

# Face, Age and Gender Recognition using Local Descriptors

by

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## Abstract

This thesis focuses on the area of face processing and aims at designing a reliable framework to facilitate face, age, and gender recognition. A Bag-of-Words framework has been optimized for the task of face recognition by evaluating different feature descriptors and different bag-of-words configurations. More specifically, we choose a compact set of features (e.g., descriptors, window locations, window sizes, dictionary sizes, etc.) in order to produce the highest possible rate of accuracy. Experiments on a challenging dataset shows that our framework achieves a better level of accuracy when compared to other popular approaches such as dimension reduction techniques, edge detection operators, and texture and shape feature extractors.

The second contribution of this thesis is the proposition of a general framework for age and gender classification. Although the vast majority of the existing solutions focus on a single visual descriptor that often only encodes a certain characteristic of the image regions, this thesis aims at integrating multiple feature types. For this purpose, feature selection is employed to obtain more accurate and robust facial descriptors. Once descriptors have been computed, a compact set of features is chosen, which facilitates facial image processing for age and gender analysis. In addition to this, a new color descriptor (CLR-LBP) is proposed and the results obtained is shown to be comparable to those of other pre-existing color descriptors. The experimental results indicates that our age and gender framework outperforms other proposed methods when examined on two challenging databases, where face objects are present with different expressions and levels of illumination. This achievement demonstrates the effectiveness of our proposed solution and allows us to achieve a higher accuracy over the existing state-of-the-art methods.

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# Table of Contents

List of Tables	vii
List of Figures	ix
Nomenclature	xi
<b>1 Introduction</b>	<b>1</b>
1.1 Motivation . . . . .	2
1.2 Problem Description . . . . .	3
1.2.1 Face Recognition . . . . .	3
1.2.2 Age and Gender Recognition . . . . .	4
1.3 Contribution . . . . .	4
1.4 Thesis Outline . . . . .	6
<b>2 Literature Review</b>	<b>7</b>
2.1 Face Recognition . . . . .	7
2.1.1 Holistic Approaches . . . . .	9
2.1.2 Feature Based Approaches . . . . .	10
2.2 Age and Gender Recognition . . . . .	11
2.3 Conclusion . . . . .	14
<b>3 Face Recognition</b>	<b>15</b>
3.1 Edge Detection Techniques . . . . .	16

3.1.1	Canny Edge Detector . . . . .	16
3.1.2	Sobel Edge Detector . . . . .	18
3.1.3	Laplacian Edge Detector . . . . .	19
3.2	Global Representation . . . . .	22
3.2.1	Principle Component Analysis (PCA) . . . . .	22
	Eigenfaces . . . . .	24
3.2.2	Linear Discriminant and Fisher Analysis . . . . .	27
3.3	Feature-Based Approaches . . . . .	30
3.3.1	Local Binary Patterns Histograms . . . . .	30
	Uniform Patterns . . . . .	32
3.3.2	Scale-Invariant Feature Transform (SIFT) . . . . .	33
3.3.3	Binary Robust Independent Elementary Features (BRIEF) . . . . .	34
3.3.4	Fast Retina Keypoint (FREAK) . . . . .	35
3.4	Block-based Bag of Words (BBoW) . . . . .	36
	<i>K</i> -means Clustering . . . . .	38
	Random Selections . . . . .	38
3.5	Matching face images for classification . . . . .	39
3.5.1	Brute-force Matching . . . . .	39
3.5.2	Compare Histograms . . . . .	39
3.5.3	Hamming Distances . . . . .	40
3.6	Experimental Results . . . . .	41
3.6.1	Dataset . . . . .	41
	The Facial Recognition Technology (FERET) Dataset . . . . .	42
	Labeled Faces in the Wild (LFW) Dataset . . . . .	43
3.6.2	Analysis of PCA, LDA, and LBPH . . . . .	44
3.6.3	Analysis of Edge Detection Operators . . . . .	45
3.6.4	Analysis of SIFT, BRIEF, and FREAK methods . . . . .	47
3.6.5	Analysis of the BoW approach . . . . .	48
3.6.6	Identification of unknown individuals . . . . .	51
3.7	Conclusion . . . . .	52

<b>4</b>	<b>Age and Gender Recognition</b>	<b>54</b>
4.1	Facial Representation . . . . .	56
4.1.1	Pool of Candidate Features . . . . .	56
4.1.2	Texture Features . . . . .	57
	The Local Binary Pattern Histogram . . . . .	57
	Gabor Texture Descriptors . . . . .	57
4.1.3	Shape Features . . . . .	59
	Scale-Invariant Feature Transform (SIFT) . . . . .	59
4.1.4	Color Features . . . . .	59
	Color Histogram . . . . .	60
	Color CENTRIST . . . . .	60
	Color-based Local Binary Pattern (CLR-LBP) . . . . .	61
4.2	Feature Selection . . . . .	63
4.3	Classification . . . . .	65
4.3.1	Support vector machine (SVM) . . . . .	65
4.4	Experimental Results . . . . .	68
4.4.1	Dataset . . . . .	68
	The Facial Recognition Technology (FERET) database . . . . .	69
	The Gallagher Collection Person Dataset (GROUPS) . . . . .	69
4.4.2	Results . . . . .	71
4.5	Conclusion . . . . .	75
<b>5</b>	<b>Conclusion</b>	<b>76</b>
5.1	Future Work . . . . .	77
	<b>References</b>	<b>78</b>

# List of Tables

3.1	The recognition rate of PCA, LDA, and LBPH with different numbers of training on the Fb probe set of the FERET database. First row indicates the number of images used for training and, under parantheses, the number of test images . . . . .	44
3.2	The recognition rate of PCA, LDA, and LBPH on the FERET database probe sets trained using Fa set. . . . .	45
3.3	The recognition rate of PCA, LDA, and LBPH on the LFW database . . . . .	45
3.4	The recognition rate of PCA, LDA, and LBPH methods combined with different edge operators on the Fc probe of the FERET database . . . . .	46
3.5	The recognition rate of the PCA, LDA, and LBPH combined with the Sobel edge operators on the FERET database probe sets . . . . .	46
3.6	The recognition rate of PCA, LDA, and LBPH combined with Sobel edge operators on the LFW database . . . . .	46
3.7	The recognition rate of the SIFT, BRIEF, and FREAK methods on the FERET database probe sets . . . . .	47
3.8	The recognition rate of the SIFT, BRIEF, and FREAK methods on the LFW database . . . . .	48
3.9	The recognition rate of the BoW method on features extracted by LBP, uLBP, and SIFT methods on the LFW database . . . . .	49
3.10	The recognition rate of BoW method over LBP features on the FERET database probe sets . . . . .	49
3.11	The recognition rate of the BoW method on features extracted by uLBP with different face alignment on the LFW database . . . . .	50
3.12	The recognition rate of BoW-uLBP method on aligned and unaligned faces of the LFW database . . . . .	50

3.13	The recognition rate of the BoW-uLBP method ( $grid = (8 \times 8)$ ) with two integer and floating point numerical systems on the LFW database . . . . .	51
4.1	Gender and age distribution in Groups dataset . . . . .	70
4.2	Comparative results of the gender recognition systems on the FERET and Gallagher's datasets. . . . .	72
4.3	Comparative results of the age recognition systems on the FERET and Gallagher's datasets. . . . .	73
4.4	Confusion matrix for three age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized). . . . .	74
4.5	Confusion matrix for five age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized). . . . .	74
4.6	Confusion matrix for seven age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized). . . . .	74



# List of Figures

1.1	Main program flow diagram . . . . .	3
1.2	Example of the recognition provided by the proposed face recognition framework under different amount of illumination and occlusion . . . . .	5
1.3	Example of the prediction provided by the proposed age and gender recognition framework . . . . .	5
2.1	Flowchart of face recognition system . . . . .	8
3.1	The Canny edge detector . . . . .	18
3.2	The Sobel edge detection. (a) Sample faces, (b) Detected edges along $x$ direction, (c) Detected edges along $y$ direction, (d) Detected edges' magnitude	19
3.3	The 2-D Laplacian of Gaussian (LoG) function . . . . .	21
3.4	The Laplacian edge detector . . . . .	21
3.5	The eigenfaces corresponding to the sample faces . . . . .	26
3.6	The fisherfaces corresponding to the sample faces . . . . .	30
3.7	The LBPH descriptor . . . . .	31
3.8	Examples of different texture structures detected by the LBP method (black circles represent of ones' "1", and white circles correspond to zeros "0") . . . . .	33
3.9	43 sampling patterns used in FREAK method . . . . .	35
3.10	Framework of Block-Based bag of Words(BBoW) . . . . .	37
3.11	Sample faces in FERET database . . . . .	42
3.12	Collected LFW database . . . . .	43

3.13	Performance evaluation results of the Bag-of-Words method over uLBP features with different number of words , gridding schemes and distances between pixels to extract descriptors . . . . .	51
3.14	Performance evaluation results of the Bag-of-Words method with 50 unknown faces with different threshold and number of regions . . . . .	52
4.1	The flowchart of a gender and age recognition application . . . . .	54
4.2	Representation of the real part of 40 Gabor filters . . . . .	58
4.3	Color Histogram descriptor . . . . .	60
4.4	Illustration of levels 2, 1, and 0 split of an image . . . . .	61
4.5	The CLR-LBP descriptor . . . . .	62
4.6	The first seven texture features selected by Ullman feature selection technique to classify gender subjects . . . . .	64
4.7	The first seven texture features selected by Ullman feature selection technique to classify age subjects . . . . .	65
4.8	The first seven shape features selected by Ullman feature selection technique to classify age subjects . . . . .	65
4.9	Support vector Machine schema . . . . .	66
4.10	Effect of the number of features selected . . . . .	75

# Nomenclature

## Abbreviations

BBoW	Block-based Bag of Words
BoW	Bag-of-Words
CBP	Centralized Binary Pattern
CENTRIST	CENsus Transform histogram
CGGH	Centralized Gabor Gradient Histogram
CH	Color Histogram
CLR-LBP	Color-based Local Binary Pattern
DCT	Discrete Cosine Transform
DWT	Discrete Wavelet Transform
EHMM	Embedded Hidden Markov Model
FERET	The Facial Recognition Technology
FREAK	Fast Retina Keypoint
HSV	Hue-Saturation-Value
ICA	Independent Component Analysis
LBP	Local Binary Pattern
LBPH	Local Binary Pattern Histogram
LDA	Linear Discriminant Analysis
LDS	Limited Discrepancy Search
LoG	Laplacian of Gaussian
LSDA	Locality Sensitive Discriminant Analysis
NN	Neural Networks
PCA	Principal Component Analysis
RBF	Radial Basis Function
RGB	Red-Green-Blue
SIFT	Scale-Invariant Feature Transform

SVM	Support Vector Machine
SVR	Support Vector Regression
ULBP	Uniform Local Binary Pattern
WLD	Weber Local Descriptor

# Chapter 1

## Introduction

The field of face processing is growing at an exponential rate, covering many technical areas such as image processing, surveillance and security, telecommunication and human-computer interaction. The world-wide range of commercial and law enforcement applications are a sign of its huge economic significance. The demand to build an automatic system to process face objects and extract the most useful information from this biometric feature leads to the necessity of overcoming some difficulties.

In this thesis, two separate problems are studied: face recognition and estimating the corresponding age and gender of face objects. Constructing applications to identify a person from their face and extract their age and gender information is a challenging task because of the necessity of creating a general model that works for all human subjects. As each person has his/her own innate face distinctive characteristics that vary in a subtle way from person to person, proposing a framework that extracts useful features to discriminate between faces requires in-depth studies of human face objects.

Processing human faces requires considering many aspects. One such aspect is to analyze face structure and determine the exact location of face elements, such as eyes, noses, mouths, eyebrows, lips and cheeks. Another is the extraction of relevant information from these detected elements which can provide us with useful information regarding the identity, age, ethnicity and gender of a person.

While face recognition has been a very active field of research in the recent decades, recognizing the age and gender from a face image has been more recently studied.

## 1.1 Motivation

Face, age and gender recognition has long been recognized as an important module for many computer vision applications such as human-robot interaction, visual surveillance and passive demographic data collections. Identifying persons to allow them access to or control of facilities, tools and information are amongst the most common applications of face recognition. As an example, facial recognition technology is currently being used by hotels and casinos to identify a blacklisted of individual. Unlocking software on mobile devices is another application that is developed and is available in Android Market (Visidon Applock) to allow the owner to secure applications. Similar applications is integrated into the iPhoto application for Macintosh, to let users organize and label their collections. Employing facial recognition instead of fingerprint recognition systems is another system which is being used for collecting the information regarding employee attendance and presence at work.

