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# Improving pedestrian detection with selective gradient self-similarity feature

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#### ABSTRACT

Gradient features play important roles for the problem of pedestrian detection, especially the histogram of oriented gradients (HOG) feature. To improve detection accuracy in terms of feature extraction, HOG has been combined with multiple kinds of low-level features. However, it is still possible to exploit further discriminative information from the classical HOG feature. Inspired by the symmetrical characteristic of pedestrian appearance, we present a novel feature of gradient self-similarity (GSS) in this work. GSS is computed from HOG, and is applied to capturing the patterns of pairwise similarities of local gradient patches. Furthermore, a supervised feature selection approach is employed to remove the non-informative pairs. As a result, the selective GSS (SGSS) feature is built on a concise subset of pair comparisons. The experimental results demonstrate that significant improvement is achieved by incorporating HOG with GSS/SGSS. In addition, considering that HOG is a prerequisite for GSS/SGSS, it is intuitional to develop a two-level cascade of classifiers for obtaining improved detection performance. Specifically, the first level is a linear SVM with the multiscale HOG features to efficiently remove easy negatives. At the second stage, the already computed HOG features are reused to produce the corresponding GSS/SGSS features, and then the combined features are used to discriminate true positives from candidate image regions. Although simple, this model is competitive with the state-of-the-art methods on the well-known datasets.

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#### 1. Introduction

Vision based pedestrian detection is a challenging task of great practical interest in the field of computer vision because of variant appearance and shapes of human. A popular paradigm for pedestrian detection is to convert the problem to binary classification. Discriminative methods extract features inside local regions and construct classifiers for detection. A sliding window strategy is often used. However, this problem involves searching a large number of local image regions for a few objects. Cascade classifiers have been applied to cope with this problem of imbalance [1]. In contrast to conventional classifiers designed for a low overall classification error rate, cascade classifiers are required to obtain a very high detection rate and moderate false positive rate within each layer. Another breakthrough was the introduction of gradient-based features to pedestrian detection. Inspired by SIFT [2], Dalal and Triggs proposed the histogram of oriented gradients (HOG) feature and reported its impressive performance [3]. Currently, HOG is considered to be an unexcelled single feature. There are many works that fused HOG feature with other features to improve its performance [4–7].

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The success of the HOG-based methods indicates that contour is an important clue for pedestrian detection. The existing methods are usually based on partitioning a detection window into a set of subregions, extracting contour features in each subregions, and combining the obtained local features. Although impressive progress has been made in local contour representation, the symmetrical characteristic of pedestrian appearance was been ignored. As shown in Fig. 1, the fragment contours in local regions located in the symmetrical positions on pedestrian's body are similar; on the other hand those located in the foreground are dissimilar to the one in the background. In addition, we found the fact that both the front and profile of pedestrians look symmetrical in most instances. A few examples are shown in Fig. 2. There is apparent symmetry in shape even in different views between the subregions of shoulders, trunk, arms and legs. Therefore, it is possible to measure the similarities among the subregions within the detection window and include the similarities into the representation vector for enhancing contour description.

Improving feature extraction is one of valuable research directions for pedestrian detection as suggested in [8]. Inspired by the fact that pedestrian appearance is usually symmetrical, we present a new feature based on local gradient similarity in this work. This feature, termed gradient self-similarity (GSS), captures pairwise statistics of spatially localized gradient orientation distribution. Since HOG is one







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Similarity matrix

Fig. 1. Illustration of pairwise similarity of HOG blocks. For an image example (left), we show the total energy in each orientation of the HOG cells (middle), and the pairwise similarity matrix of the HOG blocks (right). In the matrix, cells with higher similarity are darker. As shown in the zoomed subfigure, the two blocks located in the foreground are similar because of the symmetric characteristic of pedestrian's appearance. On the other hand, the block in the foreground is dissimilar to the one in the background.



Fig. 2. Examples of pedestrians with symmetrical appearances in different views.

of the most commonly used and effective features for capturing local gradient patterns, we adopt this feature to represent each block in a sliding window. The similarities among the blocks are measured by the Euclidean distance in the feature space. We define the GSS feature as a vector composed of the upper triangular elements of the similarity matrix of the HOG features associated with the blocks. However the high dimensionality of GSS may make the computational cost of feature extraction expensive. Considering that some pairs play more important roles than others, we use the feature generation machine (FGM) [9] to perform feature selection. FGM employs a sparse SVM to determine a subset of the feature for classification while retaining the discriminative information. As a result, only a few informative pairs are selected to construct the selective GSS (SGSS) feature. GSS/SGSS is a kind of HOG based mid-level features, and achieves additional gains from HOG in terms of exploring the association between fragment features. For the purpose of improving detection efficiency and effectiveness, our proposed framework for pedestrian detection is a short cascade, which has two levels: the first level is a linear SVM classifier combining with multiscale HOG to efficiently reject as many of the negative samples while keeping almost all positive samples to the next stage. For the candidate image regions, the HOG features are already computed and reused to produce the corresponding SGSS features. At the second level, we combine the HOG feature and the SGSS feature to discriminate true positives. We also explore the application of the combined feature associated with different classifiers including linear SVM, histogram intersection kernel based SVM (HIKSVM) and AdaBoost. The AdaBoost based cascade achieves the best performance, and is comparable to the state-of-the-art methods on multiple well-known datasets.

