \frac{v_{i c}}{\mathrm{CMRR}}\right)=2500\left(0.002+\frac{5.000}{10^{4}}\right) \mathrm{V}=6.25 \mathrm{~V} \\
& \text { In the "ideal" case, } v_{O}=A_{d m} v_{i d}=5.00 \mathrm{~V} \\
& \% \text { output error }=\frac{6.25-5.00}{5.00} \times 100 \%=25 \%
\end{aligned}
$$

The output error introduced by finite CMRR is $25 \%$ of the expected ideal output.

## uA741 CMRR Test Differential Gain

Difference Amplifier -- Differential Gain Test



Differential Gain $\mathrm{A}_{\mathrm{dm}}=5 \mathrm{~V} / 5 \mathrm{mV}=1000$

## uA741 CMRR Test <br> Common Mode Gain

Difference Amplifier -- Common Mode Gain Test



Common Mode Gain $\mathrm{A}_{\mathrm{cm}}=160 \mathrm{mV} / 5 \mathrm{~V}=0.032$
$\operatorname{CMRR}=\frac{\left|A_{d m}\right|}{\left|A_{c m}\right|}=\frac{1000}{.032}=3.125 \times 10^{4}$
$\operatorname{CMRR}(\mathrm{dB})=20 \log _{10}(\mathrm{CMRR})=89.9 \mathrm{~dB}$

## Op-Amp circuit Analysis

Consider the following circuit: $10 \mathrm{k} \Omega$
Assume the op amp is ideal.

a) Calculate $\boldsymbol{v}_{\boldsymbol{o}}$ if $\boldsymbol{v}_{\boldsymbol{s}}=100 \mathrm{mV}$
b) What is the voltage gain $v_{o} / v_{s}$ of this amplifier?
c) Specify the range of values of $\boldsymbol{v}_{\boldsymbol{s}}$ for which the op amp operates in a linear mode

What if the op amp is not ideal?

$$
\begin{aligned}
& R_{i}=10 \mathrm{k} \Omega \\
& \boldsymbol{R}_{\mathrm{o}}=1 \mathrm{k} \Omega \\
& \boldsymbol{A}=10^{3}
\end{aligned}
$$



