

## Bluetooth scatternet formation

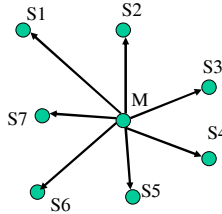
Tutorial 3

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## Bluetooth - piconet

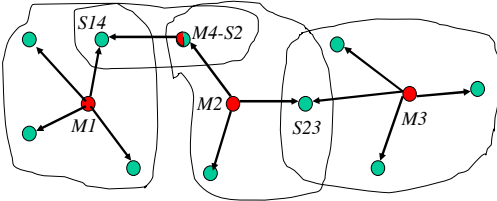
- Short-range
- Master-slave
- Frequency hopping
- PICONET = master + K slaves,  $K \leq 7$
- Additional slaves must be parked



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## Bluetooth - scatternet



Connect piconets into scatternet

Avoid master-slave bridges

Bridges participate in piconets on time division basis

Minimize number of slave roles and # of masters <sup>3</sup>

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## Scatternet in single-hop networks

- Salonidis, Bhagwat, Tassioulas, LaMaire 2001: centralized, max 36 nodes
- Law, Mehta, Siu 2001: growing one tree
- Tan et al MIT 2001: growing trees
- Sun, Chang, Lai 2002: search trees; Bluetooth IDs as keys; overhead for scatternet merge/maintenance
- Cgun-Choong, Kee-Chaing 2002: Bluerings
- Baatz, Bieschke, Frank, Martini, Scholz 2002: 1-factors, piconets not degree limited
- Miorandi, Zanella 2002: centralized, traffic known a priori
- Barriere, Fraignaud, Narayanan, Opatmy 2003: Projective geometry, connected degree limited

*Large overhead for construction and maintenance in all cases*

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## Scatternets for multi-hop networks

- Growing trees (overhead)
  - Ramachandran, Kapoor, Sarkar, Aggarwal 2000
  - Zaruba, Basagni, Chlamtac 2001
- Clustering based, no degree limit or not connected:
  - Basagni, Chlamtac, Petrioli 2001
  - Balaji, Kapoor, Nanavati, Ramachandran 2001
  - Wang, Thomas, Haas 2002
  - Guerin, Kim, Sarkar 2002
- Guerin, Sarkar, Vergetis 2002: DFS, BFS, MST 2-D, 3-D
- Ajmone-Marsan, Chiasserini, Nucci, Carello, Giovanni 2002: centralized, traffic known in advance
- Clustering based: connected, piconets degree limited, but # of slave roles not limited: Petrioli and Basagni 2002
- + Position information, connected, fully degree limited
  - Li and Stojmenovic 2001 <sup>5</sup>
  - Stojmenovic 2002 <sup>5</sup>

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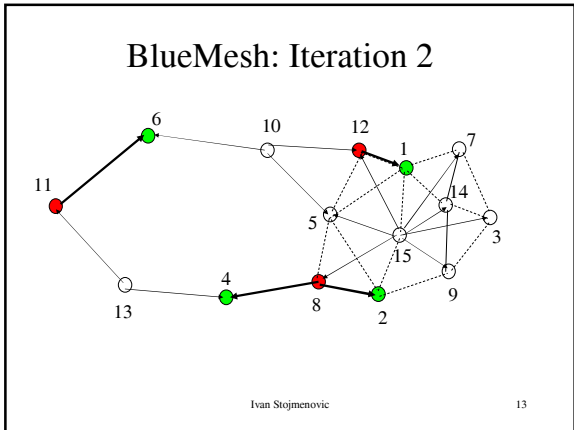
## Scatternet by growing tree

- Ramachandran, Kapoor, Sarkar, Aggarwal 2000: grow tree from root, master not always directly connected to its slave
- Zaruba, Basagni, Chlamtac 2001: grow tree from root, at most 5 slaves per master; if >5, select two connected slaves, link them, and disconnect one; Multiple blueroots extension
- *Communication overhead and Scatternet maintenance?*
- *Tree has root as communication bottleneck*