The main contributions of this work are twofolds: first, according to our observation on the symmetrical characteristics of pedestrian appearance, we develop the SGSS feature as a mid-level feature capturing the patterns of similarities among local gradient distributions to significantly improve pedestrian detection rate. Second, considering that our SGSS feature is computed from HOG, we design a two-level cascade for pedestrian detection, in which the HOG feature computed on the first level is reused to construct the SGSS feature at the second stage. Our method is therefore based on the computation of a single low-level feature (the HOG). This is an interesting simplification considering that feature extraction is often a computationally costly step in classification approaches. Moreover, we show that the proposed approach provides competitive results. The remainder of this paper is organized as follows. In Section 2, we discuss relevant works on feature extraction and discriminative methods for the pedestrian detection problem. In Section 3, we provide details on the proposed GSS feature and the corresponding feature selection approach. In Section 4, we introduce our cascade of classifiers. In Section 5, we provide the implementation details of the proposed model. In Section 6, we present experimental results based on the proposed approach, and the comparison results with existing methods are also reported. Finally, the conclusion of this paper is presented in Section 7.

#### 2. Related work

In the past decade, great progress in the research of pedestrian detection has been made through the investigation of different approaches for feature extraction, classification, and articulation handling. The surveys [10,8] provide comprehensive introductions on the existing pedestrian detection approaches. For feature extraction, Haar wavelet feature was used in the early work of pedestrian detection [11]. In contrast, HOG [3] is a popular feature used in the modern pedestrian detectors. This feature collects gradient information in local cells into histograms using normalizing overlapping blocks. Local normalization makes this representation robust to small pose variations and changes in illumination. Although there is no single feature outperforming HOG, multiple kinds of features have been reported to complement HOG, such as the motion descriptor based on histogram of optical flow (HOF) [4], the texture descriptors based on local binary patterns (LBP) [7] and center symmetric local trinary patterns (variants of LBP) [12], and the color self-similarity (CSS) feature [6]. To combine multiple kinds of low level pixel-wise features, Enzweiler and Gavrila [13] proposed a multilevel mixture-of-experts model built on HOG and LBP features computed from intensity, depth and dense flow data. Dollár et al. [14] proposed an uniform framework for integrating grayscale, LUV color, and gradient magnitude quantized by orientation. A near real-time version of this method was provided in [15]. Based on HOG, a number of high-level features were developed, such as the

global pose invariant descriptor [16]. Shape is also a commonly used cue for object detection [17-21]. In [18], the shape descriptors (shapelets) were learned from gradients in local patches, and combined by boosting to build an overall detector. Another way to represent mid-level edge features is based on contour. Lim et al. [21] clustered patches of hand drawn contours to generate sketch tokens to capture local edge structure. Combining with other multiple image channels, the representation of per-pixel token labeling is utilized as a feature for a boosted detector. Another dictionary based feature is to use sparse coding to construct the histogram of per-pixel sparse codes for local representation in [20]. The dictionaries are unsupervised learned by K-SVD. Also using an unsupervised technique to learn features from data, a convolutional network model is used to learn multi-stage shape features in [19]. In this work, we are inspired by the symmetrical characteristic of pedestrian appearance, and propose the GSS feature to capture the patterns of the similarities of fragment contours in local regions. HOG is used as a source of low-level features from which our GSS feature is computed. Different from CSS, we here explore the pairwise statistics of spatially localized gradient distributions instead of color. Furthermore, a supervised feature selection method is used to remove the non-informative components in GSS, and produce the SGSS feature. To the best of our knowledge, SGSS has not yet been used as a feature for pedestrian detection.

The most commonly used discriminative approaches to the pedestrian detection problem are various boosting classifiers [14,22,23] and SVM classifiers [3,24,25] which are usually in the form of cascade. For instance, in the work of Viola and Jones [26], the integral image concept is used for fast feature computation, the AdaBoost algorithm is used for automatic feature selection, and a cascade structure is used for efficient detection. In [27], boosted decision trees were applied to a two-level cascade architecture. Felzenszwalb et al. [24] proposed a deformable part model (DPM) in which unknown part positions was modeled in a latent SVM. In another work [28], based on DPM, an ordering of the model's parts was used to define a hierarchy of the models to gain speed which is analogous to a classical cascade. In addition, the histogram intersection kernel has been shown to be more effective than the Euclidean distance for many classification problems when using histogram features. However, for non-linear SVM classifiers, the runtime complexity is high. Maji et al. [25] proposed an approximated intersection kernel SVM which provides great speedup such that the nonlinear SVM can be used in sliding window detection. Recently, deep models have begun to be applied to pedestrian detection [29–31]. Different from the classical cascaded classifiers trained sequentially without optimization, Zeng et al. [31] proposed a multi-stage contextual deep model which jointly trains the classifiers at each stage through back-propagation.

Algorithmically, we use in this work a two-level cascade in which the first level is a linear SVM, and the second level is a linear SVM, HIKSVM or AdaBoost. This design is justified by the fact that the first level is efficient and can quickly remove most false positives, and the already computed HOG features can be reused to generate our SGSS features for further discrimination on the second level. We study here the effectiveness of these classifiers when used in conjunction with the proposed SGSS feature.

#### 3. Gradient self-similarity

The concept of HOG is to represent objects by dense grids of gradient histograms that characterize an object's contour and its spatial information to some extent. The detection window is usually divided into cells represented by gradient histograms, and each  $2 \times 2$  neighboring cells constitute a block. The  $L_2$ -normalization is performed on each block, which makes the HOG feature robust to illumination changes. Since HOG has exhibited excellent performance in representing local gradient

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distributions, we employ HOG to encode the local regions (blocks) in a detection window, and measure the similarities of these blocks by computing the distances in the feature space. To present the patterns of similarities between spatially located blocks, we begin with the introduction of the GSS feature in Section 3.1. In Section 3.2, we present an effective approach of feature selection to remove the redundant components, which provide no more information than the selected subset of components in GSS.

