GEST - A MODELLING AND SIMULATION LANGUAGE BASED ON SYSTEM THEORETIC CONCEPTS*

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ABSTRACT

GEST is the first model and simulation specification language. Specifications of the model and the experiment are totally separated. The modelling world view is based on the axiomatic system theory of Wymore which provides an excellent basis for simulation modelling and symbolic model processing. This chapter has two aims: 1) To present the GEST language and the robust and rich modelling paradigm it provides even for non-simulation application areas, as well as 2) to foster design and development of other GEST-like modelling and simulation languages which would provide other modelling formalisms within comprehensive modelling and simulation systems.

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1. INTRODUCTION

GEST is a modelling and simulation language based on general system theoretic concepts. It was conceived in 1969 and first document about it was published in 1971 (Ören 1971). Its definition has been updated a few times. The last version of it is GEST 81 (Oren 1981, 1982a). GEST, even at its first version, departed radically from other simulation languages. It is the first model-based simulation language. In GEST, specifications of the model and the experiment are totally separated. The modelling world view of GEST is based on the axiomatic system theory of Wymore (1967, 1976).

Already other GEST-like languages exist. One such language is SEMA (SEquential MAchines) (Ören and Collie 1980). Another GEST-like language is designed by Subrahmanian and Cannon (1981). Futo and Gergely (1982) developed TS-PROLOG, an advanced modelling and simulation language based on the concepts advocated by Ören and Zeigler (1979).

This chapter has two aims: 1) To present the GEST language, and 2) to foster design and development of other GEST-like modelling and simulation languages which would provide other modelling formalisms within comprehensive modelling and simulation systems. The rationale for developing such advanced tools within comprehensive modelling and simulation software systems is given in chapter 1 of this volume (Ören 1984).

A list of references where GEST is treated directly, or where GEST has been referred to is given at the end of this chapter.

2. WORLD VIEW OF GEST 81

GEST is a model and simulation specification language. Therefore a GEST program is highly descriptive and acts as a documentation (for communication among humans) as well as a specification (for man-machine communication). This documentation ability of GEST will become apparent in the sequel. If looked only superficially, some elements of GEST may appear to be cumbersome to specify, such as "END COUPLING FOR model-identifier." However, GEST has to be conceived differently.

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- 2) Experi
- 3) Output

The "model" coparameter valuatal conditions model. The "o to be used to

Expressed in B is as follows: the appendix.)

program =
"PROGRAM
model
exper

out**pu** "END PRO

First of all GEST, due to its world view is a good basis for a comprehensive modelling and simulation software system. Within such a system, the computer-assisted modelling module would have all the necessary information to generate "END COUPLING FOR model-identifier" as soon as the specification of all the input-output relationships have been completed by the user, based on system-initiated prompts.

Conceived within a computer-assisted modelling system, some GEST instructions are totally or partially generatable by the system for the convenience of the user. Thus, in addition to be user-friendly and convenient, computer assistance in specifying GEST models can assure completeness as well as consistency checks of the specifica-Another model-based language where user input is minimized through computer-assistance is SEMA (Oren and Collie 1980).

In GEST, a program consists of three distinct parts, i.e.,

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- 2) Experiment(s), and
- 3) Output module(s).

The "model" consists of a parametric model and associated set(s) of parameter values. The "experiment" is the specification of experimental conditions (or experimental frames) which have to to applied to a model. The "output module" is the specification of the output program to be used to display the result of the simulation study.

Expressed in Backus-Naur Form (BNF) the definition of a GEST program is as follows: (The meta-language used to describe GEST, is given in the appendix.)

program = "PROGRAM" identifier

> model experiment

> > output-module-specifiation

"END PROGRAM" identifier ";" .

3. MODEL

3.1 Background

A specific GEST model, is a pair of parametric model and model parameter set. As seen in Figure 1, consists of two parts: 1) a parametric model, and 2) model parameter set(s). The optional model parameter set may appear more than once. A BNF specification of "model" follows:

model =

```
parametric-model-specification
[{ model-parameter-set }] .
```

Parametric Model: A parametric model associated with a parameter set constitutes a specific model that one can use in a simulation study.

A modeller, during the formulation of a parametric model, needs only to specify the names of the parameters of a model. At this stage, the actual values of the parameters need not be specified.

A parametric model may consist of one or several component model(s). A component model may be continuous, discrete, or memoryless. A coupled model consists of a set of component model(s) and their input/output interface which is also called the coupling specification.

Component Model: A component model consists of two sections: In the first section the static structure (or the descriptive structure) of the model, is expressed. In the second section the dynamic structure (or the predictive structure) of the model is specified. This latter section consists of the state transition and the optional output function(s).

The static structure of each component model is described basically in terms of model descriptive variables such as state-, input-, and out-put-variables. However, autonomous models, by definition, do not need inputs to operate. And in some cases explicit output variables may

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Specific GEST model										
	Parame	Parametric model								
		Component models								
		Component model #1								
		•••								
		Component model #n								
		End component models								
		Coupling (i.e., input/output interface) of all component model(s)								
	End parametric model									
	Model parameter set(s)									
		Parameter set #1								
:		•••								
		Parameter set #p								
	End parameter set(s)									
End specific GEST model										

Figure 1. Parts of a specific GEST model

not exist. In this last case, some or all of the state-variables and/ or auxiliary variables may be considered to be the output-variables of the model. In memoryless component models, state variables do not exist. In this case, current output is computed based on the values of the current inputs.

Furthermore, the static structure of a model requires other declarations, such as type and range of values of the descriptive variables of the model. Several modelling formalisms can be used to express component models, such as ordinary differential equations with or without discontinuities in their state-variables and/or their derivatives, difference equations, or combined continuous and discrete-change models.

3.2 Continuous model

Basics

As is shown in Figure 2, the specification of a continuous component model consists of two parts: 1) The static structure and 2) The dynamic structure of the model.

The specification of the static structure of a continuous model consists basically of the declaration of the descriptive variables of the model under the following categories:

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output variable
auxiliary variable
constant
parameter
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tabular function declaration, and
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CONTINUOUS MODEL model-identifier STATIC STRUCTURE INPUT declaration (some or all stochastic) [range declaration] STATE declaration [range declaration]
OUTPUT declaration [range declaration]
AUXILIARY VARIABLE declaration [range declaration] CONSTANT declaration constant assignment PARAMETER declaration (some or all stochastic) [range declaration] AUXILIARY PARAMETER declaration auxiliary parameter computation TABULAR FUNCTION declaration interpolated variable declaration END STATIC STRUCTURE DYNAMIC STRUCTURE **DERIVATIVES** statements **END DERIVATIVES** OUTPUT FUNCTION (optional) statements END OUTPUT FUNCTION END DYNAMIC STRUCTURE END MODEL model-identifier

Figure 2. Layout of a continuous component model specification in GEST

The type of every descriptive variable can be specified separately. The default type is accepted to be real. The ranges of the values of the descriptive variables can also be specified as part of a model in order to enforce some automatic consistency checks. Both external input variables (those variables which are not provided by some component models of a system) and parameters can be stochastic. In this case, it is possible to declare the distribution function to be used to generate them. Another possibility is the ability of declaring tabular functions and the associated interpolation requirements.

The dynamic structure consists of two blocks, i.e. 1) The derivative block which contains the specifications of the derivatives of the state variables and the computations of the necessary auxiliary variables. 2) The output block contains the transformations of the state and/or auxiliary variables into output variables.

Examples:

Some elementary examples of continuous models expressed in GEST are given in Figures 3 and 4.