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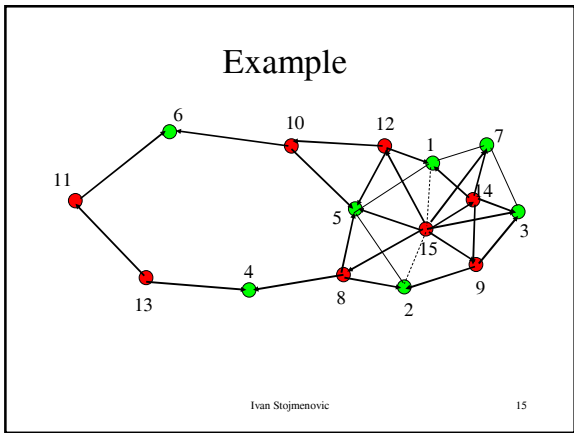




### MIS based BSF (Stojmenovic)

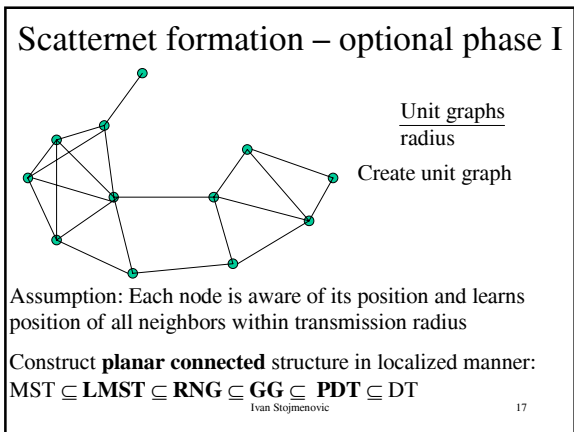
- MIS = maximal independent set: each node is in MIS or is a neighbor of node from MIS, no two nodes from MIS are neighbors
- Finding MIS: repeatedly pick up a neighbor A and eliminate all common neighbors with A
- Iteration 1: each node creates piconet by selecting MIS of its neighbors as slaves, plus adding more up to 7
- Iteration 2: Following clustering methodology, each node decides whether or not its piconet is needed for connectivity
- Same problem: # of slave roles is not limited

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### Degree limited connected scatternet formation

- Li, Stojmenovic, Wang 2001 – clustering based
- Stojmenovic 2002 – dominating set based
- *Phase I* = create unit graph and (optional) construct a planar connected structure in localized manner
- *Phase II* = eliminate some edges in the structure to **limit the degree** of each node to 7
- *Phase III* = **decide master-slave roles** between two nodes of each edge in the structure
- Phases II and III **iterative** (node by node) or concurrently by all nodes **simultaneous** approach)
- Phase III **during** or Ivan Stojmenovic **after** Phase II 16



### Sparse graphs: LMST and RNG

**LMST** – each node constructs Local MST (from local edges); keep edge if it belongs to MSTs of both endpoints

**RNG** – Relative Neighborhood Graph (Toussaint 1980): Keep edges which are not longest in any triangle

Unique edge weights:  
 $w(AB) = (|AB|, \min(ID(A), ID(B)), \max(ID(A), ID(B)))$

Each node in LMST and RNG with unique edge weight has degree < 6

RNG has average degree < 2.4 = sparse

LMST has average degree 2.04, < 3% more edges than MST

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### Gabriel graph

Gabriel graph  $GG(S)$  contains an edge  $(U,V)$  iff the disk with diameter  $(U,V)$  contains no other point from  $S$

Computing  $GG$  from unit graph requires no message exchange  
Some nodes may have high degrees

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### $RNG \subseteq GG$

- $uv \in RNG \rightarrow$  no  $w, uw < uv, vw < uv \rightarrow$  disk with diameter  $uv$  has no node  $\rightarrow uv \in GG$

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### Partial Delaunay Triangulation

Li, Stojmenovic 2001  
Delaunay Triangulation = dual Voronoi diagram

$UV$  in DT iff there exist a circle with chord  $UV$  without other nodes inside it

Test disk with diameter  $UV$ :  
If empty then  $UV$  in PDT  
If nodes inside disk on both sides then not in PDT  
Find smallest angle on both sides of  $UV$   
If together  $\geq \pi$  then not in PDT  
If together  $< \pi$  then in PDT iff both are neighbors, using 1-hop or 2-hop info

PDT= portion of DT which can be decided locally

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### Yao graph – Phase II

$k=7$

Divide into  $k$  equal cones around  $u$   
Find closest point in each cone, if any

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### Limiting degrees – cluster based