#### 3.1. GSS feature

Let  $\boldsymbol{H} = (\boldsymbol{H}_1, \boldsymbol{H}_2, ..., \boldsymbol{H}_M)$  be the HOG feature in a detection window, where  $H_i$ , i = 1, 2, ..., M, denote the features of the blocks. Since each block consists of  $2 \times 2$  neighboring cells, let  $H_i = (h_i^1, h_i^2, h_i^3, h_i^4)$  be the concatenated histogram of the *i*-th block. We measure the similarities of fragment contours through the distances of HOG blocks in the feature space. Since pedestrians are vertically symmetrical, we consider that the blocks located on the symmetrical positions of pedestrian's body, such as the left and right shoulders, should be similar, but the distances between them may be very large because of the complementarity of their gradient orientations. To solve this problem, one feasible way is to horizontally flip the HOG blocks. Let  $\tilde{H}_i = (\tilde{h}_i^3, \tilde{h}_i^4, \tilde{h}_i^1, \tilde{h}_i^2)$  denote the flipped vector of  $H_i$ . We define the distance matrix as follows:

$$\mathcal{D}_{i,j} = \min(d(\boldsymbol{H}_i, \boldsymbol{H}_j), d(\tilde{\boldsymbol{H}}_i, \boldsymbol{H}_j)), \quad i, j \in \{1, 2, ..., M\},$$
(1)

where d denotes the distance metric. Eq. (1) indicates that the similarity between a pair of HOG blocks is determined by the minimum distance between the flipped and non-flipped cases. There are many possibilities to define d. We tested a number of widely used distance functions including the Euclidean distance,  $\chi^2$ -distance, dot product, and cosine of the angle between dominant gradient orientations in the experiments. We use the Euclidean distance as it yields the best performances. The corresponding similarity matrix is computed by applying the following transform which guarantees that the similarity values are within the range (0, 1]:

$$S_{ij} = \frac{1}{1 + \left(\frac{\mathcal{D}_{ij} - \mathcal{D}_{min}}{\mathcal{D}_{max} - \mathcal{D}_{ij}}\right)^2} \tag{2}$$

where  $\mathcal{D}_{\textit{min}}$  and  $\mathcal{D}_{\textit{max}}$  denote the minimum value and the maximum value respectively (for the cases of the distance defined by dot product and cosine, the formula of similarity computation in Eq. (2)is slightly adjusted by inverting the fraction of the denominator because the similarities between the blocks are proportional to the corresponding distances).

Since S is a symmetric matrix, only the corresponding upper triangular matrix  $S_{upper}$  is taken into consideration for characterizing local gradient similarities. In  $S_{upper}$ , each element represents the similarity of a pair of blocks in the HOG feature space. Although there may exist some elements with the same value, they encode the similarity patterns at different positions. As a result, the GSS feature  $F_{GSS}$  is defined as a vector composed of all the elements of  $S_{upper}$  as follows:

$$F_{GSS} = (g_1, g_2, ..., g_N), g_n \in S_{upper} = \{ S_{i,j} | i < j \}, \quad n = 1, 2, ..., N,$$
 (3)

where  $\mathbf{F}_{GSS}$  has  $N = M \times (M-1)/2$  dimensions. We exhibit the capability of GSS in capturing pairwise local similarity patterns of pedestrian appearance by means of an example in Fig. 3. Fig. 3(a) exhibits the average similarity matrix of all the positive training samples in the INRIA dataset. In order to provide a more intuitive representation, we visualize each row of the average similarity matrix as an indicative image composed of a set of patches. The number and the positions of the patches are the same as those of the blocks in the detection window. For a certain row, the intensity value of each patch



is equal to the similarity value between the corresponding block and the reference block. The average similarity matrix contains 105 rows such that there are 105 indicative images generated. Since many of them are similar, we here exhibit a few representative ones. It is noted that there exist pedestrian structures in the indicative images in Fig. 3(b).

To further explore the discrimination capability of the proposed GSS feature, we use power-law transformation through the following operation applied on each component independently to adjust the similarity values:

$$\phi(z) = |z|^{\alpha},\tag{4}$$

with  $\alpha > 0$ . The power-law transformation is useful for generalpurpose contrast enhancement, especially successful for image enhancement. Fig. 4 shows the plot of power-law transformation with various values of  $\alpha$ . Since all the elements in the similarity matrix S are within the range (0, 1], the role of this transformation is to perform contrast stretching to the relatively small (large)





values when  $\alpha < 1$  ( $\alpha > 1$ ). In our case, we are interested in contrast stretching within the range (0.5, 1] such that similar pairs with high reliabilities can be better discriminated from the ones with a lower similarity. It can be seen from the plot of the power-law transformation that this expected contrast stretching occurs when choosing  $\alpha > 1$ . An example of the power-law transformation ( $\alpha = 2$ ) is shown in Fig. 5. After applying this transformation, the contrast of the GSS feature is enhanced. We empirically observed that this transformation indeed improves the discrimination capability of our GSS feature. Finally, the transformed GSS feature is subsequently  $L_2$ -normalized by  $F_{GSS} = F_{GSS} ||_{F_{GSS}} ||_{2}$ .