CONTINUOUS MODEL MIXED_LOGISTIC_GROWTH
STATIC STRUCTURE
STATES Y1, Y2;
OUTPUTS Y1, Y2;
PARAMETERS R1, R2, A1, A2, B1, B2;
END STATIC STRUCTURE;

DYNAMIC STRUCTURE

DERIVATIVES

Y1' = R1*Y1*(1.0 - A1*Y1 - B1*Y2);Y2' = R2*Y2*(1.0 - A2*Y2 - B2*Y2);

END DERIVATIVES;

END DYNAMIC STRUCTURE;
END MODEL MIXED_LOGISTIC_GROWTH;

Figure 3. A continuous model expressed in GEST

Figure 4

Some relevant

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CONTINUOUS MODEL FLOW

STATIC STRUCTURE

INPUT FLOW_IN;

STATE VOL;

OUTPUT VOL;

AUXILIARY VARIABLES FLOW_OUT, NIV;

PARAMETERS R, S;

END STATIC STRUCTURE;

DYNAMIC STRUCTURE

DERIVATIVES

VOL' = FLOW_IN - FLOW_OUT;

FLOW_OUT = NIV/R;

NIV = VOL/S;

END DERIVATIVES;

END DYNAMIC STRUCTURE;

END MODEL FLOW;

Figure 4. A continuous model expressed in GEST

Some relevant definitions in BNF follow:

```
continuous-model =
   "CONTINUOUS MODEL" model-identifier
       "STATIC STRUCTURE"
          [ {input-declaration}
                                    [{ range-declaration }] ]
            {state-declaration}
                                    [{ range-declaration }]
          [ {output-declaration}
                                    [{ range-declaration }] ]
          [ {auxiliary-variable-declaration}
                                    [{ range-declaration }] ]
          [ {constant-declaration}
                {constant-assignment} ]
          [ {parameter-declaration} [{ range-declaration }] ]
          [ {auxiliary-parameter-declaration}
                                    [{ range-declaration }] ]
                {auxiliary-parameter-computation} ]
         [ {tabular-function-declaration}
               {interpolated-variable-declaration} ]
      "END STATIC STRUCTURE" ";"
      "DYNAMIC STRUCTURE"
          "DERIVATIVES"
               {scatement}
          "END DERIVATIVES" ";"
        [ "OUTPUT FUNCTION
               {statement}
          "END OUTPUT FUNCTION" ";" ]
      "END DYNAMIC STRUCTURE" ";"
 "END MODEL" model-identifier ";" .
```

```
om-variabl
   "RANDOM" ["
        { varia
   "END RANDOM
   ge-declarat
    ( "RANGE OF
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 ( "RANGE OF
        "ARRAY
range-limit =
    ([boundary]
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Examples:
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efinitions of type, random-variable-declaration, and range, expressed
n BNF follow:
type = "INTEGER" | "REAL" | "BOOLEAN" | "LITERAL" .
random-variable-declaration =
   "RANDOM" ["REAL"|"INTEGER"] list-of-scalar-variable ";"
       { variable "=" distribution-name "(" list-of-parameter ")" ";" }
   "END RANDOM" ";" .
range-declaration =
   ( "RANGE OF" (scalar-variable | array-variable) "=" type
        "(" range-limit ") " ";" )
 | ( "RANGE OF" scalar-variable "=" "LITERAL"
        "(" list-of-identification ")" ";" )
 | ( "RANGE OF" array-variable "="
        "ARRAY" ("REAL" | "INTEGER" ) array-variable ";" ) .
range-limit =
    ([boundary] ".." boundary) (boundary ".." [boundary]) .
boundary = real | integer | scalar-variable .
The upper and lower boundaries of a range can be given in a model. In
this case they are considered absolute and can not be modified in an
experimental frame.
                     However, if the boundary values may depend on
experimental conditions they may be declared as parameters to be spec-
ified in experimental frames. In the last case, the range of their
acceptable values should be given as the range of the associated
parameters.
Examples:
   RANGE OF STATUS = LITERAL(ON, OFF);
   RANGE OF D
                 = REAL( ... 32.5 );
   RANGE OF PRIORITY = INTEGER ( 1 .. MAX_PRIORITY );
```

RANGE OF VELOCITY = REAL ($\emptyset.\emptyset...327.4$);

```
Definitions of input, state, and output variables follow:
input-declaration =
    ( "INPUT"["S"] [type] list-of-variable ";")
  | ( "INPUT"["S"] random-variable-declaration ";" ).
Examples:
     INPUTS A,B,C;
        RANGE OF A = REAL ( \emptyset.\emptyset\emptyset .. );
        RANGE OF B = REAL ( ... 32.80);
        RANGE OF C = REAL ( \emptyset.\emptyset\emptyset .. 100.0\emptyset);
     INPUTS ARRAY REAL K(1..15), L(1..10), M(1..15);
     INPUT AR, P(1..20);
     INPUT SWITCH;
        RANGE OF SWITCH = LITERAL (ON, OFF);
     INPUTS RANDOM REAL CUS ARRIVAL, X;
                 CUS ARRIVAL = EXPONENTIAL(LAMBDA);
                 X = NORMAL(XM, XS);
            END RANDOM;
state-declaration =
    ( "STATE"["S"] [type] list-of-variable ";" ).
Examples:
     STATE POPULATION;
     STATES YEAST, ALCOHOL;
     STATE MASS FLOW DISCHARGE;
     STATE REAL POPULATION (1..10);
output-declaration =
     ( "OUTPUT"["S"] [type] list-of-variable ";" ).
Example: OUTPUTS REAL L (1..15), N(1..LIM N);
Output variables do not depend on input variables. State variables or
auxiliary variables which are used as output must be explicitly
declared.
```

```
Definitions of auxiliary variables, constants, and parameters follow:
auxiliary-variable-declaration =
   "AUXILIARY VARIABLES" list-of-variables ; .
constant-declaration =
   "CONSTANT"["S"] [type] list-of-scalar-variable ";" .
Example:
      CONSTANTS REAL K, L;
constant-assignment =
   scalar-variable "=" arithmetic-expression ";" .
Examples:
PΙ
          = 3.1415926;
P8Ø
          = PI/180.0;
LATITUDE = 52.0;
LONGITUDE = -5.0;
parameter-declaration =
   ("PARAMETER"["S"] [type] list-of-variable ";")
| ("PARAMETER"["S"] random-variable-declarations ).
Examples:
    PARAMETER REAL PA(1..3,1..5), P1;
    PARAMETER
        RANDOM REAL KE, KD;
            KE = NORMAL(200., 20.);
            KD = NORMAL(XM, SD);
        END RANDOM;
```

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w:

Auxiliary parameters are defined in terms of parameters and constants. Once the values of the parameters are given, the values of the auxiliary parameters can be computed by the system and made available for the convenience of the user.

```
auxiliary-parameter-declaration =
    ( "AUXILIARY PARAMETER"["S"] [type]
           list-of-variable ";"
               { auxiliary-parameter-computation }
      "END AUXILIARY PARAMETER" ";" ).
Example:
     AUXILIARY PARAMETERS K, L;
         K = PI/OMEGA;
         L = 1.00/DIST;
     END AUXILIARY PARAMETER;
auxiliary-parameter-computation =
     (scalar-variable = arithmetic-expression ";")
  | for-statement
  | (identifier "(" list-of-integer ")"
                                                }
         "=" arithmetic-expression ";" ) .
Auxiliary parameters may depend on constants, parameters, and other
auxiliary parameters.
tabular-function-declaration =
     ["DISCONTINUOUS"]
      "TABULAR" ( "FUNCTION"["S"] | "FUNCTION 2")
      list-of-function-name ";" .
DISCONTINOUS and FUNCTION_2 introduce discontinuous and two-dimen-
sional tabular functions, respectively.
```

Examples:

TABULAR FUN

DISCONTINUC

"(" 1i:

{ scalar

Examples:

INTERPOLATI

INTERPOLATI

RATE1 =

RK 4

END INTERPO

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and constants.
                          Examples:
s of the auxil-
le available for
                               TABULAR FUNCTIONS GROWTH_RATE, FK;
                               TABULAR FUNCTION_2 DIFF_COEF;
                               DISCONTINUOUS TABULAR FUNCTION RAIN;
                          interpolated-variable-declaration =
                              ( "INTERPOLATION"
                                    scalar-variable "=" function-name
                                    "(" list-of-scalar-variable ")" ";" )
                            | ( "INTERPOLATIONS"
                                  { scalar-variable "=" function-name
                                    "(" list-of-scalar-variable ")" ";" }
                                "END INTERPOLATION" ";" ) .
                         Examples:
                              INTERPOLATION
                                             RATE = CURVE_1 (TEMPERATURE);
                              INTERPOLATIONS
                                  RATE1 = ABC (T);
                                        = FUN (T);
ers, and other
                              END INTERPOLATIONS;
```

and two-dimen-

3.3 Discrete and Memoryless Models

Basics

Both discrete and memoryless models, like continuous model, have two parts: 1) The static structure and 2) the dynamic structure.

Discrete models allow specification of systems expressed by a set of first order diffreence equations.

In discrete models, the static structure is like the static structure of a continuous model. However, a discrete model differs from a continuous model in the dynamic structure where the derivative block is replaced by the following block:

STATE TRANSITION
statements
END STATE TRANSITION;

A memoryless model differs in two ways from a continuous model: 1) The static structure does not have declaration of any state variable, and 2) the dynamic structure has only output function specification.

A memoryless model transforms instantaneously its inputs and parameters into some output. For the convenience of naming, if a memoryless model has one output only, the same name can be used to designate the model and its output.

Example:

MEMORYLI

STAT

END

DYNA

END I

END MODEL

Figure 5. A m

Example:

MEMORYLESS MODEL BIRTH_RATE

STATIC STRUCTURE

INPUTS

S, (* MATERIAL STANDARD OF LIVING *)

NE, (* EFFECTIVE POLLUTION

P; (* POPULATION *)

OUTPUT BIRTH_RATE;

PARAMETERS K20, K21, K22, K23, K24, K25;

END STATIC STRUCTURE;

DYNAMIC STRUCTURE

B = K20 - K21*S - K22*NE - K23*P;

IF B >= K24 AND B <= K25

THEN BIRTH RATE = B;

ELSE IF B < K24

THEN BIRTH_RATE = K24;

ELSE BIRTH_RATE = K25;

END IF;

END IF;

END DYNAMIC STRUCTURE;

END MODEL BIRTH_RATE;

Figure 5. A memoryless model expressed in GEST

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3.4 Coupling

Basics

A coupled model (or a resultant model) consists of a set of component model(s) and their coupling which specifies input/output relationships of the component models.

An example of a coupled model is given in Figure 6. A GEST representation of the coupled model represented in Figure 6, is provided in Figure 7.

The layout of a coupled model specification in GEST is given in Figure 8.

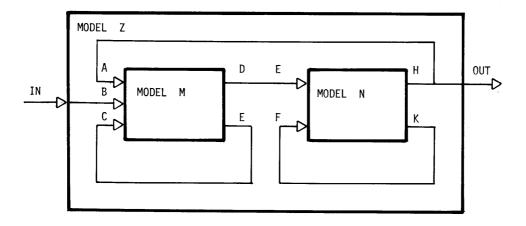


Figure 6. A coupled model

COUPLED MODEL EXTERNAL

INPUT

OUT PUT RA

END EXTERM

COMPONENT !

(* Deta

woul MODEL !

END MOI

MODEL I

END MOE

END COMPONE

EQUIVALENCI

INPUTS OUT PUTS

END EQUIVAL

COUPLING FO

M.A <--

M.B <--

M.C <--

N.F <--

N.G <--

END COUPLIN

END MODEL Z;

lgure 7. GEST re

```
COUPLED MODEL Z
       EXTERNAL
           INPUT IN;
               OUTPUT OUT;
               RANGE OF OUT = REAL (40.0 .. 75.0);
       END EXTERNAL;
       COMPONENT MODELS M, N;
           (* Detailed specifications of the component models \mathbf{M}_{\text{\tiny{F}}} \mathbf{N}
              would appear herebelow:
                                                                   *)
          MODEL M
          END MODEL M;
          MODEL N
          END MODEL N;
      END COMPONENT MODELS;
      EQUIVALENCING
          INPUTS Z.IN = M.B;
          OUTPUTS Z.OUT = N.H;
      END EQUIVALENCING;
      COUPLING FOR Z
          M.A <--- N.H;
         M.B <--- Z.IN; (* Z.IN IS AN EXTERNAL INPUT *)
         M.C <--- M.E; (* FEED-BACK COUPLING
         N.F <--- M.D;
         N.G <--- N.K;
                         (* FEED-BACK COUPLING
                                                       *)
      END COUPLING FOR Z;
 END MODEL Z;
igure 7. GEST representation of the coupled model given in Figure 6.
```

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OUT

INPUTS - list-of-external-inputs_ OUTPUTS- list-of-external-outputs END EXTERNALS COMPONENT MODELS - list-of-component-models For every component model specify STATIC STRUCTURE DYNAMIC STRUCTURE Loop EQUIVALENCING						
OUTPUTS- list-of-external-outputs END EXTERNALS COMPONENT MODELS - list-of-component-models For every component model specify STATIC STRUCTURE DYNAMIC STRUCTURE Loop						
COMPONENT MODELS - list-of-component-models For every component model specify STATIC STRUCTURE DYNAMIC STRUCTURE Loop						
For every component model specify STATIC STRUCTURE DYNAMIC STRUCTURE Loop						
STATIC STRUCTURE DYNAMIC STRUCTURE Loop						
DYNAMIC STRUCTURE Loop						
Loop						
EQUIVALENCING						
INPUTS - list-of-equivalent external and internal inputs						
OUTPUTS - list-of-equivalent-external and internal outputs						
END EQUIVALENCING						
COUPLING						
For every component model do						
For every input variable specify						
from which output variable of which component model the values are provided Loop						
Loop						
END COUPLING FOR model-identifier END MODEL model-identifier						

Figure 8. Layout of a coupled model specification in GEST

"COUPLED MODE

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"END MODEL"

[input[output

"END EXTERNAL"

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or output variable

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variables is the
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Another implicational input and out sponding variable and corresponding

Some relevant BNF definitions follow: coupled-model = "COUPLED MODEL" model-identifier [external-variables] { component-model } "END COMPONENT MODELS" ";" coupling "END MODEL" model-identifier ";" external-variables = "EXTERNAL" **tern**al inputs "END EXTERNAL" ";" . ternal outputs ich component

"COMPONENT MODELS" list-of-component-models ";" [equivalencing-external-and-internal-variables] [input-declaration [{ range-declaration }]] [output-declaration [{ range-declaration }]]

In the external variables section, the names of the external input and output variables of the coupled model are declared. For every input or output variable, range of the values may also be specified.

An implication of the ability to declare external input or output variables is the possibility to specify nested couplings where at least one of the component models is itself a coupled model.

Another implication is the ability to declare the ranges of the external input and output variables independent of the ranges of the corresponding variables of component models. The compatibility of external and corresponding internal variables can be checked algorithmically.

```
list-of-component-models =
 model-identifier [ ":" unsigned-integer "TO" unsigned-integer ]
 { "," model-identifier
                   [ ":" unsigned-integer "TO" unsigned-integer ] } .
Example: COMPONENT MODELS M:1 TO 15, N, P:3 TO 7;
This statement causes the generation of 15 replicas of a model M. The
generated copies are then named, by the system, M:1, M:2, ..., M:15.
Similarly, five replicas of the component model P are generated and
named P:3, P:4, ..., and P:7.
equivalencing-external-and-internal-variables =
     "EQUIVALENCING"
          equivalencing-inputs
          equivalencing-outputs
     "END EQUIVALENCING" ";" .
In equivalencing external and internal inputs, one has to consider
that an input to the coupled model can be the input to one or several
component models. However, every output of the coupled model is an
output of one component model only.
equivalencing-inputs =
   "INPUTS"
        { model-identifier "." input-variable "="
         model-identifier [ ":" unsigned-integer ] "." input-variable
   [{ "," model-identifier [ ":" unsigned-integer ]
                             } "." input-variable }] ";" }.
equivalencing-outputs =
   "OUTPUTS"
        { model-identifier "." output-variable "="
         model-identifier [ ":" unsigned-integer ]
                                       "." output-variable ";" } .
output-variable = scalar-variable | dimensioned-variable .
```