The objective of our research project is designing a framework which will be of low complexity such that it could be integrated into an embedded low power architecture.

In addition to the face recognition, the growing interest of the advertising industry, which seeks to launch demographic-specific marketing and targeted advertisements in public places is gaining more and more attention from researchers, who find themselves focusing on the issue of age and gender recognition. The objective of our research project is to extract demographic information of human subjects who are in front of smart TV displays, and deciding on the content to display for the audience and viewers based on the extracted information and environment.

Considerable amounts of studies conducted in the field of face processing have provided powerful and robust visual descriptors. Different visual descriptors regarding texture, shape and color information have been proposed in order to provide more compact representations for face objects. However, the challenge still remains to identify the ideal feature extraction method. While powerful new feature extractors have been proposed, they still cannot be applied to the real world applications because of their tendency to struggle to recognize faces that have been subject to minor variations. Differing image qualities, background clutter, different poses, changing facial expressions and varying levels of lighting are among the difficulties that these applications often encounter. In addition to this, collecting a good set of face images for building face models pose another problem. Designing a framework capable of recognition performances similar to the ones of humans requires a rich set of training images. For example, if we train a gender model with a set of faces

exclusively collected from Western people, it would not perform very well when tested on other ethnicity groups such as Asian people.

## 1.2 Problem Description

The objective of this thesis is to propose a methodology for the automatic recognition of facial/pattern occurrences from sample images captured in real time. Thus, two separate problems will be studied: face recognition and determining the corresponding age and gender of face objects. The common procedure for these two problems has been shown in Figure 1.1.

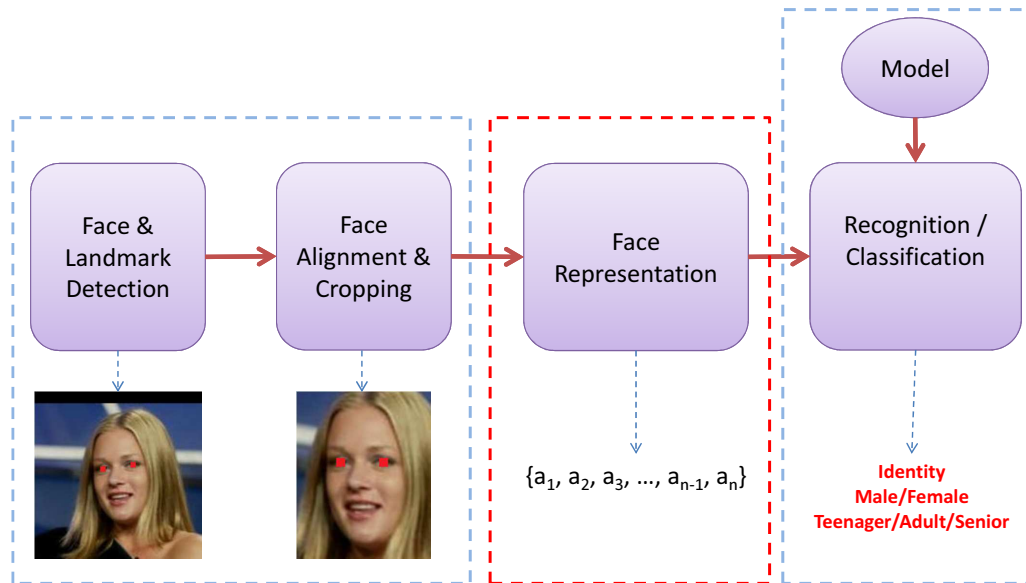


Figure 1.1: Main program flow diagram

### 1.2.1 Face Recognition

Face recognition is an interesting sub-area in the field of object recognition and can be defined as identifying or verifying human subjects in various scenes from a digital image or a video source. Human beings can recognize and identify faces learned during their lifetime even after years of separation. Thus, the subject of majority of studies in face processing is proposing a model that can recognize faces to a level similar to the average human's capacity [101].

While the currently existing face recognition systems obtained good results on face images captured in a controlled environment, they are still far from being capable of ad-

equately adapting to uncontrolled situations. Proposing a system that can adapt itself well to real-world applications and scenarios requires overcoming a number of difficulties. Of these difficulties, we can mention face pose variation, changes in expression, lighting conditions, clothing, hairstyle, makeup, background clutter, scaling, rotation, etc.

### 1.2.2 Age and Gender Recognition

Determining the age and gender of individuals from a live camera has many applications in the world of advertising. When a frame is captured, a face detection technique is employed to detect the face object. After detecting and aligning the face, the information allowing for greater facial discrimination is extracted and these data are then used to recognize the face's age and gender category.

This thesis aims at increasing the performance of face processing techniques in recognizing certain demographics (age and gender) from a face image. This information can then be used to display targeted advertisements to individuals viewing smart TV displays.

## 1.3 Contribution

This thesis has two main contributions: an approach for face recognition, and a framework for age and gender classification.

We have developed a face recognition framework that can be applied to real-world conditions. After investigating different approaches, we have adopted a bag-of-words structure [82] for face recognition by incorporating face-related features into it. We evaluated this structure on a challenging dataset containing sample images featuring a variety of poses, levels of illumination, backgrounds, expressions, clothing, hairstyles, cosmetics, etc. Figure 1.2 illustrates the face recognition application based on the proposed structure:



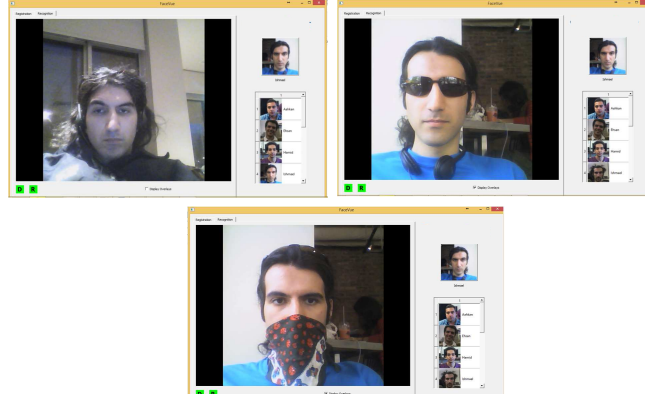


Figure 1.2: Example of the recognition provided by the proposed face recognition framework under different amount of illumination and occlusion

In addition to this, we propose a novel framework for gender and age classification that facilitates the integration of multiple feature types and, in doing so, takes advantage of various sources of visual information. Furthermore, in the proposed method, only the regions that can best separate face images of different demographic classes (with respect to age and gender) contribute to the face representations, which in turn improves the classification and recognition accuracies. Experiments performed on a challenging publicly available database validate the effectiveness of our proposed solution and show its superiority over the existing state-of-the-art methods. Figure 1.3 illustrates the age and gender recognition application based on our proposed method.

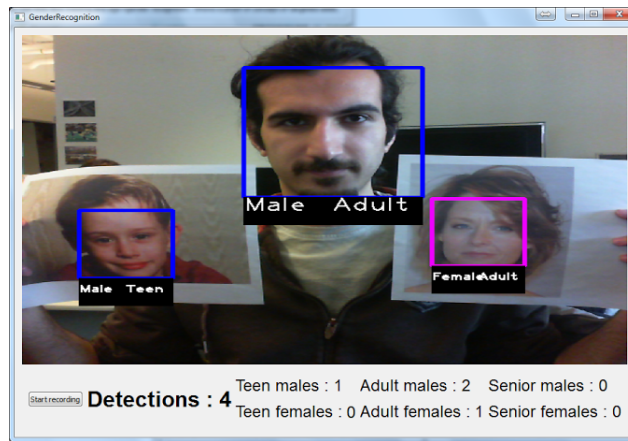


Figure 1.3: Example of the prediction provided by the proposed age and gender recognition framework

Our proposed method for age and gender recognition has been accepted in the International Conference on Image Processing (ICIP) [30].

## 1.4 Thesis Outline

This thesis is divided into two parts, one for each contribution of the thesis. In Chapter 2, we review some previously proposed ideas related to our research. In Chapter 3, we investigate different methods for face recognition. We first review well-known approaches and later compare them in order to determine the most accurate ones. Finally, an extensive experimentation was carried out in order to determine the optimal value for the parameters of our proposed face recognition approach when analyzing different real-world conditions. Chapter 4 discusses the problem of age and gender recognition. We first review existing popular descriptors for face representation. Then, we explain the functioning of our novel feature selection-based approach, which aims at facilitating the integration of multiple feature types. We end with a presentation and explanation of the results by our proposed method.

Finally, in Chapter 5, we summarize the contributions of this thesis and indicate possible future areas of development.

# Chapter 2

## Literature Review

Face processing has long been recognized as an important module for many computer vision applications. Face recognition, and the classification of the age and gender of face objects are two interesting field of research in this area. With such a face analysis component, it becomes possible to identify a person in order to allow access to private facilities or to display targeted information in advertising based on demographic category of individuals in public places. In this chapter we provide a brief review of some of existing methods in face, gender and age recognition and discuss their strengths and weaknesses.

### 2.1 Face Recognition

Face recognition has received significant attention in recent years. In spite of the progresses in this field, there are still several challenges associated with applying face recognition to real world situations. Among the most important applications in which face recognition plays a key role, we can mention access control, law enforcement and video surveillance [101].

When given an image to process, the face recognition system detects a human subject through face detection techniques and the face region is segmented from the image. The next stage is then to identify the facial features of the face in order to align it in a canonical way. A face representation is then extracted from the face. Then, the face representation is fed to the classification model to find the face in our pre-trained database, which best corresponds to the extracted face representation. In short, the entire procedure can be explained through the flowchart of Figure 2.1.

Face recognition has traditionally been divided into the following two different problems:

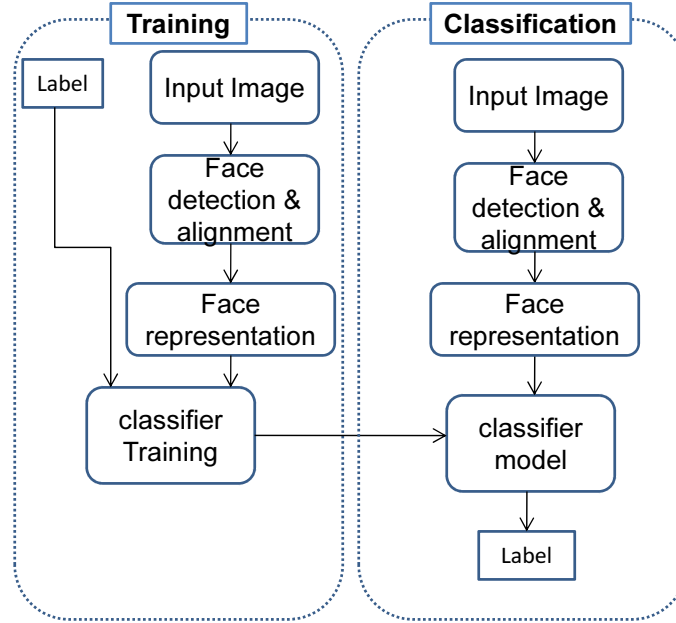


Figure 2.1: Flowchart of face recognition system

- **Face Identification:** The system has to identify the unknown face from a pool of candidate faces.
- **Face Verification:** The system must either accept or reject the claimed face as belonging to a specific person. This type of system is used in different applications, most often those related to access control or log in.

This thesis discusses the "Face Identification" problem and analyzes different methods proposed for the face representation stage.

There are multiple issues present when working with real-world images. Varying image qualities, background clutter, different face poses and expressions and changes in illumination are among the most common problems encountered in these types of applications.

The first attempts made in the history of face recognition were focused on extracting features from an edge image and finding the best match by evaluating distances between captured and trained faces[46]. In recent years, however, a large number of approaches have been proposed. These approaches can be generally divided into two categories: holistic approaches and feature-based approaches [46]. Therefore, in the following parts we will discuss these two types of methods.

### 2.1.1 Holistic Approaches

Holistic approaches developed for face recognition are based on processing the whole face and then representing it in a generic form. These methods extract features from a face without considering from which face areas they hail. As the dimension of each image is quite large, processing the whole face is difficult in practice. Because of this, dimension reduction approaches are applied in conjunction with holistic techniques.

Among the large amount of proposed algorithms in holistic approaches we can mention: Principal Component Analysis (PCA) [90], Linear Discriminant Analysis (LDA) [67], Discrete Wavelet Transform [4], Discrete Cosine Transform (DCT) [39], and Bayesian Intra-personal and Extra-personal Classifier [95].