#### 3.2. Selective GSS feature

For cases where there are many features and comparatively few samples, feature selection techniques are often used. They bring the benefit of shortening training times and enhancing generalization by reducing overfitting. High dimensional vectors may indeed result in great challenges for computation and training, and in the case of our GSS feature, it is clear that the similarities of some block pairs may be non-informative. We therefore opt for FGM as a tool to perform feature selection such that the trained classifier will be made of simplified decision rules for faster prediction. In contrast to the principal component analysis (PCA) [32] that transforms the



data into a set of linearly uncorrelated variables in an unsupervised way, FGM is a supervised method which reduces the dimensionality of GSS, while preserving discriminative information. Although the partial least square (PLS) analysis [33] is a supervised dimensionality reduction technique and has been shown to be effective for the pedestrian detection problem [34], full features still need to be computed before PLS projection which maintains the complexity of the feature extraction process.

Given a set of labeled samples { $x_l, y_l$ }, l = 1, 2, ..., L, where  $x_l$  is the feature vector and  $y_l$  is the label, FGM aims at finding a sparse solution with respect to the input features to a linear SVM can be learnt by minimizing the following structural risk functional:

$$\min_{\boldsymbol{t} \in T} \min_{\boldsymbol{\omega}, \boldsymbol{\xi}, \rho} \quad \frac{1}{2} \|\boldsymbol{\omega}\|^2 + \frac{\lambda}{2} \sum_{l=1}^{L} \xi_l^2 - \rho$$
s.t.  $y_l \boldsymbol{\omega}'(\boldsymbol{x}_l \odot \boldsymbol{t}) \ge \rho - \xi_l,$ 
(5)

where the positive constraint  $\xi_l > 0$ ,  $\omega$  is the weight vector, the feature selection vector  $\mathbf{t} = (t_1, t_2, ..., t_N) \in T$ ,  $T = \{\mathbf{t} | t_n \in \{0, 1\}, n = 1, 2, ..., N\}$  which controls the sparsity of the SVM decision hyperplane:  $\boldsymbol{\omega}'(\mathbf{x} \odot \mathbf{t})$ , and  $\lambda$  is the regularization parameter that balances the model complexity and the fitness of the decision hyperplane. Eq. (5) is a mixed-integer programming problem. After convex relaxation, Tan et al. [9] proposed an efficient cutting plane algorithm to find a sparse feature solution.

Once feature selection is performed on the training data by applying FGM, the feature subset composed of the selected elements in the GSS feature is concise, while maintaining the discriminating power almost as high as the original GSS feature as it will be shown in Section 6. Thus we define the selective gradient self-similarity (SGSS) feature as the selection of FGM:

$$\begin{aligned} \mathbf{F}_{SGSS} &= (g_{p_1}, g_{p_2}, \dots, g_{p_k}), \\ g_{p_k} &\in \{g_1, g_2, \dots, g_N\}, \\ \text{s.t.} \quad t_{p_k} &= 1, \quad p_k \in \{1, 2, \dots, N\}, \quad k = 1, 2, \dots, K, \end{aligned}$$
(6)

where K is the number of the selected elements that belong to the GSS feature. An example of selected pairs of FGM is shown in Fig. 6. It is noted that most selected pairs involve the blocks, which are located near the contours of the pedestrian structures for the anchor blocks shown in Fig. 3(b). This fact indicates that the contours contain discriminating information, which is consistent with human perception. In contrast to the HOG feature representing the contour information piece by piece, the SGSS feature is capable to explore the association patterns of pieces of contour, which can be seen as a mid-level feature on top of HOG blocks. For this reason, the SGSS feature is considered to be, to a certain extent, complementary to the HOG feature.



**Fig. 5.** An example of the power-law transformation ( $\alpha = 2$ ). Compared to the GSS feature without the transformation (a), the contrast of the transformed GSS feature (b) is enhanced.



Fig. 6. The selected pairs associated with the anchor blocks shown in Fig. 3(b) after using FGM based feature selection. The squares denote the blocks in the detection window, and the lines denote the selected pairs.

#### 4. Cascade

Another major component for pedestrian detection systems is the classifier. We therefore explore the applicability of the developed feature combined with the commonly used classifiers including linear SVM, HIKSVM and AdaBoost. As explained before, the proposed GSS feature is computed from the HOG feature. In order to obtain excellent detection performance while keeping a low computational cost, we introduce a framework composed of two-level cascade of classifiers. On the first level, a linear SVM is trained in the HOG feature space. The goal of this level is to reject as many negatives as possible, while still passing almost all of the positives to the next level. The first level is computationally efficient. The second level makes the final decisions for the candidates including positives and difficult negatives accepted by the first level. Since the HOG features of the candidates have already been computed on the first level, it is straightforward to compute the corresponding GSS features to build more discriminative descriptors combining HOG and GSS. Although GSS feature is high dimensional and the computation cost is expensive, the number of the candidates is usually small. In addition, since we performed feature selection using FGM, the obtained SGSS feature is composed of a small number of informative components. These ones are combined with the HOG feature to train the classifier of the second level to make the final decision. We here apply three different classifiers to the second level of our short cascade.

#### 4.1. Linear SVM

For simplicity, we propose to use a linear SVM model as a baseline classifier at the second level of the cascade. A linear SVM classifier learns the hyperplane that optimally separates pedestrians from background, and usually provides good performance in comparison to other linear classifiers. The combined representation vectors of the HOG feature and the corresponding SGSS feature are then fed to the linear SVM for efficient classification.