```
pling =
     "COUPLING
         { inpu
     "END COUR
mput-output-re
    model-ident
  [ model-ident
Imput-variable
Doupled Model
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Coupled Model
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coupling =
eger ]
                          "COUPLING FOR" model-identifier
                              { input-output-relationship }
eger ] } .
                          "END COUPLING FOR" model-identifier ";" .
                     input-output-relationship =
                         \verb|model-identifier [":" unsigned-integer] "." input-variable "<--"|
                       [ model-identifier [":" unsigned-integer] "." output-variable ] ";" .
del M. The
..., M:15.
                     input-variable = scalar-variable | dimensioned-variable .
nerated and
                     Coupled Model Formalism of GEST as a Top-Down Model Conception and
                     Stepwise Model Refinement Tool
                     "Coupled Model" formalism provided in GEST, facilitates top-down model
                     conception and stepwise model refinement. Figures 9 a-f show steps of
                     model conception and corresponding GEST modelling statements for the
                     example model given in Figure 7.
to consider
or several
                     In step 1, one specifies the name of the model, the input and output
model is an
                               variables of the model, and their ranges of acceptable val-
                               ues (Figure 9c, 9d).
                    In step 2, the names of the component models are specified (Figure
                               9b).
ut-variable
                    In step 3, each component model is specified separately.
                               can either be specified from scratch or can be fetched from
" }.
                               a model base (Figure 9c).
                    In step 4, the equivalencing of external and internal variables are
                               specified.
                               In this step, an input to the coupled model (i.e., an
";" } .
                               external input to the resultant model) provides values to
```

an input of one or several component models.

Then, one specifies, for every output of the coupled model (i.e., for every external output), the names of the output variable and of the component model which provides the values (Figure 9e).

In step 5, the coupling (i.e., the input/output relationships of the component models) is specified as follows (Figure 9f):

For every component model do

For every input variable do

Specify input-output relationship
Loop
Loop

Some Implications

In a nested coupling at least one component model is a coupled model. Since the resultant model has its input(s) and output(s) declared it can act as a component model in a nested coupling. The concept of nested coupling introduced in GEST in 1970 (Ören 1970) allows both top-down model refinement and bottom-up model synthesis.

Several copies of similar models can be created automatically. For example, suppose that a model called, say "M" has already been specified. If the user wants to create n (to be specific let n=15) replicas of M, in the list of component models all one has to specify is M:1 TO 15. The created n replicas may be identical or similar models depending whether or not they have identical parameter values or not. Furthermore similar models thus created (i.e., replicas of the same generic model) can have same or different specific frames (see section 4.2).

Computer-assistance is straightforward in both specifying and checking the consistencies of coupled models. In a computer-assisted modelling system even some of the checks need not be done manually, due to the guidance of the modelling system. In such a system, for every component system, every input variable is listed (by the system) after the name of the component model. Therefore it is even not possible to

misspell the names thermore if an in-(input of the resufication of input/ in Figure 8, the 1

M.B <--- Z.IN;

has to be generate also the possibil ranges of the value fied, for every (i system can also che set of the range of

Documentation

Due to GEST's welflowcharts of GEST Representation of (Oren et al. 1983 flowchart of the m

Coupling specificatems consisting of documentation mode according to Figurand other input/out

Documentation of structures (input several application large software, or the coupled model
mes of the output
provides the val-

ationships of the
(Pigure 9f):

hip

a coupled model.(s) declared itThe concept ofallows boths.

matically. For eady been specilet n=15) replis to specify is r similar models r values or not.
cas of the same
mes (see section

ing and checking isted modelling ly, due to the or every compotem) after the ot possible to

misspell the names of component models or the input variables. Furthermore if an input variable has been declared as an external input (input of the resultant system) then the system can finish the specification of input/output relationship. For example in the model given in Figure 8, the line

M.B <--- Z.IN; (* EXTERNAL INPUT *)

has to be generated fully by the modelling system, thus eliminating also the possibility of a wrong input/output connection. If the ranges of the values of the input and output variables are also specified, for every (input, output) pair specified in the coupling, the system can also check whether or not the range of the output is a subset of the range of the input and hence detect inconsistencies.

Documentation

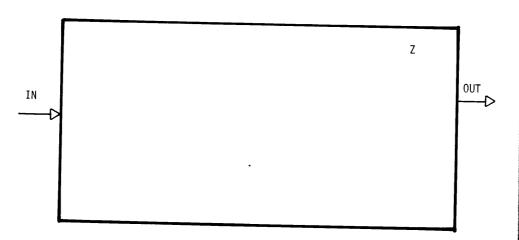
Due to GEST's well-structured nature, computer generated structured flowcharts of GEST models can easily be obtained. ORGEST (Organized Representation of GEST programs) is being implemented for this purpose (Oren et al. 1983). As an example, Figure 10 depicts a structured flowchart of the memoryless model of Figure 5.

Coupling specification can be very useful in the documentation of systems consisting of large number of interacting component systems. A documentation module would display each component model separately according to Figure 11 where external input(s), output(s), feedback and other input/output interface are easily displayed.

Documentation of models specified partially by part of their static structures (input and output variables only) can be very useful in several application areas such as documentation of organizations, large software, or hardware systems.

- STEP 1 Specify: 1) name of the model,
 - 2) input and output variables, and
 - 3) ranges of acceptable values of input and output variables

PICTORIAL REPRESENTATION:



GEST MODELLING:

```
COUPLED MODEL Z

EXTERNALS

INPUT IN;

RANGE OF IN = REAL(>= 0.00, <= 100.00);

OUTPUT OUT;

RANGE OF OUT = TEAL(>= 40.00, < 75.00);