PCA, as proposed by K. Pearson [74] and H. Hotelling [40], extracts a set of orthogonal basis vectors from the training data and then represents each data vector by a weighted sum of the extracted basis. This method has also been applied to face images by M. Turk in [90] where PCA was applied as a dimension reduction technique to preserve the most significant basis (called eigenfaces). Following this, each face was represented in the subspace spanned by these bases. They proposed a near-real-time application based on this method and experimented on a set of 2500 face images collected under controlled conditions [90].

LDA, invented by R.A. Fisher [67], is a method for dimension reduction and data classification which relies on mapping data to a new space within which each class, data have minimum variance and the maximum distance between classes. This method was applied to face recognition by K. Etemad and R. Chellappa [29] on a set of features extracted by Wavelet Transform and experimented on a database provided by The Olivetti Research Laboratory (ORL) and containing 40 different subjects featuring a variety of changes in illumination, facial expression and facial details (glasses or no glasses) as well as some side movements.

Discrete Wavelet Transform (DWT) is another holistic techniques and is based on the discrete sampling wavelet transform. In its basic format, DWT is used by a 2-D wavelet decomposition, which applies a 1-D transformation in X-direction and another Y-direction. This transformation generates four sub-images, which correspond to the different frequencies in each direction (High-High, High-Low, Low-High, Low-Low). Following this, the feature vector is constructed by using information of the Low-Low sub-image which is then employed for finding the match within trained faces ([76], [80]).

Discrete Cosine transform is a popular method in image compression and is another

method in the category of holistic transform. This method applies a 2-D DCT on image and then codes the entropy of the quantized samples to get the result. DCT is a strong technique for "energy compaction" and was applied to the process of face recognition by M. J. Er et al. [39], who carried out their experiments on three databases : 1) ORL, 2) The FERET database and 3) The Yale database.

The Bayesian Intra-personal and Extra-personal Classifier method exploits the fact that two different image classes span subspaces with Gaussian distribution properties [89]. Moghaddam and Pentland [69] showed that these subspaces (called extra-personal and intra-personal subspaces) cooperated with similarity measurements computed by a Bayesian rule that gives the probability on how likely a vector belongs to a specific subspace [69].

### 2.1.2 Feature Based Approaches

These approaches rely on the fact that all human subjects share the same fundamental structures and the only true difference is the geometric relations between said structures. Therefore, feature-based methods will, at first, extract facial features like eyes, nose, mouth, eyebrows, etc and then extract the existing relationship between these facial features. Of the common algorithms employed for this purpose, we can mention deformable templates, the Hough Transform method and Elastic Bunch Graph Matching.

The deformable templates method is based on the idea that a family of objects can be represented by deformations of a basic ideal template. This notion is what makes this technique more robust against the different scales and positions that a face object can adopt as well as changes in illumination [98]. This method finds sets of features by using spatial relations and prior knowledge of the general layout of a face to build a vector of features, which is then used to represent and recognize faces.

The basic Hough Transform method has been applied to detect straight lines [41] and was later extended by R. Duda and P. Hart[26] so as to be able to compute shape analysis and identify arbitrary shapes. This approach was applied for the purposes of face recognition in [41] and proved its robustness against various noises. It also has high level of efficiency in terms of its memory usage.

One of the other feature-based methods frequently used is Elastic Bunch Graph Matching. This approach builds a graph based on the face structure, that connects the detected facial features, such as eyes, nose, etc. The edges represent the similarity distance between the nodes. Wiskott et al. [95] used Elastic Bunch Graph Matching in face recognition by

constructing each node with Gabor filter results and utilizing the edges to describe the geometrical properties of each face.

In this section, we presented a short overview of the two main categories in face recognition. Holistic approaches process the entire face and extract a global representation, which is then be fed to the recognition stage system. Feature-based methods directly identify facial features and employ the spatial structures between them to identify the face. Although processing each facial structure separately creates a system that is robust against position variation, lighting condition changes and noise, in the last few decades, holistic approaches have attracted more attention from researchers specializing in the field of face processing [101]. In our thesis we will look over different methods in these categories to identify which ones offer optimal performances in the real world.

## 2.2 Age and Gender Recognition

Age and gender recognition is an important modules for many computer vision applications such as human-robot interaction, visual surveillance and passive demographic data collections. More recently, the advertising industry’s growing interest in the launching demographic-specific marketing and targeted advertisements in public places has attracted the attention of more and more researchers specialized in the field of computer vision. In this section, we will take a brief look at the different techniques proposed in the field of age and gender recognition. A detailed survey of studies on age and gender recognition can also found [71], [68])

Among the early algorithms in the field of age and gender recognition, Cottrel and Metcalfe [22] extracted whole-face features called Holons, which were fed into a back propagation network model to classify males and females. Golomb et al. [36] proposed ”SEXNET” Neural Network model for gender recognition. This network compresses faces using faces’ raw pixels and then estimates their sex in subsequent layers of their proposed network. In 1995, Brunelli and Poggio [11] achieved a 79% recognition rate for gender by using the HyperBF network on a set of geometrical features extracted from faces and, shortly after, Abdi et al.[2] employed the RBF network and achieved a 90% recognition rate on data preprocessed by PCA. In 1997, wavelet components (jets) were exploited by Wiskott et al.[96] in order to describe face features and build Elastic Bunch Graph models. In 1999, Kwon and Lobo[52] proposed a method for age classification that first extracted specific features of the face elements such as eyes, noses, mouths and chins. It then compute the ratios estimated between the top of sides of the head before, finally, processing skin wrinkle

information in order to classify people in three classes: babies, young adults and seniors.

Wen Bing Horng et al[9] employed Sobel edge detector with a back-propagation Neural network to classify human face subjects into four classes: babies, young adults, middle adults and old adults.

Lyons et al. [66] applied Gabor wavelets and LDA to create a neuro-fuzzy system for gender classification, which gave them a more accurate system when compared with previously existing methods. In 2002 Sun et al. [87] proposed a feature selection method by using genetic algorithms to select features extracted by PCA. They compared different classifiers such as Bayesian, NN, LDS and SVM and demonstrated that using a SVM classifier is a better approach for classifying gender. Moghaddam and Yang[70] claimed that the support vector machine (SVM), when using a RBF kernel, generates a stronger classifier than those previously used in gender recognition. They experimented on both small images ( $21 \times 12$ ) and good quality images ( $64 \times 72$ ) of the FERET database and they achieved a 96.6% accuracy on the second image data. In addition to this, they claimed that the difference between the two different qualities is just 1%. Following this, Lanitis et al. ([55], [53], [54]) claimed that combination of shape and texture features with different techniques such as an active appearance model, PCA, Mahalanobis distance, a Multi-Layer perceptron and a Neural network can be used as a good age estimator.

In 2004, Jain and Huang[47] proposed an approach using an independent component analysis (ICA) as one of the feature-based methods for extracting features and employed LDA as classifier. Costen et al.[21] proposed a sparse SVM to classify genders and claimed an accuracy rate of 94.42% on Japanese face images. In 2005, Ye Sun et al.[86] proposed an approach that used the relationship between key feature points in human faces to train an Embedded Hidden Markov Model(EHMM) to estimate age.

PCA and Locality Sensitive Discriminant Analysis (LSDA) was later applied to learn different manifolds of aging patterns based on the fact that each age category was distributed on a specific manifold in a large dimensional subspace [37]. Local Binary Pattern (LBP) was used as a method for extracting texture features by Sun et al. [85] in 2006. LBP, which builds up the spatial structure of each pixel by comparing its intensity with that of its neighborhood, was used with both Adaboost classifier[77] and SVM classifier to facilitate gender classification.

Classifying facial expressions prior to gender classification was used to improve the classification rate by Saatci and Town(2006) [79]. Although Saatci and Town investigated the interdependency of gender recognition upon expression and they showed that the gender classification rate decreased even with using separate gender data for different expression



classes. In 2007, a color descriptor relying on the construction of histograms with 4 bins per color channel in the RGB color space was proposed for gender classification [45]. The fusion approach, 2D PCA and the centralized Gabor gradient histogram (CGGH) were other methods that were employed in feature extraction [Lu and shi (2009)[65], Len Bui (2010)[12], Xiaofeng Fu(2010)[32]]. Xiaofeng Fu[32] combined CBP and Gabor gradient magnitudes to extract more discriminative features at multiple scales and orientation[45]. By feeding these features into a nearest center-based neighbor classifier, they achieved a 96.56% accuracy rate on FERET and a 95.25% accuracy rate on CAS-PEAL. Meanwhile, in 2010, Guo-Shiang Lin and Yi-Jie Zhao [60] proposed a color-based approach on SVM for gender classification. In 2011, compressive sensing framework was applied by Duan-Yu Chen and Po-Chiang Hsieh [17] to represent face images in a sparse frequency domain. They extracted two feature sets for each gender; the first set presenting features that are common between all the images in corresponding gender classes and the other one representing each individual face in that class. Ihsan Ullah et al. (2012) [91] used spatial WLD as a texture descriptor for gender recognition. They divided the image into a number of blocks, calculated the WLD descriptor for each block and concatenated them.

In 2013, Chen, Y. et al.[18] introduced a new method based on subspace learning that operates as a set of constrained optimization problems to characterize age-related features. By employing semi-supervised learning techniques they applied the Support Vector Regression(SVR) methods onto the features to create an age estimators model. Juan E. Tapia and Claudio A. Perez (2013)[88] proposed a method, which uses feature selection based on mutual information and the fusion of intensity, shape and texture features to classify gender classes. They then calculated LBP features with different radial and spatial scales, and then selected features using mutual information. They tested three different techniques to measure mutual information: minimum redundancy and maximum relevance[25], normalized mutual information[28], and conditional mutual information-based [19].

Therefore, we can summarize that the most of the efforts made to optimize in gender and age recognition from a face object attempt to best represent the face object. While some methods choose to use raw pixels (e.g., [2], [3] and [4]) without any modification, the majority of the existing methods use local visual descriptors to produce stronger and, often, more compact representations of face images. Examples of visual information commonly used for age and/or gender recognition are texture information (e.g., used in [55],[53],[54], [85], [91], [3]), shape information (e.g., used in [88], [27], [13]) and color information (e.g., used in [60] and [45]). In these methods, local descriptors are extracted from a dense regular grid placed over the entire image and the face representation is built by concatenating these extracted descriptors into a single vector. A key issue in this framework is to determine the

optimal grid parameters (e.g., spacing, size, number of grids in multi-resolution/pyramid approaches, etc.). Dago-Casas et al. [24] proposed to use raw pixels, Gabor jets and LBPs on Gallaghers database for gender recognition. They reduced the size of extracted features by using Principle Component Analysis and showed that, by using Gabor jets followed by SVM high gender classification, a greater accuracy is obtained. While the aforementioned methods for age and gender recognition used fixed settings and performed trial-and-error to determine the right grid parameters, a better approach consists in using feature selection to allow only the most informative image regions (or grid cells) to contribute to the face representation, i.e., those that can best separate face images that belong to different demographic classes. This approach further facilitates the integration of different types of descriptors (e.g., color based, shape based, texture based, etc.) and allow for more compact representations by preventing redundant features from contributing to the face representation.

## 2.3 Conclusion

This chapter has described different attempts that have been made in the fields of face, gender and age recognition. The main issue addressed by these methods is how to best represent a face in such a way that it will be most efficiently identified. It is in this vein that we will go over different techniques used to represent faces and to try to come up with a generic algorithm that can be applied to solve our problem: accurate face representation and recognition.

# Chapter 3

## Face Recognition

The development of applications to extract the distinctive features from face images has been the motivation behind the majority of studies in the field of face processing. These studies proceed by detecting a face and extracting a compact representation from it. As face processing research has progressed, increasingly complex challenges have been encountered, and new techniques have been proposed to provide accurate and robust ways of solving these problems.

Although there are many different branches in the field of face processing, face recognition is an essential component. In general, solving this problem requires overcoming certain difficulties, such as differing image qualities, background clutter, poses, facial expressions, and varying levels of lighting. This chapter summarizes some popular methods for facial recognition and propose a face recognition approach that is robust, simple, and efficient to use when compared to other existing methods.

While some methods choose to extract features from raw pixels, others first employ pre-processing techniques to reduce the impact of changing illumination and contrast before extracting the facial features. Section 3.1 presents some common edge detectors that can be used to this end. Then, section 3.2 highlights the two classic techniques that have been applied for the global representation of a face image. Section 3.3 is dedicated to popular feature-based methods, in particular LBPH, SIFT, BRIEF, and FREAK. Section 3.4 describes the Block-based Bag-of-Words method representation method. Section 3.5 presents a matching strategy to effectively establish face matches. Finally, experimental results are reported in section 3.6. We introduce two datasets against which we benchmark the previously mentioned methods.

