

CSI2101 PRACTICE EXERCISES - PROPOSITIONAL LOGIC

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For each propositional formula (also called *compound proposition* in Rosen textbook) below, solve the following exercises:

- (1) Write its truth table.
- (2) Write an equivalent formula in disjunctive normal form (DNF), i.e. *disjunction* (= *or's*) of *terms* (= *conjunctions of literals*).
- (3) Write an equivalent formula in conjunctive normal form (CNF), i.e. *conjunction* (= *and's*) of *clauses* (= *disjunctions of literals*).
- (4) Write an equivalent formula that only uses connectives in $\{\wedge, \neg\}$.
- (5) Write an equivalent formula that only uses connectives in $\{\vee, \neg\}$.
- (6) Construct logic gates (and-gate, or-gate, inverter) that computes a boolean function represented by each of the above propositions.
- (7) Prove that the original formula is logically equivalent to the DNF (CNF) one by using logical equivalences.

Some formulas for you to practice:

- $(p \vee q) \rightarrow (p \oplus q)$
- $(x \vee y) \rightarrow (\neg x \wedge z)$
- $(p \leftrightarrow q) \oplus (\neg p \leftrightarrow q)$
- Choose others from the textbook...