END EXTERNALS;
```

Figure 9a. Step 1 in top-down model conception and step-wise model refinement in GEST $\,$

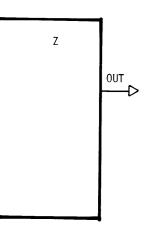
PICTOI DI

GEST M

Figure 9

STEP 2 - Specify names of component models

t and output variables

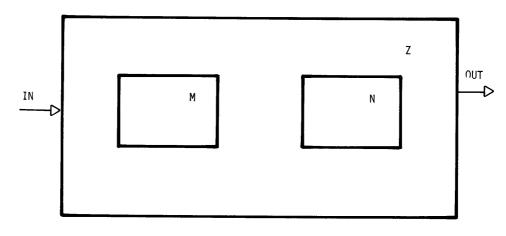


).00);

,00);

step-wise

PICTORIAL REPRESENTATION:

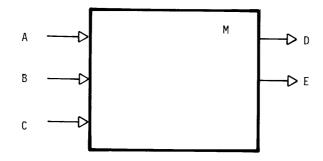


GEST MODELLING:

COMPONENT MODELS M, N;

Figure 9b. Step 2 in top-down model conception and step-wise model refinement in GEST

PICTORIAL REPRESENTATION:



GEST MODELLING:

CONTINUOUS MODEL M;

STATIC STRUCTURE

INPUTS A, B, C; STATE ... OUTPUTS D, E;

• • •

END STATIC STRUCTURE;

DYNAMIC STRUCTURE

DERIVATIVES

...

END DERIVATIVES;

OUTPUT FUNCTION

END OUTPUT FUNCTION;

END DYNAMIC STRUCTURE;

END MODEL M;

Figure 9c. Step 3 in top-down model conception and step-wise model refinement in GEST

PICTORIAL REPS

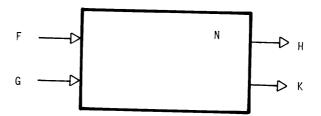
GEST MODELLING

CONT

END I

Figure 9d. Sta

PICTORIAL REPRESENTATION:



GEST MODELLING:

CONTINUOUS MODEL N;

STATIC STRUCTURE

INPUTS F, G; STATES ... OUTPUTS H, K;

. . .

END STATIC STRUCTURE;

DYNAMIC STRUCTURE

DERIVATIVES

• •

END DERIVATIVES;

OUTPUT FUNCTION

. . .

END OUTPUT FUNCTION;

END DYNAMIC STRUCTURE;

END MODEL N;

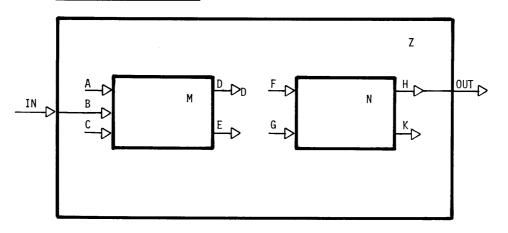
Figure 9d. Step 3 (for the second component model of ${\tt Z}$)

nd step-wise

₽ E

> 2) for every external output corresponding internal output

PICTORIAL REPRESENTATION:



GEST MODELLING:

EQUIVALENCING

INPUTS Z.IN = M.B;

OUTPUTS Z.OUT = N.H;

END EQUIVALENCING;

Figure 9e. Step 4 in top-down model conception and step-wise model refinement in GEST $\,$

PICTORIA B C

TEP 5 - Spec

GEST NO

Figure 9

STEP 5 - Specify

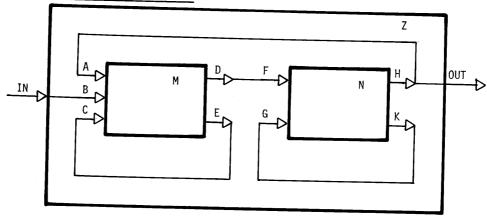
coupling of component models, i.e.,

for every component model for every internal input specify

from which output variable of which component model the values are provided

loop

loop PICTORIAL REPRESENTATION:



GEST MODELLING:

COUPLING FOR Z

M.A <-- N.H; M.B <-- Z.IN; M.C <-- M.E; N.F <-- M.D; N.G <-- N.K; END COUPLING FOR Z;

Figure 9f. Step 5 in top-down model conception and step-wise model refinement in GEST

Z

H

OUT

K

tep-wise

MEMORYLESS MODEL BIRTH RATE											
STATIC STRUCTURE											
INPUTS S, (* MATERIAL STANDARD OF LIVING *) NE, (* EFFECTIVE POLLUTION *) P; (* POPULATION *)											
OUTPUT BIRTH RATE; PARAMETERS K20, K21, K22, K23, K24, K25;											
END STATIC STRUCTURE;											
DYNAMIC STRUCTURE											
B = K20 - K21*S - K22*NE - K23*P;											
IF B >= K24 AND B <= K25											
THEN BIRTH_RATE = B;											
ELSE IF B < K24											
THEN BIRTH_RATE = K24;											
ELSE BIRTH_RATE = K25;											
END IF;											
END IF;											
END DYNAMIC STRUCTURE;											
END MODEL BIRTH_RATE;											

Figure 10. Structured documentation of the memoryless model given in Figure 5 $\,$

COMES FROM:

EXTERNAL

N.H

M.E

Figure 11.

C

			CON	MES FROM	:				
			N.I	Н	Α -	A	MODEL	М]
LIVING	*) *) *)		EXTER	NAL	В		>		
K2 5;			M.E	Ē	С				
				Figure 1	11. Do	ocumentati	on of th	e input/o	utput rel
					is	ne of the s represen	componen ted in F	t models (igure 6)	of a coup
K24;									
K2 5;									

memoryless

CONNECTED TO: **→** D N.F ÐE M.C

lationships of oled model (which

3.5 Model Parameter Sets

In a parameter set basically two things are done: 1) The values of the model parameters are specified and 2) The tabular functions used in a model are defined point by point. There are four possibilies for the specification of model parameter sets, i.e., specification of single or multiple parameter set for a model consisting of one or several component models. Examples of model parameter set specifications are included in the system models given in section 5. It is also possible to specify discontinuous tabular functions. For every discontinuity point, two points have to be given with the same abscissa as follows:

(Xc,Yl) / (Xc,Yr)

where

Xc is the common abscissa

Yl is the left-hand value of the ordinate

Yr is the right-hand value of the ordinate

In a computer-aided documentation system two- or three-dimensional tabular functions can also be displayed graphically for the user's convenience. Graphic display of the tabular functions may also help the user to detect some of the specification errors.

4. EXPERIMENTATION

4.1 Basics

The specification of the experiments, as shown in Figure 12, may comprise up to three sections which are:

- (1) experimental frames
- (2) model/frame pairs (or simulation runs)
- (3) post study section

End exper

En

Experim

E

Figure 12.

1) The values of the r functions used in a r possibilies for the cification of single of one or several st specifications are It is also possible r every discontinuity

three-dimensional
ally for the user's
ctions may also help
s.

gigure 12, may com-

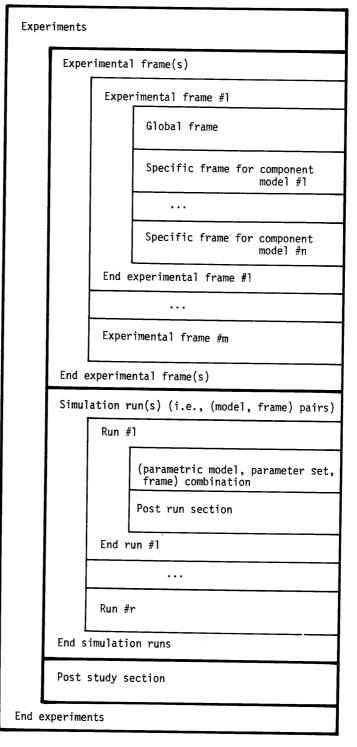


Figure 12. Elements of specifications of experiments in GEST

An experimental frame specifies the simulation experiments. It can be conceived of having two parts which are global frame and specific frame.

In the global frame, overall specifications such as time unit declaration, termination condition specification, etc, are given.

Specific frames given for every component model separately, include initialization of the state variables, data collecting requirements, and specification of communication intervals and input values.

A model-frame pair specifies the combination of the parametric model, the parameter set, and the experimental frame to be used in a simulation study. It also includes a post run section.

The post run section includes specification of the aditional computations to be performed after the simulation and outputting the results of a simulation run. The post study section resembles to a post-run section, with an additional level of generalization. In a post-study section, one can refer to data generated during different simulation runs. The output module consists of the specifications for displaying the results of the simulation study on different types of output units. Examples are included in the three system models given in section 5.

4.2 BNF Definitions

Some relevant definitions in BNF follow:

```
experiment =
    { experimental-frame }
    { model-frame-pair } .
```

single multip ingle-expe "PRAM " END multiple-ex "MULT "END global-frame "GLOBAL" teri inte

{

{ .

time

acti para

data

inte

COM rena "END GLOE

```
me and specific
                                single-experimental-frame
                              | multiple-experimental-frame .
me unit declara-
                           single-experimental-frame =
ven.
                                 "FRAME" identification "FOR" model-identifier
rately, include
                                      global-frame
ng requirements,
values.
                                    { specific-frame }
rametric model,
                                 "END FRAME" identification ";" .
sed in a simula-
                           multiple-experimental-frame =
itional computa-
                                 "MULTIPLE FRAME" multiple-identification
ing the results
                                          "FOR" model-identifier
s to a post-run
                                      global-frame
In a post-study
rent simulation
                                    { specific-frame }
for displaying
ypes of output
                                 "END MULTIPLE FRAME" multiple-identification ";" .
s given in sec-
                           global-frame =
                              "GLOBAL"
                                   time-unit-declaration
                                 | termination-condition
                                 | integration
                                 | activation-of-discrete-models
                                 | parameter-asignment
                                 | data-for-tabular-function
                                 | interpolation-type
                                 | communication-interval
                                 | renaming-declaration
```

"END GLOBAL" ";" .

experimental-frame =

ents. It can be