**Phase 2:** Applied on **active** nodes = nodes with highest keys among undecided neighbors

- apply Yao construct
- assign role to itself
- marks itself decided
- contacts neighbors about deleted edge or its role

graph remains undirectional

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### Deciding master-slave roles

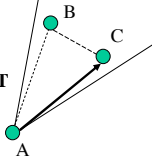
- Key= Bluetooth ID (one-hop neighbor discovery)
- Key= (degree, ID) (two-hop neighbor information)
- Active node decides on roles on each undeleted edge:
- Higher original key, or
- Clustering based: if undecided or any master role assigned  $\rightarrow$  master role, otherwise slave role to itself
- Variant: if any slave role  $\rightarrow$  slave role

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## Yao construct preserves connectivity

- Sort all edges of unit, GG or RNG or PDT by  $w(AB) = (|AB|, \min(ID(A), ID(B)), \max(ID(A), ID(B)))$ .
- Construct MST by considering edges in increasing order, include if no cycle created (Kruskal's scheme)

If AB not in Yao then  $\exists C, AC$  in Yao,  
 $AB < AC$ ,  
 $BC < AB$  (angle  $< \pi/6$ )  
 $\Rightarrow BC, AC$  already considered for MST  
 and connected,  
 $\Rightarrow AB$  not needed in MST  
 $\Rightarrow$  MST is included in Yao

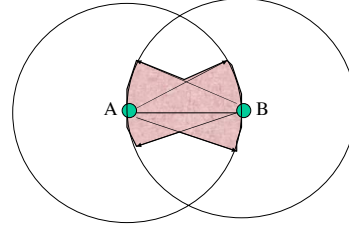


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## Yao bidirectional edges is connected

- Contains RNG as subgraph (Wang, Li 2002)
- Unique edges enforced on the graph by  $w(AB)$



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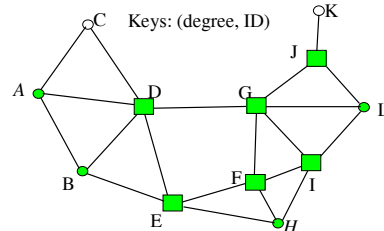
## Dominating set based master-slave roles

- Phase 2 applied on each node simultaneously
- Phase 3: assigning roles to endpoints of each edge
- Localized maintenance
- Solution 3:
  - find a **dominating set**,
  - key=(dominating, degree, id)
  - higher key node on each edge is master
  - Two non-dominating nodes may not be connected
  - Nodes in dominating set only can be masters

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## Dominating sets



Keys: (degree, ID)

Wu, Li '99

Higher degree priority: [SSZ]

Localized maintenance;  
No communication overhead

C,K not intermediate = any two neighbors connected

A,B,H,L not inter-gateway = covered by a neighbor

Any path via H can be replaced by a path via F (EHI  $\rightarrow$  EFI)

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Gateway nodes = not covered by two connected neighbors

## Avoiding position information ?

- Single-hop networks: **virtual positions** (Wang, Li, Stojmenovic 2004)
- MST can be used instead of LMST, RNG, GG
- Delaunay triangulation can also be used (with Yao structure) for denser planar graph

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## On-demand scatternet formation

- Liu, Lee, Saadawi 2003
- Create scatternet only when route is needed
- Use flooding, which creates piconets during destination search, or
- Flooding could use single channel MAC while routing later uses scatternet/Bluetooth
- Destroy scatternet when routing completed

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## Three-dimensional scatternets ?

- Guerin, Sarkar, Vergetis 2002: DFS, BFS, MST
- They construct a tree where all nodes at one level are either masters or slaves (bipartite graph)
- MST nodes in 3-D can have degrees up to 13
- MST not localized, but RNG contains MST

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## Optimize edge lengths in scatternets



- Use sparse localized network (RNG or LMST)
- Degree of each node already limited to 6, average is 2 (LMST)
- Selected edges are *short* edges
- Add long edges up to degree 7, choose them in all directions
- Routing has reduced hop count due to adding four long edges on average
- For power efficiency add edges of preferred length

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## Future work

- Experiments: not many
- Bluetooth scatternet formation without position information and with slave degree limitation ??
- Routing in scatternets
- Power efficient scatternets
- Denser planar graphs ?
- Neighbor discovery and non-unit graphs
- Scheduling, capacity, QoS ...
- Fuzzy unit graph for scatternet formation
- Three-dimensional scatternets ?

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