## 3.1 Edge Detection Techniques

As mentioned in the previous chapter, one of the main steps of face processing is face representation, which requires extracting the most relevant information to characterize a face. Although edge detection operators are not categorized as powerful descriptors, combining them with other methods can lead to the removal of noise artifacts while preserving the useful face features.

Generally, edge detection consists in computing the gradient magnitude of an image. Edges localize sudden changes in intensities of color or illumination in images. An image gradient can be computed by applying convolution masks on the image. In this section we describe the Canny edge detector as well as the Sobel and Laplacian edge detection techniques. The objective of employing these techniques is to limit the impact of intensity variation in the face image, thus allowing for more robust descriptors to be extracted.

### 3.1.1 Canny Edge Detector

The Canny Edge detector is one of the most common edge detection techniques. This technique proceeds as follows:

- First, a blurring operation, such as a Gaussian filter, is applied to the image to suppress input noises and distinguish between the simple edges and meaningful edges, such as the contour of objects.

To smooth the image and suppress unnecessary texture edges, the following Gaussian filter can be applied:

$$G(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}} \quad (3.1)$$

where  $\sigma$  value controls the smoothing level.

- Next, the gradient magnitude and direction is computed by evaluating the gradient in  $x$  and  $y$  directions:

$$M = |\sqrt{G_x^2 + G_y^2}| \quad \text{Where} \quad G_x = \frac{\partial I_s}{\partial x} \quad \text{and} \quad G_y = \frac{\partial I_s}{\partial y} \quad (3.2)$$
$$\theta = \arctan\left(\frac{G_y}{G_x}\right)$$

Then the angle computed for  $\theta$  is rounded to four directions:  $0^\circ$ ,  $45^\circ$ ,  $90^\circ$ , and  $135^\circ$ . Finally, nonmaxima suppression is applied to the computed gradient magnitude.

In this procedure, edges which have the large gradient's magnitude are preserved. Additionally, broad ridges are thinned and all other edges that belong to smooth textures on the ridge are suppressed. For this purpose, we seek local maxima by checking the  $3 \times 3$  region around each pixel, taking into account its orientation [15]:

- 1) If  $\theta_r(x, y) = 0$ , then we compare the  $M(x, y)$  value with  $M(x - 1, y)$  and  $M(x + 1, y)$
- 2) If  $\theta_r(x, y) = 45$ , then we compare the  $M(x, y)$  value with  $M(x - 1, y - 1)$  and  $M(x + 1, y + 1)$
- 3) If  $\theta_r(x, y) = 90$ , then we compare the  $M(x, y)$  value with  $M(x, y - 1)$  and  $M(x, y + 1)$
- 4) If  $\theta_r(x, y) = 135$ , then we compare the  $M(x, y)$  value with  $M(x - 1, y + 1)$  and  $M(x + 1, y - 1)$

In the aforementioned situations, if  $M(x, y)$  has a large value, it would be kept as an edge. Otherwise, it would be removed as it is not a local maxima.

At this stage, the algorithm suggests to employ double thresholding techniques to detect and link edges [15]. By using two levels of thresholding, more meaningful edges are obtained. Applying a high value threshold will give us edges corresponding to real contours that are then linked using edges detected at a lower threshold.

Figure 3.1 illustrates the result of applying a Canny edge detector on the face images.



Figure 3.1: The Canny edge detector

### 3.1.2 Sobel Edge Detector

Sobel, as proposed by Irwin Sobel [84], is another popular technique for edge extraction. This method, which approximates the 2-D spatial gradient of images, has been combined with several algorithms for the purpose of face recognition (e.g., [58], [61], and [100]). The basic version of this filter convolves two  $3 \times 3$  kernel filters with a grayscale image. These two filters,  $G_x$  and  $G_y$ , which correspond to horizontal and vertical derivative masks are defined as follows [84]:

$$G_x = \begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix} \quad G_y = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} \quad (3.3)$$

And the gradient magnitude is computed as:

$$\theta = \arctan\left(\frac{G_Y}{G_X}\right) \quad (3.4)$$

$$G = \sqrt{G_X^2 + G_Y^2}$$

where  $G_x$  and  $G_y$  are the computed gradient values of a pixel in location  $(x, y)$ .

Figure 3.2 shows the result of applying  $G_x$  and  $G_y$  on an image and  $G$  as the corresponding image's magnitude:

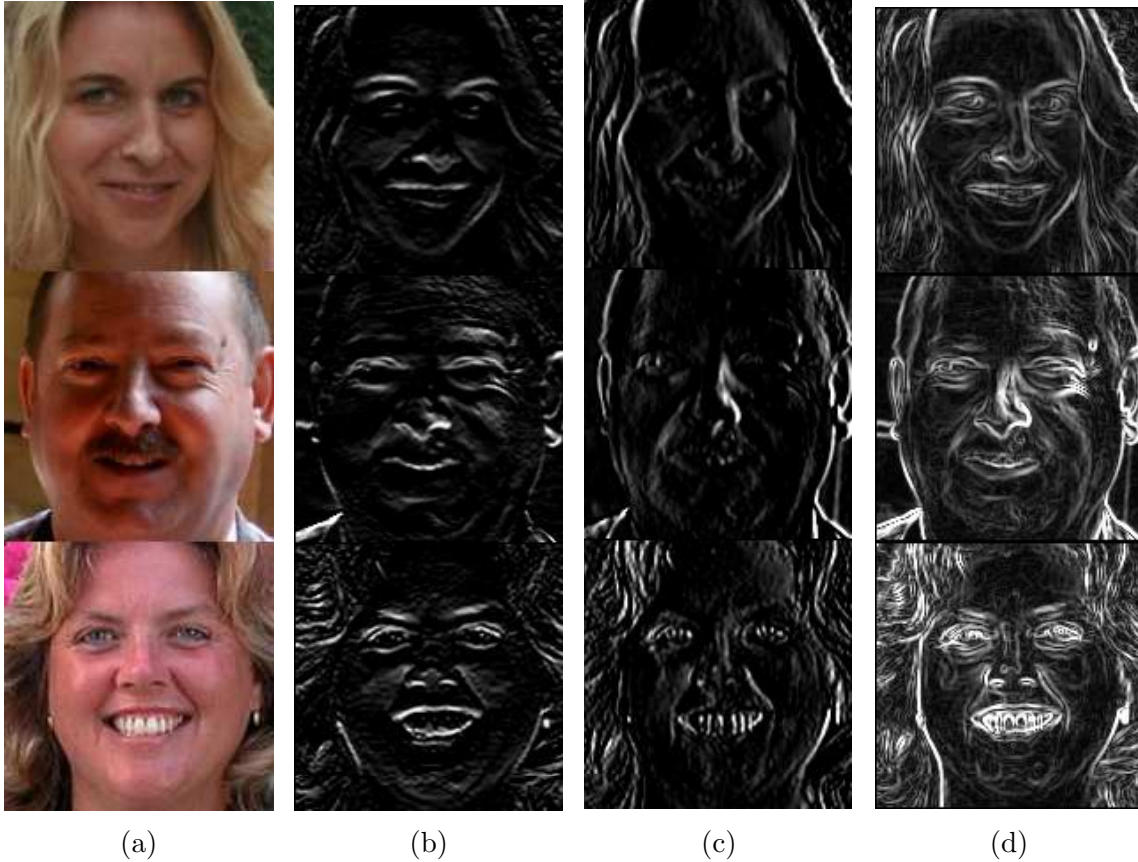


Figure 3.2: The Sobel edge detection. (a) Sample faces, (b) Detected edges along  $x$  direction, (c) Detected edges along  $y$  direction, (d) Detected edges' magnitude

### 3.1.3 Laplacian Edge Detector

The next technique is the Laplacian edge detector. Unlike the Sobel technique, which finds intensity variations by observing the first derivation of images, the Laplacian method uses the second derivation of images. Since intensity changes appear as the maximum or minimum points in the first derivation of the image, the second derivative crosses the zero axis in these critical points. On this basis, the 2-D Laplace operator has been defined as follows:

$$\begin{aligned}
 \nabla^2 &= \nabla \cdot \nabla = \left( \frac{\partial}{\partial x} \vec{i} + \frac{\partial}{\partial y} \vec{j} \right) \cdot \left( \frac{\partial}{\partial x} \vec{i} + \frac{\partial}{\partial y} \vec{j} \right) = \left( \frac{\partial^2}{\partial x^2} \right) (\vec{i} \cdot \vec{i}) + \left( \frac{\partial^2}{\partial y^2} \right) (\vec{j} \cdot \vec{j}) + \left( \frac{\partial}{\partial x} \frac{\partial}{\partial y} \right) (\vec{i} \cdot \vec{j}) + \left( \frac{\partial}{\partial x} \frac{\partial}{\partial y} \right) (\vec{j} \cdot \vec{i}) \\
 &= \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}
 \end{aligned}
 \tag{3.5}$$

This operator can be utilized by employing a filter mask. We first calculate an approx-

imation kernel for second derivation and then convolve it into the image. For this purpose we can create filters with different sizes by manipulating partial sums of the Taylor series:

$$f(x+h) = f(x) + \frac{h^1}{1!}f'(x) + \frac{h^2}{2!}f''(x) + \frac{h^3}{3!}f'''(x) + \frac{h^4}{4!}f^{(4)}(x) + \dots$$

$$f(x-h) = f(x) - \frac{h^1}{1!}f'(x) + \frac{h^2}{2!}f''(x) - \frac{h^3}{3!}f'''(x) + \frac{h^4}{4!}f^{(4)}(x) + \dots$$

$$f(x+h) + f(x-h) = 2f(x) + 2\frac{h^2}{2!}f''(x) + 2\frac{h^4}{4!}f^{(4)}(x) + h^6c$$

$$f''(x) = \frac{f(x+h) - 2f(x) + f(x-h) - 2\frac{h^4}{4!}f^{(4)}(x) - h^6c}{h^2} = \frac{f(x+h) - 2f(x) + f(x-h)}{h^2} + h^2c'$$

$$\text{So by setting } h = 1: \quad \frac{\partial^2 I(x, y)}{\partial x^2} \approx f(x+1, y) - 2f(x, y) + f(x-1, y)$$

$$\text{and similarly} \quad \frac{\partial^2 I(x, y)}{\partial y^2} \approx f(x, y+1) - 2f(x, y) + f(x, y-1)$$

$$\begin{aligned} \text{as} \quad \nabla^2 I(x, y) &= \frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2} \\ &= \begin{bmatrix} 0 & 0 & 0 \\ f(x-1, y) & -2f(x, y) & f(x-1, y) \\ 0 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 0 & f(x, y-1) & 0 \\ 0 & -2f(x, y) & 0 \\ 0 & f(x, y+1) & 0 \end{bmatrix} \\ &= \begin{bmatrix} 0 & f(x, y-1) & 0 \\ f(x-1, y) & -4f(x, y) & f(x-1, y) \\ 0 & f(x, y+1) & 0 \end{bmatrix} \end{aligned} \quad (3.6)$$

As such, kernel  $L_1 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$  is one of the kernels that can be used as an approximation for the second derivative. Other common forms of  $3 \times 3$  kernels that have been derived in a similar way have been provided as follows:

$$L_2 = \begin{bmatrix} 2 & -1 & 2 \\ -1 & -4 & -1 \\ 2 & -1 & 2 \end{bmatrix} \quad L_3 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & -8 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

Although kernels in other sizes can be employed to make this approximation (3.5) more accurate, all of them are extremely sensitive to noise due to their nature. The simple solution to overcome this problem is to apply an additional Gaussian filter to suppress the noise. By the associative property of convolution, we can write:

$$\nabla^2 [G(x, y) * I(x, y)] = \nabla^2 [G(x, y)] * I(x, y) \quad (3.7)$$



where the term  $G(x, y)$  represents the Gaussian filter and  $\nabla^2[G(x, y)]$  is the denoted Laplacian of Gaussian (LoG( $x, y$ )). LoG is computed by taking the derivative which is equal to:

$$LoG(x, y) = -\frac{1}{\pi\sigma^4}\left(1 - \frac{x^2 + y^2}{2\sigma^2}\right)e^{-\frac{x^2+y^2}{2\sigma^2}} \quad (3.8)$$

As demonstrated above, a mask filter can be used in different scales of  $\sigma$ , as is the case in the following figure, which corresponds to LoG with  $\sigma = 1.5$ :

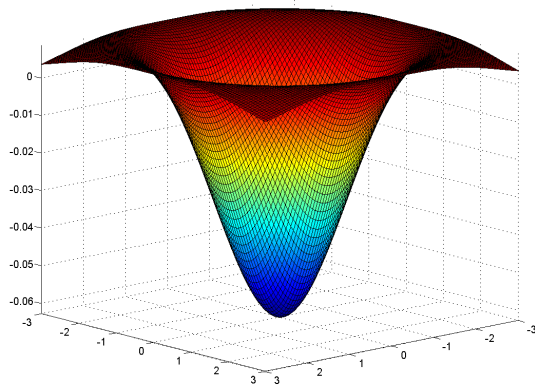


Figure 3.3: The 2-D Laplacian of Gaussian (LoG) function

Here is the result of applying this kernel with size  $9 \times 9$  on the sample face images:



Figure 3.4: The Laplacian edge detector

## 3.2 Global Representation

As discussed earlier, global representation for face recognition is based on processing the whole face and then representing it in a generic form. These methods extract features from a face without considering the areas of the face from which these come. The objective of these approaches is to reduce the dimensionality of feature data extracted from the face image, thus allowing for more distinctive data to be used to represent a face. In this section, two classical approaches, PCA and LDA, will be discussed.