#### 4.2. Approximated intersection kernel SVM

Kernelized SVMs are typically used for machine learning based discriminant. Replacing the linear SVM with a nonlinear kernel usually improves performance at the cost of much higher run times because the application of kernelized SVMs to classification requires computing the kernel distance between the input vector and each of the support vectors. As a result, kernelized SVMs are rarely used for detection task because of their high computational load. To make this computation more efficient, we employ an approximated intersection kernel SVM [25] on the second level of the cascade which has the benefit of being independent to the number of support vectors.

For a trained HIKSVM, the decision function is given as follows:

$$\mathcal{J}(\boldsymbol{x}) = \sum_{r=1}^{K} a^{r} y^{r} \mathcal{K}(\boldsymbol{x}, \boldsymbol{x}^{r}) + b$$
$$= \sum_{r=1}^{R} a^{r} y^{r} \left( \sum_{u=1}^{U} \min(x_{u}, x_{u}^{r}) \right) + b,$$
(7)

where  $\mathcal{K}(\cdot, \cdot)$  is the kernel function, and  $\mathbf{x}^r = (x_1^r, x_2^r, ..., x_U^r)$ , r = 1, 2, ..., R, are the support vectors. Exchanging the summations in Eq. (7), we obtain

$$\mathcal{J}(\mathbf{x}) = \sum_{u=1}^{U} \left( \sum_{r=1}^{R} a^{r} y^{r} \min(x_{u}, x_{u}^{r}) \right) + b$$
$$= \sum_{u=1}^{U} \left( \sum_{1 \le r \le q} \overline{a}_{u}^{r} \overline{y}_{u}^{r} \overline{x}_{u}^{r} + x_{u} \sum_{q < r \le R} \overline{a}_{u}^{r} \overline{y}_{u}^{r} \right) + b$$
$$= \sum_{u=1}^{U} \mathcal{J}_{u}(x_{u}) + b, \tag{8}$$

where  $\overline{x}_{u}^{r}$  denotes the increasingly sorted values of  $\mathbf{x}^{r}$  in the *u*-th dimension, and  $\overline{a}_{u}^{r}$  and  $\overline{y}_{u}^{r}$  are the corresponding weight and label. After computing  $\mathcal{J}_{u}(\overline{x}_{u}^{r})$ ,  $\mathcal{J}_{u}(x_{u})$  can be estimated by first finding q and then linearly interpolating between  $\mathcal{J}_{u}(\overline{x}_{u}^{q})$  and  $\mathcal{J}_{u}(\overline{x}_{u}^{q+1})$ . In practice, the input data is quantized in each dimension, and the piecewise constant approximation is used to compute  $\mathcal{J}_{u}$ . As a result, only a lookup table is required for prediction. In our case, the SGSS feature can be quantized before training the intersection kernel model. The discrete SGSS feature is then made more robust to changes in gradients. The quantization distortion of the SGSS feature does not cause loss in classification accuracy because of the piecewise constant approximation of  $\mathcal{J}_{u}$ .

#### 4.3. AdaBoost

AdaBoost offers another fast approach to learning over high dimensional data. In contrast to SVMs, boosting methods minimize the classification error on the training data by combining weak classifiers iteratively. Choosing the appropriate weak classifier is important to produce a strong classifier. We use the regression stumps as our weak classifiers, which are very simple and computationally inexpensive because they classify input samples according to a single dimension of the combined feature vector of HOG and SGSS. We use the gentle AdaBoost algorithm [35] to train the model on the second level of our cascade, which is very similar to other AdaBoost algorithms. During the training phase, the same weight is initially assigned to each sample. A weak classifier is then trained on the weighted training set. The misclassified samples are assigned to higher weights, which enable the training process to more focus on a subset of misclassified data. However, classic AdaBoost algorithm is sensitive to noisy data and outliers. Gentle AdaBoost fits a regression function by minimizing a weighted least-squares loss, and modifies the weighting method to put less weight on outlier samples, which leads to better generalization performance. When the number of individual regression stumps is met, the output of the trained weak classifiers is combined into a weighted sum, which is defined as the final output of the boosted classifier. The runtime of this model is linear in the number of regression stumps.

#### 5. Implementation

Since our objective is to explore the applicability of the SGSS feature, we here use a simple two-level cascade for the task of pedestrian detection. The first level is the commonly used HOG and linear SVM combo. For the candidates passing the first level, the already computed HOG features are used to compute the corresponding SGSS features. The HOG feature and the SGSS feature are then concatenated and fed to the classifiers (linear SVM, HIKSVM, or AdaBoost) on the second level. We will first present the details on the parameter setting and the training procedure for this model, and subsequently introduce the postprocessing technique in the following subsections.

#### 5.1. Parameter setting

Our classification model scans a  $64 \times 128$  detection window with a stride of  $8 \times 8$  across the image, running a pre-trained classifier on the descriptors extracted from each resulting image window. For multiscale detection, we use a scale stride of 1.05. The widely used version of the HOG feature consists of  $7 \times 15$  blocks of histogram features with 36 dimensions per block. Thus there are 5460 block pairs and the corresponding GSS feature is a 5460 dimensional vector of similarities. For feature selection on the GSS feature, the regularization parameter  $\lambda$  in Eq. (5) controls the tradeoff between the model complexity and the fitness. The greater the value of  $\lambda$  is, the higher the dimension of the SGSS feature is. In the experiment, the value of  $\lambda$  is empirically set to 10. In the cascade model, the threshold of the first level is set to 0. For the second level, we use the SVM tool LIBSVM [36] to train a linear SVM and a HIKSVM setting both the values of the parameter C balancing the training error and the rigid margin to 0.1. In addition, we also trained a boosted classifier with 500 regression stumps.