```
specific-frame =
   "MODEL" model-identifier
            [ ":" unsigned-integer "TO" unsigned-integer ]
        parameter-assignment
      | data-for-tabular-function
      | interpolation-type
      | communication-interval
      | renaming-declaration
      | initialization
      | input-scheduling
      | activation-of-discrete-model
      | output-sampling
      | data-collecting
   "END MODEL" model-identifier ";" .
model-frame-pair =
    single-run
  \mid multiple-run [ post-study-specification ] .
single-run =
   "RUN" identification
        "TO OBSERVE MODEL" model-identifier
      [ "WITH PARAMETER SET" identification ]
        "IN FRAME" identification
      [ "WITH POST RUN"
            { statement | output-module-reference }
        "END POST RUN" ";" ]
   "END RUN" identification ";" .
Examples:
      RUN 1 TO OBSERVE MODEL POPULATION GROWTH
            WITH PARAMETER SET HIGH_BIRTH RATE
             IN FRAME LOW EMPLOYMENT;
      END RUN 1;
      RUN 7 TO OBSERVE MODEL EVAPORATION_FROM_SOIL
            WITH PARAMETER SET CLAY
            IN FRAME RAINY SEASON ;
      END RUN 7;
```

EXAMPLES:

f them comment f variables of

Example 1

Example 2

Example 3

5. EXAMPLES:

eger]

The following examples of complete GEST programs are provided. In all of them comments are kept at a minimum level, i.e., to provide a list of variables only.

Example 1 - DEER POPULATION

Study consists of:

One component model
One parameter set, and
One experimental frame

Example 2 - EVAPORATION FROM SOIL

Study consists of:

One component model
One parameter set, and
One experimental frame

Example 3 - MOTOR CONTROLLER

Study consists of:

A coupled model
One parameter set, and
One experimental frame

PROGRAM STUDY OF DEER POPULATION

(* This model is adopted from: P.W. House and J. McLeod (1977). Large-scale models for policy evaluation. Wiley-Interscience, New York, pp. 148-153 *)

CONTINUOUS MODEL DEER_POPULATION

STATIC STRUCTURE

STATE DP; (* DEER POPULATION OUTPUT DP, PP, DKPP; AUXILIARY VARIABLES DNI, (* DEER NET INCREASE DPR, (* DEER PREDATION RATE DD; (* DEER DENSITY PARAMETERS AREA, NIR; (* NET INCREASE RATE TABULAR FUNCTIONS PPT, (* PREDATOR POPULATION TABLE DKPPT; (* DEER KILL PER PREDATOR TABLE *) INTERPOLATIONS PP, (* PREDATOR POPULATION DKPP; (* DEER KILL PER PREDATOR *) PP = PPT(TIME);DKPP = DKPPT(DD);

DYNAMIC STRUCTURE

END STATIC STRUCTURE;

DERIVATIVES

DP' = DNI - DPR; DNI = NIR*DP; DPR = PP*DKPP; DD = DP/AREA; END DERIVATIVES; END DYNAMIC STRUCTURE;

END INTERPOLATIONS;

END MODEL DEER POPULATION;

AREA = 8000 TABULAR FU (* GIVE (1880., END TABULAR TABULAR FUN

(* GIVE

(0.0,

PARAMETER SET 1

(0.015, END TABULAR END PARAMETER SI

FRAME 1 FOR DEL

*)

*)

*)

*)

*)

*)

*)

GLOBAL. TIME UNI SIMULATE INTEGRAT END GLOBAL; MODEL DEER P INITIALI SAVE DP. INTERPOL

RUN 1 TO OBSERVE WITH POST RU OUTPUT M END POST RUM

END FRAME 1;

END MODEL DE

OUTPUT MODULE 1 PRINT 1 HEADI STUDY OF DEER PLOT DP, PP,

END RUN 1;

END OUTPUT MODULE END PROGRAM STUDY_OF

```
PARAMETER SET 1 FOR DEER POPULATION
      AREA = 800000.0; NIR = 0.2;
      TABULAR FUNCTION PPT WITH 2 POINTS
                      - PREDATOR POPULATION AS A FUNCTION OF TIME *)
          (* GIVES PP
          (1880., 300.) (1960., 300.)
     END TABULAR FUNCTION PPT;
     TABULAR FUNCTION DKPPT WITH 6 POINTS
          (* GIVES DKPP - DEER KILL PER PREDATOR
                         AS A FUNCTION OF DD - DEER DENSITY
                                                              *)
                  0.0) (0.005, 3.0) (0.010, 13.0)
         (0.0,
         (0.015, 32.0) (0.020, 51.0) (0.025, 56.0)
     END TABULAR FUNCTION DKPPT;
 END PARAMETER SET 1;
 FRAME 1 FOR DEER POPULATION
     GLOBAL
         TIME UNIT IS YEAR
         SIMULATE UNTIL TIME = 1970, START TIME = 1880;
         INTEGRATE BY RUNGE KUTTA, REL_ERROR = 0.001;
     END GLOBAL;
    MODEL DEER POPULATION
         INITIALIZE STATE DP = 4000.;
        SAVE DP, PP, DKPP AT EVERY YEAR ;
         INTERPOLATION LINEAR PP, DKPP;
    END MODEL DEER POPULATION;
END FRAME 1;
RUN 1 TO OBSERVE MODEL DEER POPULATION WITH PARAMETER SET 1 IN FRAME 1
    WITH POST RUN
        OUTPUT MODULE 1 ON PRINTER:
    END POST RUN;
END RUN 1;
OUTPUT MODULE 1
    PRINT 1 HEADING LINE;
   STUDY OF DEER POPULATION
    PLOT DP, PP, DKPP VERSUS TIME;
END OUTPUT MODULE 1;
```

END PROGRAM STUDY_OF_DEER_POPULATION;

*)

*)

*)

*)

*)

*)

*)

ON TABLE

ON

DATOR

DATOR TABLE

```
PROGRAM STUDY OF EVAPORATION FROM SOIL
```

(* This model is adopted from:

C.F. Shaykewich and L. Stroosnijder (1977).

The concept of matric flux potential applied to simulation of evaporation from soil. Neth. J. Agric. Sci., PP. 63-82.

GEST 78 Version of this model appeared in Oren and Den Dulk 1978.

(To ease the comparison with the original version,

the units used in the original version are kept.

However, for SI units, note that 1 mbar = 100 Pascal)

LIST OF IDENTIFIERS:

- WATER VAPOR PRESSURE IN ATMOSPHERE (MBAR) (MILLIBAR)

EC - WATER VAPOR PRESSURE AT SOIL SURFACE

> (CURRENT PRESSURE) (MBAR)

ES - WATER VAPOR PRESSURE AT SOIL SURFACE

> (AT SATURATION) (MBAR)

F - FACTOR ACCOUNTING FOR THE EFFECT OF

> WIND ON EVAPORATION (CM/DAY.MBAR)

FΚ - HYDRAULIC CONDUCTIVITY AS A FUNCTION

WATER CONTENT

FLW - FLUX OF WATER (CM**3/(CM**2),DAY)

FLW(1) - EVAPORATION (I.E. FLOW FROM TOP COM-

PARTMENT (CM**3/(CM**2),DAY)

FPSI - PSI AS A FUNCTION OF WATER CONTENT

- HYDRAULIC CONDUCTIVITY K(-) (CM/DAY)

MFLP(-) - MATRIX FLUX POTENTIAL (CM**3/DAY) * -1

- MFLP AS A FUNCTION OF WATER CONTENT MFLPT

PSI(-) - WATER POTENTIAL (CM H2Ø) * 1

RDF(-) - RECIPROCAL OF THE DISTANCE BETWEEN

CENTRES OF COMPARTMENTS (1/CM)

RTC(-) - RECIPROCAL OF COMPARTMENT THICKNESS (1/CM)

TCM(-) - COMPARTMENT THICKNESS (CM)

TEVAP - ACCUMULATED EVAPORATION (CM)

W(-) - WATER CONTENT (FRACTION) (CM**3/CM**3)

COMMENT ON THE PHYSICAL LAW FOR FLUX:

ALL FLUXES ARE CALCULATED WITH DARCY'S LAW FOR

VERTICAL FLOW OF WATER IN THE SOIL:

 $FLUX = COND * ((-D_PSI/D_Z) -1)$

CONTINUOUS MODEL

STATIC STUCT

STATE

TEVA

W(1..

OUTPUT

TEVA

W(1..

PSI (1

K(1..

PLW(1

AUXILIAR

PARAMETE

AUXILIAR

TCM (]

RTC (1

RDF (1

FOR I

LOOP

RDF (1

FOR 1

LOOP

END AUXII

TABULAR I

FK,

FPSI,

MFLP

CONTINUOUS MODEL EVAPORATION FROM SOIL

led to simulation

Sci., PP. 63-82.

(MBAR) (MILLIBAR)

version,

100 Pascal)

kept.

E

(MBAR)

(MBAR)

(CM/DAY)

(1/CM)

(1/CM)

(CM)

(CM)

FOR

(CM/DAY.MBAR)

(CM**3/(CM**2),DAY)

(CM**3/(CM**2),DAY)

(CM**3/DAY) * -1

(CM H2Ø) * 1

(CM**3/CM**3)

*)

Oren and Den Dulk 1978.