### 3.2.1 Principle Component Analysis (PCA)

Principle Component Analysis (PCA), as proposed by Karl Pearson [74], is one of the more commonly used statistical approaches to dimensional reduction and data classification. This method computes the transformation of a set of correlated variables into a set of linearly uncorrelated vectors called principal components. The relevance of this transformation lies in the fact that the number of required components to represent data is less than the full dimension of its original one. This method, also known as the **discrete Karhunen-Leove** transform, represents a stochastic process as an infinite linear combination of orthogonal basis vectors.

In the Karhunen-Leove method ([49], [1]), a signal ( $X$ ) is assumed to be made of  $N \times 1$  random vector with an auto-correlation defined as  $R = E[XX^H]$ . Employing the Cholesky factorization method, we can write the matrix  $R$  as  $R = U\Lambda U^H$ , where the columns of  $U$  correspond to the normalized eigen-vectors of  $R$ . Then, our data can be transformed to the zero-mean random vector  $Y$  with uncorrelated components:

$$E[YY^H] = \Lambda \tag{3.9}$$

Furthermore, our original data ( $X$ ) can be synthesized by employing a linear combination of the uncorrelated random variable  $Y$  as follows:

$$X = UX = \sum_{i=1}^N u_i Y_i \tag{3.10}$$

However, as mentioned previously, the  $Y$  vectors are a set of orthogonal vectors (which are basically the eigen-vectors of the correlation matrix  $R$ ), and this representation is called the *Karhunen-Leove* expansion of  $X$ .

The aim is to find an approximate representation of a signal  $X$  requiring as few components as possible based on the approximation:

$$\hat{x} = Kx \quad (3.11)$$

where  $K$  is an  $N \times N$  matrix with a rank of less than  $N$ . This representation of  $X$  can be determined using a mean-squared error minimization approach. Such an approximation is called a low-rank approximation. By considering that  $\lambda_1, \lambda_2, \dots, \lambda_N$  and  $x_1, x_2, \dots, x_N$  correspond to the set of eigen-values and eigen-vectors of the auto-correlation matrix  $R$ , the mean-squared error can be expressed as follows:

$$\begin{aligned} e^2(K) &= E[(X - \hat{X})^H(X - \hat{X})] = \text{tr}(E[(X - \hat{X})(X - \hat{X})^H]) = \text{tr}(E[(X - KX)(X - KX)^H]) \\ &= \text{tr}(E[(I - K)XX^H(I - K)^H]) = \text{tr}((I - K)R(I - K)^H) \end{aligned} \quad (3.12)$$

Then, by using orthogonal decomposition and assuming that  $K$  is Hermitian, we can write:

$$K = \sum_{i=1}^r \mu_i u_i u_i^H = U M_r U^H \quad (3.13)$$

where  $r$  is the new rank ( $r < N$ ),  $U$  is a unitary matrix and  $M_r$  is equivalent to:

$$M_r = \begin{bmatrix} \mu_1 & 0 & 0 & 0 & 0 & \cdots & 0 \\ 0 & \mu_2 & 0 & 0 & 0 & \cdots & 0 \\ \vdots & 0 & \ddots & 0 & 0 & \cdots & 0 \\ 0 & \cdots & 0 & \mu_r & 0 & \cdots & 0 \\ 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (3.14)$$

As such, the error in equation 3.12 is expressed as follows:

$$e^2(K) = \sum_{i=1}^r u_i^H R u_i (1 - \mu_i)^2 + \sum_{i=r+1}^N u_i^H R u_i \quad (3.15)$$

It follows that in order to minimize 3.15 all values  $\mu_1, \mu_2, \dots, \mu_r$  should be equated to one (1) in the first term and those in the second term ( $\sum_{i=r+1}^m u_i^H R u_i$ ) should be minimized. As stated previously,  $u_i$  corresponds to the  $i$ 'th eigen-vector of  $R$ . Therefore, the rank- $r$

projection matrix  $K$  can be expressed as follows:

$$K = \sum_{i=1}^r u_i u_i^H = U I_r U^H \quad (3.16)$$

where:

$$I_r = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & 0 & 0 & \cdots & 0 \\ \vdots & 0 & \ddots & 0 & 0 & \cdots & 0 \\ 0 & \cdots & 0 & 1 & 0 & \cdots & 0 \\ 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (3.17)$$

Based on this derivation, PCA tries to collect the principle components having the highest variance. At each step, eigen-vectors corresponding to the largest principle component are selected under the constraint of orthogonality to preceding components. When the signal to process is a face image, these eigen-vectors are often referred to as eigen-faces. The following section will describe how a set of eigen-faces is selected to represent a face image.

## Eigenfaces

A face image with size  $N \times N$  can be considered as a vector of dimension  $N^2$ . If each pixel takes a value between 0 and 255, the face image lies on a large hypercube with  $N^2$  dimensions where most of the points in the space does not correspond to any face. Therefore, it can be assumed that face data in fact belongs to a lower dimensional subspace. By employing PCA based on the Karhunen-Loeve algorithm, it is possible to find the vectors that best account for the distribution of face data within this space.

Assuming that our training face images are represented by  $I_1, I_2, \dots, I_M$ , the average face vector can be easily expressed as follows:

$$\Psi = \frac{1}{M} \sum_{i=1}^M I_i \quad (3.18)$$

After subtracting the average face from all face images, we employ their covariance matrix to compute the orthornormal vectors,  $u_i$ , and extract the distribution of the training face

data:

$$\begin{aligned}\Phi_i &= I_i - \Psi \\ C &= \frac{1}{M} \sum_{i=1}^M (\Phi_i)(\Phi_i)^T = \frac{1}{M} AA^T\end{aligned}\tag{3.19}$$

where  $A = [\Phi_1 \ \Phi_2 \ \dots \ \Phi_M]$  and  $C$  is a  $N^2 \times N^2$  matrix corresponding to the covariance matrix. It is obvious that if the number of face images is less than the dimension of our space ( $N^2$ ), a maximum of  $M - 1$  eigen-values would be non-zero, and the rest of them are not associated with meaningful eigen-vectors.

Afterwards, we have to compute the eigen-vectors of matrix  $C(AA^T)$ :

$$AA^T v_i = \mu_i u_i\tag{3.20}$$

Since  $AA^T$  is a huge matrix, finding its eigen-vectors is not always practical. Thus, we go over matrix  $A^T A$ , which has the same eigen-values, and for which the eigen-vectors are computed as follows:

$$A^T A v_i = \lambda_i v_i\tag{3.21}$$

premultiplying both sides by  $A$ :

$$AA^T A v_i = \lambda_i A v_i \Rightarrow AA^T (A v_i) = \lambda_i (A v_i)\tag{3.22}$$

As  $v_i$ , and  $u_i$  are the eigen-vectors corresponding to  $A^T A$  and  $AA^T$  respectively, we have:

$$u_i = A v_i\tag{3.23}$$

By preserving the  $r$  largest eigen-values, the size of each face representation will be reduced. These eigen-vectors ( $u_i$ ) span a range of face images. Figure 3.5 shows eigen-faces extracted from some face images.



Figure 3.5: The eigenfaces corresponding to the sample faces

Next we project a face image onto an eigenface component by the following mapping:

$$\hat{I}_k = u_k^T(I - \Psi) \quad k = 1, \dots, r \quad (3.24)$$

Finally, face representation is constructed in the eigenface's space by concatenating all computed components:

$$\hat{I} = [\hat{I}_1, \hat{I}_2, \dots, \hat{I}_r] \quad (3.25)$$

This representation will be used next for classification, in finding the best match between face classes. Each face class is calculated by obtaining the average over the results of the eigen-face representation for all faces within it. In addition to this, a threshold,  $\theta_k$ , is assigned to each class to determine the maximum allowable distance between those faces. This threshold is calculated based on all face data within that class.

One of the first and most prevalent ways to find the best match for a test image is to compare the Euclidean distance between its extracted descriptor by PCA ( $\hat{I}_o$ ) and the ones extracted from the input set ( $\hat{I}_k \in S_M$ ). It can be expressed as follows:

$$I_p = \arg \min_{I_k \in S_M} \|(\hat{I}_o - \hat{I}_k)\| \quad (3.26)$$

where  $S_M$  is the set of the face classes.

### 3.2.2 Linear Discriminant and Fisher Analysis

Another popular approach in pattern classification is the Linear Discriminant Analysis (LDA) [67]. This method aims at finding the projection that best separates different classes. For this purpose, LDA defines a measurement of separation between the classes:

$$J(\mu) = |\mu_1 - \mu_2| \quad (3.27)$$

where,  $\mu_i = \frac{1}{N_i} \sum_{x \in C_i} x$  and  $C_i$  represents class  $i$ .

Therefore, LDA aims to find an appropriate projection of  $y = W^T x$ , which will allow the distance to become sufficiently large, as shown below:

$$J(w) = |W^T \mu_1 - W^T \mu_2| = |W^T (\mu_1 - \mu_2)| \quad (3.28)$$

Since this expansion simply considers the distance between the means of classes, and does not provide any other information regarding the scattering of data in each class, it is not always a good measurement of the distances between them. Consequently, Fisher [67] proposed a measurement for two classes as follows:

$$J(w) = \frac{|W^T \mu_1 - W^T \mu_2|^2}{\tilde{s}_1^2 + \tilde{s}_2^2} \quad (3.29)$$

where  $\tilde{s}_1^2$  and  $\tilde{s}_2^2$  are the parameters that correspond to the variability within class 1 ( $C_1$ ) and class 2 ( $C_2$ ) after projection. As such,  $\tilde{s}_1^2 + \tilde{s}_2^2$  measures the variability within the two classes and is called the *within-class scatter* of the projected samples.

Fisher's technique aims to maximize the function 3.29 by finding a projection in which data from the same class are projected very close to one another, while data from different

classes are placed as far apart as possible. This projection can be found as follows:

$$\begin{aligned}
J(w) &= \frac{|W^T \mu_1 - W^T \mu_2|^2}{\tilde{s}_1^2 + \tilde{s}_1^2} \\
|W^T \mu_1 - W^T \mu_2|^2 &= (W^T \mu_1 - W^T \mu_2)(W^T \mu_1 - W^T \mu_2)^T = W^T \underbrace{(\mu_1 - \mu_2)(\mu_1 - \mu_2)^T}_{S_B} W = W^T S_B W \\
\tilde{s}_1^2 + \tilde{s}_1^2 &= \sum_{x \in C_1} (W^T x - W^T \mu_1)^2 + \sum_{x \in C_2} (W^T x - W^T \mu_2)^2 \\
&= \sum_{x \in C_1} W^T \underbrace{(x - \mu_1)(x - \mu_1)^T}_{S_1} W + \sum_{x \in C_2} W^T \underbrace{(x - \mu_2)(x - \mu_2)^T}_{S_2} W \\
&= W^T S_1 W + W^T S_2 W = W^T (S_1 + S_2) W = W^T (S_W) W \\
J(w) &= \frac{|W^T \mu_1 - W^T \mu_2|^2}{\tilde{s}_1^2 + \tilde{s}_1^2} = \frac{W^T S_B W}{W^T S_W W}
\end{aligned} \tag{3.30}$$

Where  $S_B$  and  $S_W$  are the between-class scatter and within-class scatter matrices of the training data.