#### 5.2. Training procedure

We train the classifiers on both the two levels of the cascade on the INRIA dataset. Generally, for machine learning algorithms, more training data means better performance. However, for the scanning window classifiers, there are too many negative samples to fit into memory at a single time, and another relevant issue is that training becomes time consuming in the case. As a result, the bootstrapping process is crucial to obtain best performance while keeping the memory requirements manageable. We train the classifiers involved in the cascade with initial subsets of negative samples. For the linear SVM on the first level, 2 negative samples are selected at random for each negative training image. For the classifiers on the second level of the cascade, 2 negative samples having responses from the first level greater than a preset threshold are selected randomly. Next, the negative samples that are incorrectly classified by the initial classifiers are extracted. The training procedure is repeated by including a subset of these difficult negatives into the training set. In our case, we limit the number of hard negative samples added to the training set to 2 for each image. This process is repeated until the change in the miss rates between two iterations is smaller than a pre-specified threshold.

#### 5.3. Postprocessing

In the test phase, the proposed cascade is performed on each test image in all positions and scale with the window stride and the scale factor specified above. Each object is usually detected in multiple overlapping bounding boxes. To eliminate repeated detections, non-maximal suppression is used to merge the multiscale nearby predictions having the final classifier responses greater than a certain threshold. Specifically, we sort the surviving windows by response, then iteratively take the highest one and remove the less confident windows that sufficiently overlap it. In the experiment, the overlap threshold is set to 0.65.

The PASCAL evaluation criterion is usually used to assess detection performance. A detection is considered to be a true positive if the detected bounding box overlaps more than 50% with the ground truth bounding box, where the overlap is measure as the ratio of the intersection area to the union area. For the test images, the ground truth bounding boxes are tight in both height and width of pedestrian. However, the positive training samples are normalized only according to the height such that the change in the foreground area is significant, especially for the case of profile. As a result, it may occur that a detected bounding box well fits a pedestrian in height but fails to match the ground truth because of the width. To solve this problem, we roughly divide the positives into two groups according to the width of pedestrian. For each group, an appropriate cropping solution is made. Once detection is obtained, we compare the detection with the prototypes of the two groups in the HOG\_SGSS feature space, and adopt the cropping solution of the closed group.

#### 6. Experiments and discussion

In this section, we evaluate our GSS/SGSS feature and the proposed cascades on well-known datasets. All detection rates are compared using false-positive-per-image (FPPI) curves. First, to confirm the improvement on detection accuracy by introducing the GSS feature, we employ a linear SVM, and compare the detection performance with HOG and the combinations of HOG and GSS based on various distance metrics and various power-law transformations. Second, to show the effectiveness of feature selection, we study the involved parameters, and compare the performance of using GSS and SGSS. We also evaluate the cascades associating SGSS with different classifiers. Finally, we compare the AdaBoost based cascade using multiscale HOG and the corresponding SGSS with state-of-the-art approaches. In the experiments, we found that receiving about 0.17% of the detection windows is sufficient for the second level to obtain a significant performance boost when compared to the baseline method. In addition, our SGSS feature is composed of the discriminative elements (about 26%) that belong to the GSS feature, therefore it also reduces the computational effort. We performed our experiments on a 3.5 GHz Core i7 PC, and it takes on average 0.4146 s to process a  $640 \times 480$  image. Note that only 6.5% of the time is taken in the SGSS computation and the additional classifier evaluation on the second level.

#### 6.1. Dataset

The test dataset includes the INRIA [3], ETH [37], TUD-Brussels [5], and Caltech [38] pedestrian datasets. Although the scale of the INRIA dataset is relative small, it is popular for evaluating the methods of pedestrian detection due to variable appearance, wide variety of articulated poses, complex backgrounds and illumination changes. The training set includes 2416 images of mirrored pedestrian samples and 1218 pedestrian-free images, and the test set includes 288 images with 589 annotated pedestrians and 453 pedestrian-free images. Only the positive testing images are used for evaluation. The ETH and TUD-Brussels datasets are captured in urban areas using a camera mounted to a stroller or vehicle. In the TUD-Brussels dataset, there are 508 image pairs with overall 1326 annotated pedestrians. In addition, the ETH dataset consists of three test sets including 999, 450 and 354 consecutive frames with 5193, 2359 and 1828 annotated pedestrians respectively. The Caltech dataset is the most challenging and the largest by far. It contains 11 subsets of videos, the first 6 for training and the last 5 for test. There are total 350k pedestrian bounding boxes around 2300 unique pedestrians annotated. The evaluation on this dataset is performed using every 30-th frame.

#### 6.2. Distance metric

The definition of the distance metric in Eq. (1) is the key to construct discriminative GSS features. The first experiment is to explore several possibilities for defining the function d. Having obtained the HOG feature of a sliding window, we here test the common distance functions including the Euclidean distance, dot product,  $\gamma^2$ -distance, and cosine function (for each pair of HOG blocks, the value of d is defined as the mean of the cosine values of the angles between the dominant gradient orientations of the corresponding cells). We evaluate the different combinations of the HOG feature and these types of GSS features by training linear SVMs and testing them on the INRIA dataset. The results shown in Fig. 7 demonstrate that the addition of our GSS feature gives a significant boost to detection accuracy, which indicates that these GSS features are complementary to HOG indeed. Some representative results shown in Fig. 8 more specifically demonstrate the enhanced discriminability in the cases of occlusion and deformation. Compared with the other three types of distance functions, the Euclidean distance is the best. HOG\_GSS (Euclidean) is consistently better than HOG, and improves by 0.17 the detection rate at  $10^{-1}$  FPPI. In the subsequent experiments, we will use the Euclidean distance based GSS feature.