```
STATIC STUCTURE
    STATE
                        (* ACCUMULATED EVAPORATION
                                                         *)
        W(1..18);
                         (* CURRENT WATER CONTENT
                                                         *)
   OUTPUT
       TEVAP,
                        (* ACCUMULATED EVAPORATION
                                                         *)
       W(1..18),
       PSI(1..8),
                        (* WATER POTENTIAL
                                                         *)
       K(1..8),
                        (* HYDRAULIC CONDUCTIVITY
       FLW(1);
                        (* FLUX OF WATER FROM
                           TOP COMPARTMENT, I.E.
                           EVAPORATION
                                                         *)
   AUXILIARY VARIABLE FLW(1..19), K(1..19),
                            MFLP(1..18), PSI(1..18);
   PARAMETER
       TCM(1..18);
                       (* COMPARTMENT THICKNESS
                                                         *)
   AUXILIARY PARAMETERS
       RTC(1..18),
                        (* RECIPROCAL OF COMPARTMENT
                           THICKNESS
                                                         *)
       RDF (1..18);
                        (* RECIPROCAL OF THE DISTANCE
                           BETWEEN CENTERS OF
                          COMPARTMENTS
                                                        *)
      FOR I=1 TO 18 DO
          RTC(I) = 1.0/TCM(I);
      LOOP
      RDF(1) = RTC(1);
      FOR I=2 TO 18 DO
          RDF(I) = 2.0 / (TCM (I-1) + TCM (I));
      LOOP
  END AUXILIARY PARAMETERS;
  TABULAR FUNCTIONS
      FK,
            (* HYDRAULIC CONDUCTIVITY AS
                A FUNCTION OF WATER CONTENT
                                                       *)
      FPSI, (* PSI AS A FUNCTION OF WATER CONTENT
                                                       *)
```

MFLPT; (* MFLP AS A FUNCTION OFWATER CONTENT

*)

```
INTERPOLATIONS
         K(I) = FK(W(I));
         PSI(I) = FPSI(W(I));
         MFLP(I) = MFLPT(W(I));
     END INTERPOLATIONS;
 END STATIC STRUCTURE;
 DYNAMIC STRUCTURE
     DERIVATIVES
         TEVAP' = FLW(1);
         FOR I = 1 TO 18 DO
             W(I)' = (FLW(I+1) - FLW(I))*RTC(I);
         LOOP
            (* CALCULATION OF EVAPORATION
                (I.E. FLOW FROM TOP COMPARTMENT = FLW(1))
               EQUATION IS:
               EVAPORATION = F*(EC-EA)/(ES-EA)
               F
                        = 0.8 CM/DAY (DEPENDS ON WINDSPEED)
                         = 31.45 MBAR (25C, AT SATURATION)
               ES
               EΑ
                         = 7.06 MBAR (20C, 30] RELATIVE HUMIDITY)
               F/(ES-EA) = \emptyset.8/(31.45-7.06) = \emptyset.0328
               EC
                       = ES/EXP(PSI*7.127E-7)
                                                            *)
        FLW(1) = MAX (0.0,
                        0.0328*(31.45/EXP(7.127E-7 * PSI(1)) - 7.06)
            (* CALCULATION OF FLUX, USING WATER POTENTIAL
               AND HYDRAULIC CONDUCTIVITY INDEPENDENTLY *)
        FOR I = 2 TO 18 DO
            FLW(I) = (RDF(I) * (PSI(I-1) - PSI(I)) - 1.)
                                          * (K(I-1) + K(I))/2.0;
        LOOP
        FLW(19) = \emptyset.\emptyset;
    END DERIVATIVE;
END DYNAMIC STRUCTURE;
```

END MODEL EVAPORATION FROM SOIL;

(*

کد (5.

(5.

PARAME

```
PARAMETER SET 1 FOR EVAPORATION FROM SOIL
   TCM(1..18) = 5*1.0, 5*1.5, 3*2.5, 4*5.0, 10.0;
   TABULAR FUNCTION FK
                                 WITH 17 POINTS
       (* GIVES THE HYDRAULIC CONDUCTIVITY K(-)
      AS A FUNCTION OF WATER CONTENT W(-)*)
       (0.03
               ,2.4E-10)(0.06 ,2.4E-9)(0.085 ,2.4E-8)(0.12 ,2.4E-7)
       (\emptyset.145 , 2.4E-6)(\emptyset.175 , 2.4E-5)(\emptyset.19 , 6.\emptysetE-5)(\emptyset.205 , 2.4E-4)
       (0.2175 ,6.0E-4)(0.235 ,2.4E-3)(0.25 ,6.5E-3)(0.27 ,2.4E-2)
       (\emptyset.2925, 1.0E-1)(\emptyset.305, 2.4E-1)(\emptyset.33, 9.0E-1)(\emptyset.35, 2.4)
               ,7.0)
   END TABULAR FUNCTION FK;
   TABULAR FUNCTION FPSI WITH 13 POINTS
       (* GIVES THE MATRIX WATER POTENTIAL (*-1) PSI(-)
      AS A FUNCTION OF WATER CONTENT W(-)*)
      (Ø.01 ,1.0E7 )(Ø.04 ,1.0E6)(Ø.095 ,1.0E5 )(Ø.135 ,2.7E4 )
       (0.165 ,1.0E4 )(0.2075 ,2.0E3 )(0.225,1.0E3 )(0.24 ,700.0 )
       (0.275 , 300.0)(0.32 ,100.0)(0.37 ,10.0 )(0.39 , 1.0)
       (0.41, -600.0)
   END TABULAR FUNCTION FPSI;
   TABULAR FUNCTION MFLPT WITH 30 POINTS
       (* GIVES THE MATRIC FLUX POTENTIAL (* 1) MFLP(-)
      AS A FUNCTION OF WATER CONTENT W(-)*)
               ,43.0 )(0.144 ,42.688)(0.165 ,42.698)(0.1785,42.468)
       (0.189 ,42.348)(0.197 ,42.24 )(0.2075 ,42.14 )(0.216 ,41.88 )
      (0.2275 ,41.65 )(0.239 ,41.0 )(0.245 ,40.1 )(0.2525,39.68 )
      (0.261 ,38.88 )(0.268 ,37.38 )(0.274 ,35.94 )(0.277 ,34.58 )
```

```
(Ø.189 ,42.348) (Ø.197 ,42.24 ) (Ø.2075 ,42.14 ) (Ø.216 ,41.88 ) (Ø.2275 ,41.65 ) (Ø.239 ,41.0 ) (Ø.245 ,40.1 ) (Ø.2525,39.68 ) (Ø.261 ,38.88 ) (Ø.268 ,37.38 ) (Ø.274 ,35.94 ) (Ø.277 ,34.58 ) (Ø.281 ,33.68 ) (Ø.284 ,32.64 ) (Ø.2875 ,31.4 ) (Ø.292 ,29.9 ) (Ø.297 ,27.7 ) (Ø.299 ,24.9 ) (Ø.301 ,23.2 ) (Ø.303 ,21.4 ) (Ø.307 ,19.0 ) (Ø.309 ,16.2 ) (Ø.313 ,13.1 ) (Ø.3165, 9.5 ) (Ø.32 ,5.3 ) (Ø.34 ,Ø.0 )
```

END PARAMETER SET 1;

PLW(1))

WINDS PEED)

TURATION)

OTENTIAL

) - 1.)

) + K(I))/2.0;

DENTLY *)

28

LATIVE HUMIDITY)

*)

* PSI(1)) - 7.06));