For finding the appropriate value of  $w$  that maximizes  $J(w)$ , differentiation is applied and set equal to zero:

$$\begin{aligned}
\frac{\partial}{\partial W} \left( \frac{W^T S_B W}{W^T S_W W} \right) &= 0 \\
\frac{\frac{\partial}{\partial W} (W^T A W) = 2AW}{\rightarrow} &= \frac{(W^T S_W W (2S_B W) - W^T S_B W (2S_W W))}{(W^T S_W W)^2} = 0 \\
\Rightarrow (W^T S_W W (2S_B W) - W^T S_B W (2S_W W)) &= 0 \\
\frac{\text{Deviding by } 2W^T S_W W:}{\rightarrow} & \left( (S_B W) - \underbrace{\frac{2W^T S_W W}{W^T S_B W}}_{J(W)} (S_W W) \right) = 0 \\
\Rightarrow S_B W - J(W) S_W W &= 0 \xrightarrow{\text{As } J(W) \text{ is a scalar:}} S_B W = J(W) S_W W \\
\Rightarrow S_W^{-1} S_B W &= J(W) W
\end{aligned} \tag{3.31}$$

The final formula in 3.31, is an eigen-value equation and the maximum value for  $J(W)$  is equivalent to the largest eigen-value of  $S_W^{-1} S_B$ , which is equivalent to:

$$J(W)_{\max} = S_B^{-1} (\mu_1 - \mu_2) \tag{3.32}$$



To extend these formulas to multiple classes, our  $X$ ,  $Y$ , and  $W$  are expressed as follows:

$$\begin{aligned}
 X &= \begin{bmatrix} x_1(1) & x_2(1) & \cdots & x_M(1) \\ x_1(2) & x_2(2) & \cdots & x_M(2) \\ \vdots & \vdots & \cdots & \vdots \\ x_1(n) & x_2(n) & \cdots & x_M(n) \end{bmatrix}_{n \times M} \\
 Y &= \begin{bmatrix} y_1(1) & y_2(1) & \cdots & y_M(1) \\ y_1(2) & y_2(2) & \cdots & y_M(2) \\ \vdots & \vdots & \cdots & \vdots \\ y_1(M-1) & y_2(M-1) & \cdots & y_M(M-1) \end{bmatrix}_{M-1 \times M}
 \end{aligned} \tag{3.33}$$

$$W = W^T X \qquad W = [W_1, W_2, \dots, W_{C-1}]$$

Note that for  $M$ -classes, we have  $M - 1$  projection vectors. Then  $S_W$  and  $S_B$  in equation 3.29 become:

$$\begin{aligned}
 S_W &= \sum_{i=1}^M S_{C_i} \\
 S_B &= \sum_{i=1}^M N_i (\mu_i - \mu)^2 \quad \text{where} \quad \mu = \frac{1}{N} \sum_{\forall x} x \quad \text{and} \quad \mu_i = \frac{1}{N_i} \sum_{x \in C_i} x
 \end{aligned} \tag{3.34}$$

where  $N$  = Number of all data      and       $N_i$  = Number of data in class  $C_i$

As shown above, unlike the PCA which maximizes the overall scatter, the LDA method maximizes the ratio of between-classes to within-classes scatter. This method has been applied to face recognition by Belhumeur et al. [7]. Based on their approach, LDA is being applied to learn a class-specific transformation matrix ( $W$ ) that omits other information regarding noise, such as illumination, leading to a basic improvement when compared to the PCA approach. The use of the LDA, which uses the best facial features to separate the persons in the training set, is dependent on the input set. If the system is trained with the well-illuminated faces, it would not be a robust model to recognize faces in badly-illuminated or unconstrained conditions.

Figure 3.6 shows the reconstruction of the projected face images using the Fisher-faces technique:



Figure 3.6: The fisherfaces corresponding to the sample faces

### 3.3 Feature-Based Approaches

In contrast to the methods presented in the previous sub-sections, which treat the whole image as a single vector. Feature-based approaches focus on extracting local features related to edges, corners, and other structures within an image. Since these approaches extract information by considering the important parts inside the image, they map better to face recognition problems in comparison to global representation techniques. In this section, we describe LBPH, SIFT, BRIEF and FREAK which are popular feature-based approaches in face recognition.

#### 3.3.1 Local Binary Patterns Histograms

Local Binary Pattern Histogram (LBPH) is one of the most powerful texture-encoding descriptors. It extracts the spatial structure of each pixel by looking at the intensity of its neighbors. These informative features are extracted for all the images' pixels, and then occurrences statistics for different blocks are collected. This section will cover the Local Binary Pattern Histogram method and explain how these local features are collected from an image.

The basic version of the local binary pattern operator, proposed by Ojala [73], consists in extracting a pattern from a  $3 \times 3$  block of an image. In this method, the central pixel is used as a threshold when compare with its neighbors. If this center pixel's value is greater

than the neighbor's value, we set the neighbor's value as "1", otherwise, it is set to "0". As we have 8 neighbors in a  $3 \times 3$  block, LBP produces an 8-digit binary number. This number will be converted to a decimal numeral system to get a number between 0 and  $2^8 - 1$ .

We then divide the image into a number of regions and extract the histogram of LBP values inside each patch. These histograms characterize the visual pattern inside each region. Each histogram is generally normalized such that the sum of its elements is 1. Finally we concatenate histograms of all regions to build the feature vector for the whole image of the face. The whole procedure is in Figure 3.7.

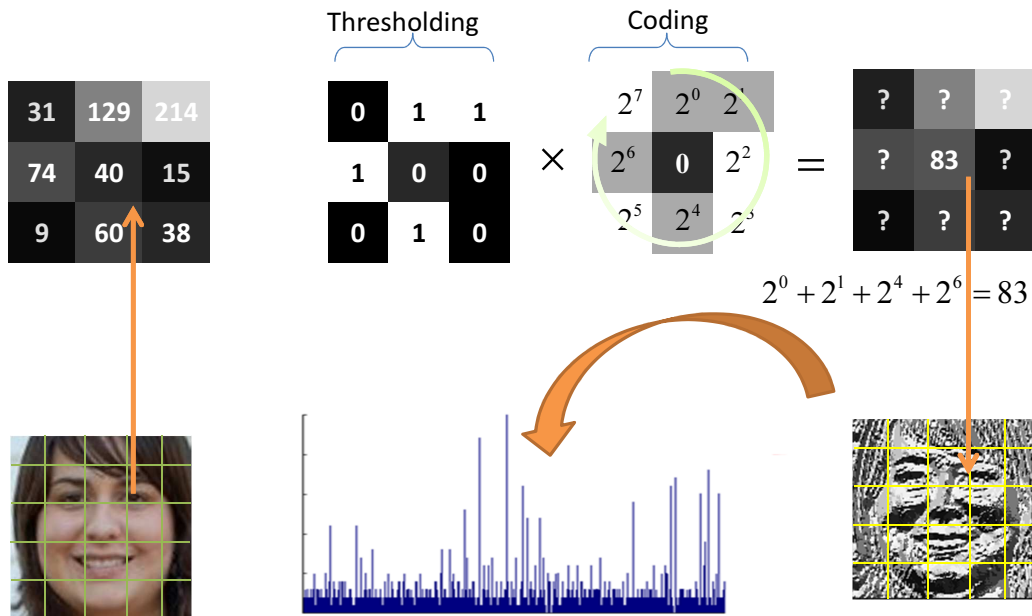


Figure 3.7: The LBP descriptor

This framework, which uses  $3 \times 3$  blocks, can be easily extended to larger blocks. Consider a monochrome image,  $I$ , and let  $I_g$  be its gray level image, where  $I_g(x, y)$  indicates the intensity of pixel  $(x, y)$ . Then the  $N$  circular neighborhood pixels with radius  $R$  around each pixel will be:

$$\begin{aligned}
 x_p &= x + \left[ R \cos\left(\frac{2\pi p}{N}\right) \right] \\
 y_p &= y - \left[ R \sin\left(\frac{2\pi p}{N}\right) \right] \quad \text{where } p = 0, \dots, N-1
 \end{aligned}$$

$$LBP_{N,R}(x_c, y_c) = \sum_{p=0}^{N-1} s(I_g(x_p, y_p) - I_g(x_c, y_c)) 2^p \quad \text{where } s(z) = \begin{cases} 1 & \text{if } z \geq 0 \\ 0 & \text{if } z < 0. \end{cases} \quad (3.35)$$

In the formula shown above, we must also take into consideration the following facts:

- In computing the pixel values, sampling points that are not on the sampling grid, bilinear interpolation can be employed.
- Since extracting  $LBP_{N,R}$  from images' borders is not possible, only the central part of the image is being considered.

This extension of  $LBP$  is a generic formulation of the operator that allows us to use a larger neighborhood.

### Uniform Patterns

One of the important characteristics of a good descriptor is its invariance to the rotation of the target image. To this end, the uniform pattern has been proposed later by Ojala et al. [72] as an extension of the  $LBP$  method. They [72] defined a uniformity measurement  $U$  (pattern) that computes the number of bitwise transitions from 0 to 1, or 1 to 0. This measurement is expressed as follows:

$$\begin{aligned}
 U(LBP_{N,R}(I_g(x_c, y_c))) &= |s(I_g(x_{N-1}, y_{N-1}) - I_g(x_c, y_c)) - s(I_g(x_0, y_0) - I_g(x_c, y_c))| \\
 &+ \sum_{p=1}^{N-1} |s(I_g(x_p, y_p) - I_g(x_c, y_c)) - s(I_g(x_{p-1}, y_{p-1}) - I_g(x_c, y_c))|
 \end{aligned} \tag{3.36}$$

For example,

$$\begin{aligned}
 \text{pattern} = \text{"00000000"} &\Rightarrow U(\text{"00000000"}) = 0 \\
 \text{pattern} = \text{"00000111"} &\Rightarrow U(\text{"00000111"}) = 1 \\
 \text{pattern} = \text{"00011000"} &\Rightarrow U(\text{"00011000"}) = 2 \\
 \text{pattern} = \text{"10011011"} &\Rightarrow U(\text{"10011011"}) = 4
 \end{aligned}$$

They then map the pattern ( $p$ ) to its corresponding number if the number of transitions is less than or equal to 2 ( $U(p) \leq 2$ ) and the rest of the patterns are mapped to a unique number. They applied this extension to the circular pattern extracted from LBP and referred to it as the uniform local binary pattern (uLBP):

$$LBP_{N,R}^{riu2} = \begin{cases} \sum_{p=0}^{N-1} s(I_g(x_p, y_p) - I_g(x_c, y_c)) & \text{if } U(LBP_{N,R}) \leq 2 \\ N(N-1) + 3 & \text{otherwise} \end{cases} \tag{3.37}$$

The superscript *riu2* shows the rotation invariant uniform patterns of the  $U$  function with, at most, 2 bitwise transitions having been applied. This way of mapping for patterns can be interpreted as encoding different local structures, such as spots, flat areas, edges, edge ends, and curves, as shown in Figure 3.8:

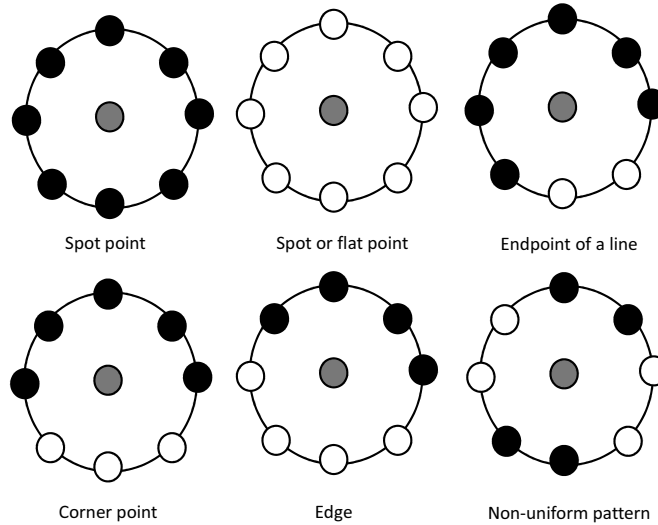


Figure 3.8: Examples of different texture structures detected by the LBP method (black circles represent of ones' "1", and white circles correspond to zeros "0")

To this end, it has been observed that uniform LBP (uLBP) patterns have better performances in recognition tasks when compared to LBP.

### 3.3.2 Scale-Invariant Feature Transform (SIFT)

The Scale Invariant Feature Transform (SIFT) descriptor proposed by Lowe [63] is a powerful description method for characterizing image regions, which has been widely used for various computer vision applications. SIFT produces a 128-dimensional representation for each image region by employing a local gradient operator around the region's center point (which is called a keypoint). This representation is built by using a 3D (2 locations and 1 orientation) histogram of gradient locations and orientations. In this process, each patch surrounding a keypoint is scaled at different ratios, and then the orientation histogram over  $4 \times 4$  regions is computed. The orientation of each region is computed from a histogram of a gradient magnitude in eight directions. These orientation histograms

from 16 regions are concatenated and result in a 128 element feature descriptors. The quantization of gradient locations and orientations makes SIFT descriptors robust to small geometric distortions and certain illumination variations.