#### 6.3. Power-law transformation

In this experiment, we assign a set of values to the parameter  $\alpha$  in Eq. (4), and test the corresponding GSS features on the INRIA dataset to investigate its effect on the classification result. We here train a linear SVM fed with the combination of HOG and different GSS to obtain the detector. Fig. 9 shows the resulting detection-error-tradeoff curves for different values of  $\alpha$ : 0.5, 1, 2, 3, 4, and 5. At 10<sup>-1</sup> FPPI, when compared to the case where no power-law transformation is applied ( $\alpha = 1$ ), the performance of the detector is the worst for  $\alpha = 0.5$ . When  $\alpha > 1$ , the differences in similarity measurement between the highly similar pairs and the ones with a lower similarity are amplified, and the detector exhibits better performance. When  $\alpha = 2$ , the detector achieves the highest detection accuracy. In this case, the transformed GSS feature becomes more discriminative, and the detection rate is improved by 5 percent points.



Fig. 7. Comparison of the different types of GSS features on the INRIA dataset.



Fig. 8. Some representative results of (a) HOG and (b) HOG\_GSS (Euclidean).

#### 6.4. Feature selection

To reduce the computation cost of the GSS feature while keeping discriminative information, we apply FGM to determine

a concise subset of GSS components as the SGSS feature. Since FGM is supervised, it is guaranteed that the obtained feature will be discriminative. The parameter  $\lambda$  controls the dimension of SGSS. We here test different values of  $\lambda$ : 0.1, 1, 10 and 100. In each



Fig. 9. Comparison of GSS features using different power-law transformations on the INRIA dataset.



Fig. 10. Comparison of the GSS feature and the SGSS features on the INRIA dataset.

case, we combine the HOG feature and the obtained SGSS feature to retrain a linear SVM, and the performance is shown in Fig. 10. With the value of  $\lambda$  increasing, the dimension of SGSS becomes higher, and the corresponding performance is closer to that of GSS. Even in the case of  $\lambda = 0.1$ , combined with the HOG feature, the SGSS feature of 426 dimensions improves the detection rate by 0.15 at  $10^{-1}$  FPPI on the INRIA dataset. The change in performance is not significant when  $\lambda = 10$  and 100. In the following experiments, we set the value of  $\lambda$  to 10 because the dimensionality of the SGSS feature is less than half that of the GSS feature (5460 dimensions) with only a minor loss in detection rate at  $10^{-1}$  FPPI.

#### 6.5. Cascade evaluation

In a sliding window setup, most candidate regions do not show an instance of pedestrian. No need to apply a complex classifier at all possible positions and scales. Our solution is to adopt a twolevel cascade of increasingly powerful classifiers. The first level of the cascade proposes a small number of candidate regions, which are then classified on the second level by using more discriminative features (and a more powerful classifier). An ideal first level of the cascade should reject all regions in which no pedestrian is present, while keeping all regions that do contain a pedestrian instance. To decide which potential regions to forward from the first level to the second of the cascade, we set a threshold  $\gamma$  on the response of the first classifier, which controls the number of potential candidates that will be accepted by the first layer. The lower the threshold is, the more candidate there will be. Of course, if this threshold is set to low, then there will be a large number of candidate windows that will have to be tested by the second laver. thus reducing the efficiency of the classification process. We introduce the miss rate- $\gamma$  curve to seek an operating point with respect to this tradeoff. We evaluate the effect of this cascade parameter on the miss rate. Inspired by [39,40], the detail of our evaluation procedure is described as follows: for each test image in the INRIA dataset, we perform the first level of the cascade to obtain the responses of all detection windows. For each value of  $\gamma$ , we extract the candidates with responses greater than this value, and compute the maximal overlap with any of the ground truth bounding boxes (an overlap of 50% or greater is labeled as true



**Fig. 11.** The plot of the miss rate– $\gamma$  curve for the classifier on the first level.



Fig. 12. Comparison of linear SVM, HIKSVM and AdaBoost as the second level of the cascade on the INRIA dataset.

#### Table 1

Comparison of linear SVM, HIKSVM and AdaBoost on the second level at various settings of  $\gamma$  (with the corresponding average number of candidates) in terms of miss rate at  $10^{-1}$  FPPI on the INRIA dataset (The numbers in bold show the best results of the classifiers).

γ	-2.5	-2.0	- 1.5	- 1.0	-0.5	0	0.5	1.0	1.5
(# Candidates)	(1736)	(984)	(556)	(318)	(185)	(109)	(65)	(37)	(23)
Linear SVM	0.2340	0.2340	0.2340	0.2357	0.2357	0.2149	<b>0.2028</b>	0.2578	-
HIKSVM	0.1867	0.1867	0.1867	0.1872	0.1854	<b>0.1768</b>	0.1958	0.2426	-
AdaBoost	0.1854	0.1854	0.1750	0.1794	0.1872	0.1837	<b>0.1733</b>	0.2270	-

positive). From the result, we calculate the miss rates, and plot them against the values of  $\gamma$ . Fig. 11 shows the resulting plot, and we can see that when  $\gamma < -0.5$ , the curve hardly changes, which means that proposing to the second layer a larger number of candidates does not lead to a higher detection rate.