```
FRAME 1 FOR EVAPORATING FROM SOIL
```

GLOBAL

SIMULATE UNTIL TIME = 5.0; INTEGRATE BY RUNGE_KUTTA; END GLOBAL;

MODEL EVAPORATION FROM SOIL

INITIALIZE STATES

TEVAP = \emptyset .; W(1..18) = $18*\emptyset.2925$;

COMMUNICATE AT EVERY 0.25 TIME UNIT;

SAVE W(1..16), PSI(1..8), K(1..8), FLW(1), TEVAP;

INTERPOLATION LINEAR K, PSI, MFLP;

END MODEL EVAPORATION FROM SOIL;

END FRAME 1;

RUN 1 TO OBSERVE MODEL EVAPORATION_FROM_SOIL
WITH PARAMETER SET 1 IN FRAME 1
WITH POST RUN
OUTPUT MODULE 1 ON PRINTER
END POST RUN
END RUN 1

OUTPUT MODULE 1

PRINT FOR FIRST PAGE 1 HEADING LINE;

STUDY OF EVAPORATION FROM SOIL - VERSION 1

LIST TIME, W(1..16), PSI(1..8), K(1..8), FLW(1);

PLOT TEVAP VERSUS TIME;

PLOT FLW(1) VERSUS TIME WHILE (TIME <= 1.0);

PLOT W(1) VERSUS TIME WHILE (TIME <= 0.5);

END OUTPUT MODULE 1;

END PROGRAM STUDY_OF_EVAPORATION_FROM_SOIL;

PROGRAM ST

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```
PROGRAM STUDY_OF_MOTOR_CONTROLLER
```

(* This model is adapted from:
 Elmquist, H. (1975). SIMNON User's Manual,
 Report 7502, Dept. of Automatic Control,
 Lund Institute of Technology, Sweden *)

COUPLED MODEL MOTOR_CONTROLLER
EXTERNAL

INPUT YREF;

END EXTERNAL;

COMPONENT MODELS PID_CONTROLLER, MOTOR;

CONTINUOUS MODEL PID_CONTROLLER;

STATIC STRUCTURE

INPUTS YREF, Y;

STATES I, X;

OUTPUT U;

AUXILIARY VARIABLES E, P, D;

PARAMETERS G, GD, TD, TI;

END STATIC STRUCTURE;

DYNAMIC STRUCTURE

DERIVATIVES

I' = E/TI;

X' = -GD/TD*(X - Y);

E = YREF - Y;

END DERIVATIVES;

OUTPUT FUNCTION

U = P+I+D;

 $P = G \star E;$

D = -GD*(Y - X);

END OUTPUT FUNCTION;

END DYNAMIC STRUCTURE; END MODEL PID_CONTROLLER;

), TEVAP;

1);

```
CONTINUOUS MODEL MOTOR
        STATIC STRUCTURE
           INPUT U;
           STATES TH, THDOT;
           OUTPUT Y;
           AUXILIARY VARIABLES ME, I;
           PARAMETERS KM, R, J, CT;
        END STATIC STRUCTURE;
        DYNAMIC STRUCTURE
           DERIVATIVES
              TH' = THDOT;
              THDOT' = ME/J;
              ME
                     = KM*I;
                     = (U-KM*THDOT)/R;
           END DERIVATIVES;
           OUTPUT FUNCTION
              Y = CT*TH;
           END OUTPUT FUNCTION;
        END DYNAMIC STRUCTURE;
    END MODEL MOTOR;
END COMPONENT MODELS;
EQUIVALENCING
   INPUTS
      MOTOR CONTROLLER.YREF = PID_CONTROLLER.Y_REF;
END EQUIVALENCING;
COUPLING FOR MOTOR CONTROLLER
    PID_CONTROLLER.YREF <--- MOTOR_CONTROLLER.YREF;
                                    (* EXTERNAL INPUT *)
    PID_CONTROLLER.Y <--- MOTOR.Y;
   MOTOR.U
                        <--- PID CONTROLLER.U;
END COUPLING FOR MOTOR_CONTROLLER;
```

END MODEL MOTOR_CONTROLLER ;

END

PRN

END I

```
PARAMETER SET 1 FOR MOTOR_CONTROLLER
```

```
MODEL PID_CONTROLLER
       G = 1.0;
       GD = 1.0;
       TD = 1.0;
       TI = 1.E10;
    END MODEL PID_CONTROLLER;
    MODEL MOTOR
       KM = 6.2 E-3;
       R = 5.3;
       J = 7.5 E-7;
       CT = \emptyset.033;
    END MODEL MOTOR;
END PARAMETER SET 1 ;
FRAME 1 FOR MOTOR_CONTROLLER
   GLOBAL
      TIME UNIT IS SECOND;
      SIMULATE UNTIL TIME = 5.0;
      INTEGRATE BY RUNGE KUTTA, REL_ERROR = 0.0001;
      COMMUNICATE AT EVERY Ø.01 SECOND;
   END GLOBAL;
   MODEL PID CONTROLLER
      INITIALIZE STATES TO ZERO;
      SAVE U;
   END MODEL PID_CONTROLLER;
   MODEL MOTOR
      INITIALIZE STATES
         TH = \emptyset.\emptyset;
         YHDOT= \emptyset.\emptyset;
      SAVE Y;
   END MODEL MOTOR;
END FRAME 1;
```

R.Y_REF;

R. YREF;

.U;

RNAL INPUT *)

RUN 1 TO OBSERVE MODEL MOTOR_CONTROLLER
WITH PARAMETER SET 1 IN FRAME 1;

WITH POST RUN
OUTPUT MODULE 1 ON PRINTER;
END POST RUN;
END RUN 1;

OUTPUT MODULE 1

PRINT FOR FIRST PAGE 1 HEADING LINE;
STUDY OF MOTOR_CONTROLLER
PLOT AND LIST U, V VERSUS TIME;

END OUTPUT MODULE 1;

END PROGRAM STUDY_OF_MOTOR_CONTROLLER;

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- Bleha, L.J. (197 Combined Dig versity of O
- Dogbey, F. (1984 continous-Che of Simulation Ottawa, Ont.,
- Elzas, M.S. (1979) odology in S Elzas, G.J. I 57-91.
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APPEND

- Terminal symbol
 tion marks and
- Non-terminal sycase characters
- When a non-termis used between
- A blank separat
- A period "." in
- Left and right equivalence sym from."
- Exclusive or is
- Parentheses "(
- Square brackets rence.
- Curly brackets occurences.
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Partial Models. **arge-**Scale Sysor Cybernetics,

APPENDIX: THE METALANGUAGE USED TO DEFINE GEST 81

- Terminal symbols of the GEST 81 language are enclosed within quotation marks and are written in UPPER CASE CHARACTERS.
- Non-terminal symbols of the GEST 81 language are written in lower case characters.
- When a non-terminal symbol requires more than one word, hyphen "-" is used between-the-words.
- A blank separates two syntactic units.
- A period "." indicates end of a rule.
- Left and right sides of any rule of the grammar are separated by the equivalence symbol "=" which can be read "is" or "can be formed from."
- Exclusive or is represented by the symbol "|" which can be read "or"
- Parentheses "()" indicate grouping without repetition.
- Square brackets "[]" indicate option, that is, zero or one occurence.
- Curly brackets "{ }" indicate repetition, that is, one or more occurences.
- Zero or more occurences of a syntatic unit is represented by a combination of square and curly brackets, i.e., by "[{ $}$]".

Simulation and Model-Based Methodologies: An Integrative View

Edited by

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Chapter 3

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