### 3.3.3 Binary Robust Independent Elementary Features (BRIEF)

The Binary Robust Independent Elementary Features (BRIEF), proposed by Calonder et al. [14], is a binary descriptor that is fast and simple to compute. This approach is similar to the method of LBP in terms of evaluating differences between intensity pixels. The BRIEF method first smooths the image patches to reduce noise. Then, the differences between the pixels' intensity is employed to construct the descriptor. For this purpose, Calonder et al. [14] defined a test  $\tau$  between pixel  $I(x_1, y_1)$  and pixel  $I(x_2, y_2)$  by:

$$\tau(I(x_1, y_1), I(x_2, y_2)) = \begin{cases} 1 & \text{if } I(x_1, y_1) < I(x_2, y_2) \\ 0 & \text{o.w} \end{cases} \quad (3.38)$$

The BRIEF descriptor for a patch is constructed in a  $k$ -length bitstring by performing a test on a set of pixels within it. In order to generate this descriptor for a patch  $P$ , the following score is computed for  $k = 128, 256$ , or  $512$ :

$$d_P = \sum_{i=1}^k 2^{i-1} \tau(I(x_i, y_i)) \quad (3.39)$$

In order to find an appropriate set of pixels, there are many ways to select them from a patch size  $N \times N$ . For this purpose, Calonder et al. [14] conducted an experiment over the following five sampling geometries:

- 1 Selection has been done by using an i.i.d.  $\text{Uniform}(-\frac{N}{2}, \frac{N}{2})$  distribution, which means that pixels are chosen by equivalent distribution from all pixels over the region.
- 2 Pixels have been sampled by an i.i.d.  $\text{Gaussian}(0, \frac{N^2}{25})$  distribution, which means that they are employed by an isotropic Gaussian distribution with experimentally adjusted variance equivalent to  $\frac{N^2}{25}$ .
- 3 Pixels have been sampled by two zero mean i.i.d. Gaussian distributions, one with variance  $\frac{N^2}{25}$  centered on origin and another one with variance  $\frac{N^2}{100}$  centered on the selected pixel. These variances have been tuned by experiments to capture more local information from a patch.

4 Pixels were chosen by random selection over a coarse polar grid.

5  $K$  possible points over diagonals of coarse polar grid centered by  $I(0, 0)$ .

Making use of their extensive recognition setup, Calonder et al. [14] reported that second selection (i.i.d. Gaussian  $(0, \frac{N^2}{25})$ ) leads to the best result in terms of recognition rate (i.e. the rate of correct decisions to the number of overall decisions, which can be interpreted as the Rank 1 identification rate). Furthermore, they claimed that the BRIEF descriptor is robust against image blurs and illumination changes while still being sensitive to rotation and scale changes.

### 3.3.4 Fast Retina Keypoint (FREAK)

The bio-inspired FREAK descriptor proposed by Alahi et al. [5] employed a retinal sampling circular grid. The FREAK method employs 43 sampling patterns based on retinal receptive fields that are shown in Figure 3.9.

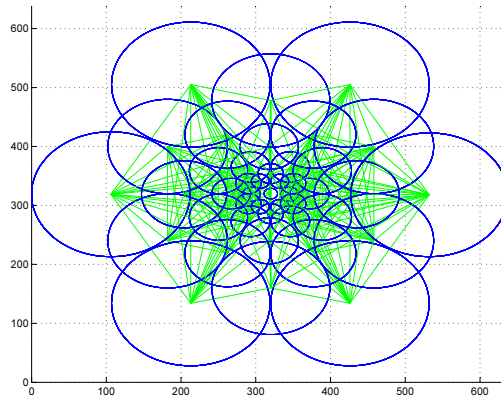


Figure 3.9: 43 sampling patterns used in FREAK method

These 43 receptive fields are sampled by decreasing factors as the distance from the patch's center yields to a thousand potential pairs to extract a binary descriptor. Each pair is smoothed with Gaussian functions, and then binary descriptors are generated by setting a threshold and considering the sign of differences between pairs. For a pair,  $P_a$ , this descriptor is defined by

$$D(P_a) = \sum_{i=1}^k 2^i T(P_a) \quad (3.40)$$

where

$$T(P_a) \begin{cases} 1 & \text{if } I(P^r 1_a) > I(P^r 2_a) \\ 0 & \text{o.w} \end{cases} \quad (3.41)$$

As it would be preferable to select pairs with a high discriminant power and ignore highly correlated ones, FREAK examined all possible choices for about 50,000 detected keypoints in a set of images. It then sorts them based on their discrimination power.

This method selected the 512 most discriminative pairs. It group these 512 pairs into four clusters - each having 128 pairs - which has the benefit of not only keeping the symmetric scheme, but also of capturing the coarse-to-fine structure.

Another factor that should be considered is the fact that long-distance receptive fields are used to capture orientation, and short-distance receptive fields are used to capture more details from the patch. Consequently, the first resulting cluster is initially used to estimate the position of the object of interest, and the short distance cluster is then used to validate our estimation. This scheme approximates the human visual system by considering the fact that humans look at a scene with discontinuous eye movements. This searching strategy is called a "Saccadic" search. The Saccadic search scheme in feature-matching applications can dramatically reduce the processing time by discarding nontarget features as quickly as possible by comparing only 16 bytes in the first cluster.

### 3.4 Block-based Bag of Words (BBoW)

The Bag-of-Words (BoW) method is a powerful technique in object recognition [82] that represents an object by creating a histogram over extracted elements from sample images from different categories. This method maps extracted features from a large domain to a smaller one that is created by clustering meaningful elements extracted from similar images. Z. Li et al. [59] applied this approach to face recognition by employing dense SIFT features extracted from different patches through the image.

Since face objects all share the same basic structure and elements, each face can be represented by building a histogram over a collection of candidates. This collection, called codebooks, contains different candidates corresponding to different local regions, which are called codewords. The main focal point of this approach is then creating rich codebooks and representing each face in the form of occurrence frequency distribution of codewords in the constructed codebooks.

When constructing codebooks, the first step is to divide face images into regions denoted



by patches. Then, features within each patch are extracted for all images. Those belonging to certain specific areas are gathered and fed into the clustering process in order to be partitioned into  $K$  clusters. By choosing a set of meaningful and appropriate features, recognition become more robust against the noise and other possible intrinsic variations.

Once the codebook is created, the algorithm characterizes each region by mapping all extracted feature vectors to the closest codewords for that region. In other words, each region is described based on the occurrence statistics of the set of codewords. Finding the closest codeword for each feature vector is based on a distance metric that depends on the type of features. Euclidean distance, Hamming distance, Histogram Intersection, and cosine similarity are among the most useful distance metric systems. The thus obtained histograms are concatenated to represent the face to be used in the training and testing stages. The whole procedure of our block-based bag of words (BBoW) method to extract facial features for face recognition is shown in Figure 3.10.

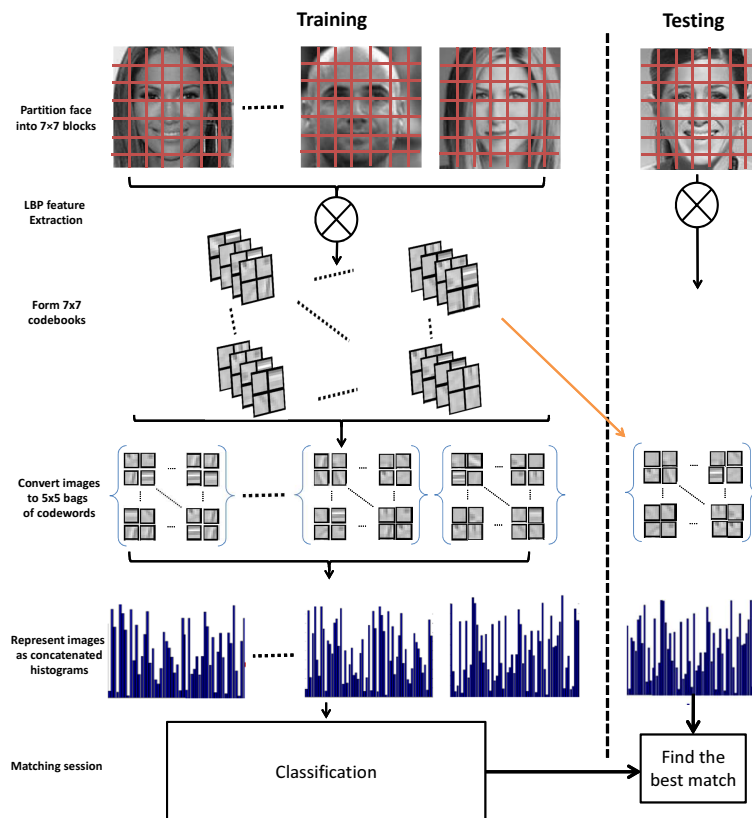


Figure 3.10: Framework of Block-Based bag of Words(BBoW)

As mentioned above, one of the main stages of BoW is to build an appropriate codebooks. For this purpose, different unsupervised methods can be employed, such as  $K$ -means and random selections. In the subsequent sections, we briefly describe these two methods.

## **$K$ -means Clustering**

$K$ -means clustering proposed by Stuart Lloyd [62], is a popular technique in data clustering. This method finds certain points that correspond to the center of clusters by using the fact that any point in a cluster is closer to its corresponding center than to the other clusters' centers.

Assuming there are  $K$  clusters with centers  $\mu_1, \dots, \mu_K$  belonging to  $R^d$  space,  $K$ -means clustering aims to minimize overall distances between all data and the corresponding cluster's centers:

$$L = \sum_{i=1}^K \sum_{i: x_i \text{ assigned to } \mu_j} \|x_i - \mu_j\|^2 = \sum_{i=1}^K \sum_{i: x_i \text{ assigned to } \mu_j} \alpha_{i,j} \|x_i - \mu_j\|^2 \quad (3.42)$$

where

$$\alpha(i, j) = \begin{cases} 1 & \text{if } x_i \text{ assigned to } j \\ 0 & \text{o.w} \end{cases} \quad (3.43)$$

$K$ -means tries to minimize  $L(3.42)$  with respect to all the  $\alpha_{i,j}$  and  $\mu_j$ , by applying the following iterations:

- Choosing an optimal set of  $\alpha$ s for the fixed values of  $\mu$ s
- Choosing an optimal set of  $\mu$ s for the fixed values of  $\alpha$ s

This greedy algorithm repeats these two iterations until convergence is achieved.

## **Random Selections**

Random cluster selection is another popular technique in codebook construction. This method, which requires fewer parameters to be tuned for constructing clusters, is popular because of its simplicity and its ease of implementation. It simply consists in choosing a random number of features from a large set of data. Studies have even shown [48] that selecting clusters by  $K$ -means does not beget better results than random selection does. In fact, by gathering a large number of features from each local region,  $K$  number of

features are randomly selected within features regarding each cluster label and will be evenly distributed in the codebooks.

## 3.5 Matching face images for classification

Previous sections described how to extract features from a face image. These extracted features are used in the next stage to find the nearest face in a dataset. This procedure can be done by using Brute-force Matching, Support Vector Machine (SVM), Artificial Neural Network (ANN), or a Bayesian classifier. As Brute-force Matching is quite simple and easy to implement, we go over this method and apply it to find the nearest face in a trained dataset. The SVM classifier is explained in chapter 4.

### 3.5.1 Brute-force Matching

Brute-force Matching is a popular and simple technique that is applicable to a wide variety of problems, including face identification challenges. In this approach, we find the best match for a face object among the stored faces. Once a face is captured, features regarding the face are extracted and the closest pre-extracted feature vector is found. Finding the closest face is dependent on the type of extracted features and how the distance between them is computed. To identify a face among a set of faces, there are two factors to analyze: an appropriate distance metric and the setting of a threshold for the identification of unknown individuals. The next section presents different forms of measurement for the histogram and Hamming distances, while identification of unknown faces is discussed in the results section.

### 3.5.2 Compare Histograms

Of particular interest to us is the case of histogram descriptors. The Local binary pattern histogram and the Bag-of-Words methods collect occurrence statistics of each image by using a histogram representation. To compare these types of descriptors, the Histogram Intersection, Chi-Square, and Correlation method can be employed.