We also evaluate the detection performance of the cascades introduced in Section 4 on the INRIA dataset. To fully explore the discrimination capability of the SGSS feature, we use the multiscale HOG feature, which includes 3 different window sizes:  $64 \times 128$ ,  $32 \times 64$  and  $16 \times 32$ . Specifically, for a  $64 \times 128$  sliding window, we resize the image region to  $32 \times 64$  and  $16 \times 32$ , and compute the corresponding HOG features. To compute the corresponding GSS feature, we take the similarities of the blocks in different scales into consideration. As a result, there are total 129 HOG blocks, and the corresponding GSS feature has 8256 dimensions. After feature selection, the SGSS feature only has 2162 dimensions (about 26% of the GSS feature dimensions). A common linear SVM trained with the multiscale HOG feature is adopted on the first level of the three two-level cascades to be evaluated. On the second level, a more discriminative feature composed of the multiscale HOG feature and the SGSS feature is then fed to a linear SVM. HIKSVM or AdaBoost classifier. The results shown in Fig. 12 demonstrate that the two-level cascade significantly outperform the linear SVM associated with a single scale HOG. This is mainly due to the multiscale representation and our complementary SGSS feature. In addition, both the HIKSVM and the AdaBoost used on the second levels of the cascade are better than the linear SVM, and the performance of the AdaBoost is the best.

Table 1 shows how the performance of the three cascades is affected as the value of  $\gamma$  is increased. Although the average number of candidates is rapidly decreased, the cascades keep stable performance due to the reason that the candidate windows, which better overlap the pedestrian ground truth bounding boxes, are usually classified with a higher score than others, and thus the weak candidates are filtered first without impacting on the detection performance. However, insufficient candidate windows may lead to that there is no one well overlapping some ground truth bounding boxes. In this case, the detection rate of the cascade will decrease, e.g.  $\gamma = 1$ . In addition, neighboring candidates will be merged at the post-processing stage such that the miss rate at  $10^{-1}$  FPPI may not be available, e.g.  $\gamma = 1.5$ . The three cascades achieve relatively better performance when the value of  $\gamma$ lies in the range [0, 0.5]. In this case, compared with the first level, considered here as a baseline method (the miss rate 0.31 at  $10^{-1}$ FPPI), only about 100 candidate windows (0.17% of total detection windows) are used to extract SGSS features fed to the second level to generate significant improvement in detection accuracy by above 10 percent points.

#### 6.6. Comparison

We finally evaluate our SGSS feature based classifier on the INRIA, ETH, TUD-Brussels and Caltech pedestrian datasets, and compare the proposed approach with the existing methods. We here employ the AdaBoost-based cascade using the multiscale HOG



Fig. 13. Comparison of different methods on the INRIA dataset.



Fig. 14. Comparison of different methods on the ETH dataset.

and the corresponding SGSS as the one used in the above experiment. The results are shown in Figs. 13–16; note that for all the experiments, our classifier has been trained on the INRIA dataset. Our detector significantly outperforms the baseline detector (HOG) by about 0.32, 0.15, 0.23 and 0.17 in the detection rate of  $10^{-1}$  FPPI on the four datasets respectively. Although the proposed model is simple, our detector is close to DPM (LatSvm-V2) as the best detector purely based on the HOG feature on the INRIA dataset, and exhibits better performance on the other three datasets. The other state-of-the-art methods consider more feature channels such as



Fig. 15. Comparison of different methods on the TUD-Brussels dataset.



Fig. 16. Comparison of different methods on the Caltech (reasonable) dataset.

color and gradient magnitude. Despite this fact, our approach provides very competitive results, especially on the ETH, TUD-Brussels and Caltech datasets. The relative ordering of the proposed method is roughly preserved across different datasets, which indicates that our SGSS feature is robust to imaging condition changes.

#### 7. Conclusion

Given a HOG based baseline method for pedestrian detection, we intend to re-use the already computed HOG feature to produce a new mid-level feature instead of computing other low-level features to boost the performance. According to our observation on the symmetrical characteristics of pedestrian appearance, we design the SGSS feature to capture the pairwise similarity patterns of local regions in the HOG feature space. The main topic of this study is to verify the complementarity of the HOG feature and the corresponding SGSS feature, and explore the application of the SGSS feature to improving detection rate, while keeping computation manageable. As demonstrated in the experiments, when combining HOG and GSS/SGSS, the performance of the baseline method becomes better. Furthermore, when combining the baseline method and an additional SGSS based classifier to build a twolevel cascaded architecture, the performance results are better than that of the other existing methods purely based on HOG, and is comparable to that of state-of-the-art methods. Comparing to other features used for pedestrian detection, such as LBP and Haar-like features, the main advantage of our SGSS feature is that it constitutes a mid-level feature built on top of HOG, and provides an effective clue to capture pairwise similarity patterns which are beneficial to pedestrian detection task. We also think that the SGSS feature can be easily applied to other detection systems.

Note that the proposed GSS/SGSS feature is built on simple regular grids and composed of comparisons of a number of HOG block pairs in the sliding window. This leads to the question on how to design an ideal sampling pattern, which would work better than regular grids. Inspired by the work of Alahi et al. [41] mimicking the human visual system, we now would like to design a center-symmetric sampling pattern which has higher density of points near the center with a variation of the Gaussian kernel size in order to gain performance in our future work.

#### **Conflict of interest**

None declared.

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