The Histogram Intersection is a robust technique that is not affected by rotation and small changes in distance. This distance is defined as follows:

$$d(H_1, H_2) = \sum_{i=1}^n \min(h_1^{(i)}, h_2^{(i)}) \quad (3.44)$$

Another measurement for histogram comparison is the Chi-Square method. Inspired by the  $\chi^2$  test-statistic [83], this method has been employed in several texture and object categories' classification algorithms (e.g. [23], [99], [93], and [8]). In the most cases, the differences between large bins in histogram is less important than the difference between small bins. So Chi-Square distance is defined by the fact that differences between the large bins' value being equivalent to the differences between the small bins' value. This can be accomplished by taking the norm of the bins into account. The two following equations are popular measurements to compute this distance:

$$d(H_1, H_2) = \sum_{i=1}^n \frac{(h_1^{(i)} - h_2^{(i)})^2}{h_1^{(i)}} \quad (3.45)$$

$$d(H_1, H_2) = \sum_{i=1}^n \frac{(h_1^{(i)} - h_2^{(i)})^2}{h_1^{(i)} + h_2^{(i)}}$$

The Correlation Method considers each histogram as a 1-D signal. It then computes the correlation with the following formula:

$$d(H_1, H_2) = \frac{\sum_{i=1}^n (h_1^{(i)} - \bar{h}_1)(h_2^{(i)} - \bar{h}_2)}{\sqrt{[\sum_{i=1}^n (h_1^{(i)} - \bar{h}_1)^2][\sum_{i=1}^n (h_2^{(i)} - \bar{h}_2)^2]}} \quad (3.46)$$

In the Histogram Intersection distance and the Correlation distance, a high score value indicates that the two histograms present a measurably better match than two histograms with a low score value. Conversely, the lowest value in the Chi-Square method indicates that the two histograms are a better match.

These bin-to-bin distances are generally sensitive to quantization effects, and the differences between their accuracy is not very significant. Therefore, because of its ease of implementation, Histogram Intersection is selected here.

### 3.5.3 Hamming Distances

Once features have been extracted, we can compare them by different distance measurements. The BRIEF and FREAK methods are associated with constructing binary descriptors for images. In this case, for two  $k$ -length binary descriptors  $D(I_1) \in \{0, 1\}^k$

and  $D(I_2) \in \{0, 1\}^k$  that represent two points in  $k$  dimensional Hamming space, the Hamming distance is defined as

$$Ham(D(I_1), D(I_2)) = \sum_{i=1}^k D_i(I_1) \otimes D_i(I_2) \quad (3.47)$$

where  $\otimes$  is the single instruction bitwise XOR operation.

## 3.6 Experimental Results

This section provides the result of the described methods on two publicly available databases: the FERET and LFW database. All codes are implemented in C++ using the OpenCV 2.4.2 library, which is an open source library specialized for computer vision applications.

The rest of this section is organized as follows: Section 3.6.1 describes the two publicly available databases which have been used to evaluate our methods. In section 3.6.2 we compare two global representation approaches, PCA and LDA, with the LBPH feature-based technique. Then, in sub-section 3.6.3 we employ edge detection techniques to remove the artifacts induced by noise and appearance changes. In contrast to the previous sub-section, we use the results of the edge detection techniques as an input of PCA, LDA, and LBPH, and we show that a significant improvement can be obtained by using these techniques. In section 3.6.4, we evaluate the SIFT, BRIEF and FREAK descriptors on the FERET and LFW database. Thereafter, in section 3.6.5 we analyze Bag-of-Words method on the SIFT and LBPH descriptors. Finally, in section 3.6.6, we propose a model to detect unknown individuals. Additionally, extensive experimentation has been carried out to determine the optimal value for parameters of our face recognition framework.

### 3.6.1 Dataset

The performance of the different descriptors explained above has been evaluated using standard benchmark databases for face recognition: the Facial Recognition Technology (FERET) database and the Labeled Faces in the Wild (LFW) database.

## The Facial Recognition Technology (FERET) Dataset

The FERET Database [75] of face images collected between August 1993 and July 1996, contains 1564 sets of images for a total of 14,126 images. These images were captured at a variety of illumination levels, face positions and includes people with various facial expressions, ages, degrees of occlusion, and facial hair. The image data has been captured at a resolution of  $180 \times 200$ . Some other information, such as age, ethnicity, and gender is also included in the database ground truth files.

A set of different categories of images in the database is shown in Figure 3.11. Among these categories, the five frontal views (Fa, Fb, Fc, Dup I, and Dup II) are the most popular.

- Fa probes: images are taken of neutral facial expressions, all with the same lighting (1196 images)
- Fb probes: images are captured with an alternative frontal expression seconds after the Fa (1195 images)
- Fc probes: images are taken under different levels of illumination (194 images)
- Dup I probes: images are taken anytime between one minute and 1031 days after the corresponding Fa (722 images)
- Dup 2 probes: images are taken at least 18 months after their corresponding Fa (234 images)

All images in the database are cropped and normalized by employing an affine transform to the size of  $100 \times 100$  using the coordinates of the faces' eyes and mouths as given by ground truth.



Figure 3.11: Sample faces in FERET database

## Labeled Faces in the Wild (LFW) Dataset

The LFW database [43] is a rich database containing over 13,000 photographs of faces in unconstrained conditions which were collected from the Web. The LFW images are captured from faces with a variety of poses, illuminations, backgrounds, expressions, clothing, hairstyles, cosmetics, and so on. These images belong to people of different ages, genders, and ethnicities and are good examples of the real world images with which most face recognition applications strive to work. As such, training a system to employ this type of database, ensures that the proposed system can be generalized to real-world applications.

Later, a commercial system [42] was used to align the images in the LFW database so that the positions of the faces' eyes and mouths would be the same for all face images.

Of the 5,749 individuals in this database, 4,069 people have only one image and the others have two or more images. In order to build a dataset suitable for face recognition benchmarking, we collected a set of face images from 20 individuals having 10 images per person.



Figure 3.12: Collected LFW database

It must be noted that the LFW database has more face images includes people of Western ethnicities than of other ethnic groups. Also, much like the FERET database, LFW

images were taken in a short period of time. Therefore, a good verification performance on LFW does not necessary guarantee effectiveness in a real environment.

In this section we go through the described methods and test them on two LFW and FERET frameworks for face recognition.

### 3.6.2 Analysis of PCA, LDA, and LBPH

In this section, the performance of PCA, LDA and LBPH were evaluated for the purpose of face identification on the FERET and LFW databases. Two FERET image sets (Fa and Fb) have been used in our face recognition test. In this experiment the 1,196 images in the Fa probe were used for training, and the system was tested on the 1,195 images of the Fb probe. All images in the training or testing sets were scaled to  $100 \times 100$ .

In face identification, one of the most important parameters is the size of the available database. Since increasing the number of training samples would change the results, a good testing would include testing and training sets of different sizes. For this purpose, we tested random sets of 100, 300, and 800 in five runs on the FERET database. The results for the entire database are reported in the last column of Table 3.1.

Table 3.1: The recognition rate of PCA, LDA, and LBPH with different numbers of training on the Fb probe set of the FERET database. First row indicates the number of images used for training and, under parantheses, the number of test images

Methods	100(100)	300(300)	800(800)	1196(1195)
PCA	75.62	69.67	64.43	71.11
LDA	73.15	69.33	62.74	68.43
LBPH	90.8	88.12	82.68	78.39

As it can be seen, LBPH performs better than PCA and LDA. In the next step, we test these methods to evaluate their robustness against the other parameters such as illumination and the aging factor. As mentioned in the previous section, the FERET dataset provided the Fc that contains illumination changes, and Dup I and Dup II that includes aging over time. By testing these probes, it is evident that the tested methods appear to be sensible to these changes, as shown in Table 3.2.



Table 3.2: The recognition rate of PCA, LDA, and LBPH on the FERET database probe sets trained using Fa set.

Methods	Fa(Fb)	Fa(Fc)	Fa(Dup I)	Fa(Dup II)
PCA	71.11	11.86	23.96	8.99
LDA	68.43	15.76	22.02	10.27
LBPH	78.39	23.71	28.39	11.98

We also tested these methods on the LFW database ([43]). This evaluation is repeated over nine iterations, where, at iteration  $i$ , the first  $i$  images are used for training and the last  $(10 - i)$  images are used for testing. As seen in Table 3.3, LBPH seems to be superior when the number of training images increases.

Table 3.3: The recognition rate of PCA, LDA, and LBPH on the LFW database

Methods	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
PCA	21.11	19.38	27.14	28.33	30	33.75	35	37.5	35	26.78
LDA	16.67	29.38	36.43	47.5	58	55	55	57.5	55	39.34
LBPH	22.78	35.63	41.43	44.17	51	52.5	50	52.5	50	40.33

### 3.6.3 Analysis of Edge Detection Operators

In this section, we evaluate various types of edge detection operators on our data. The objective of using edge detectors is to limit the effect of some parameter variations such as illumination and age from the face’s main structure. We first apply different edge detectors such as Sobel, Canny, and Laplacian operators on the image. Then, the resulting image is fed into the PCA, LDA, and LBPH methods to extract their face descriptors.

The results of these operators on Fc probes of the FERET database are reported in Table 3.4:

Table 3.4: The recognition rate of PCA, LDA, and LBPH methods combined with different edge operators on the Fc probe of the FERET database

Methods	Sobel	Laplacian	Canny	raw image
PCA	65.46	30.31	53.09	11.86
LDA	64.95	35.91	59.79	15.76
LBPH	60.31	43.21	31.96	23.71

The parameters responding of these edge operators, such as kernel size, and sigma size, have been tuned to get the best result possible. It is evident that employing edge detector operators improves the algorithms' robustness against the illumination changes. The best combination corresponds to the Sobel and PCA methods.

We also tested the above-mentioned methods on three other categories in the FERET dataset: Fb, Dup I, and Dup II. The Sobel edge detector once again outperformed the other edge detection methods. The results are provided in Table 3.5.

Table 3.5: The recognition rate of the PCA, LDA, and LBPH combined with the Sobel edge operators on the FERET database probe sets

Methods	Fa(Fb)	Fa(Dup I)	Fa(Dup II)
PCA+Sobel	48.41	26.48	15.56
LDA+Sobel	42.38	22.33	13.42
LBPH+Sobel	80.49	31.16	28.39

In the next experiment, we employed this method to test face recognition performance in an uncontrolled environment. For this purpose, we tested this method on the LFW dataset:

Table 3.6: The recognition rate of PCA, LDA, and LBPH combined with Sobel edge operators on the LFW database

Methods	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
Sobel+PCA	19.44	28.75	26.43	28.33	29	31.25	33.33	30	40	27.33
Sobel+LDA	20	16.25	18.57	30	31	31.25	40	32.5	45	25.11
Sobel+LBPH	27.78	38.75	45.71	45	51	55.25	48.33	52.5	50	42.8

It can be seen in Table 3.6 that extracting a histogram of local binary patterns significantly outperforms the PCA and LDA methods. Adding Sobel to LBPH and PCA methods improved their discriminating power, but it is still far from the acceptable performance necessary for real-world applications.

### 3.6.4 Analysis of SIFT, BRIEF, and FREAK methods

In this section, we report results of applying the SIFT, BRIEF, and FREAK methods on our two benchmark datasets. As we previously explained, SIFT produces a 128-dimensional representation for each image region using a 3D (2 locations and 1 orientation) histogram of gradient locations and orientations. The use of the BRIEF and FREAK methods as texture-encoding descriptors based on local binary patterns was also tested. It should be mentioned that the distances between BRIEF and FREAK descriptors are computed by Hamming distance. The results of these methods on four probes of Fb, Fc, Dup I, and Dup II are given in Table 3.7.

Table 3.7: The recognition rate of the SIFT, BRIEF, and FREAK methods on the FERET database probe sets

Methods	Fa(Fb)	Fa(Fc)	Fa(Dup I)	Fa(Dup II)
SIFT	86.18	77.84	46.24	22.22
BRIEF	78.57	35.54	36.43	16.24
FREAK	76.72	48.45	36.70	24.36

As expected, the SIFT method shows better result on the  $Fc$  probes, which shows the robustness of this method against illumination variations.

Thus, in real world situations where all possible variations can be observed, a recognition task based on methods which are sensitive to appearance variations have a low level of accuracy. To demonstrate this, the results of empirical investigation on the LFW have been shown in Table 3.8.

Table 3.8: The recognition rate of the SIFT, BRIEF, and FREAK methods on the LFW database

Methods	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
SIFT	33.89	46.25	57.86	60	63	68.75	63.33	65	60	53.56
BRIEF	25.56	32.5	38.57	41.67	46	51.25	53.33	55	55	39.33
FREAK	27.78	35.63	45.71	46.67	48	53.75	55	57.5	60	42.89

The above results show how popular methods for feature extraction offer results for face recognition that are far from acceptable.

From the results indicated above, it is evident that recognizing a face simply employing powerful descriptors cannot lead us to an accurate system. A good approach to tackling this problem is to apply methods that try to describe the captured using global structures. In the subsequent section, we test the BoW method on the LFW dataset to show how much our results can be improved by adjusting and finding appropriate parameters to reach the best possible results.

### 3.6.5 Analysis of the BoW approach

In this section we experiment the Bag-of-Words approach on the LFW and FERET datasets. Here, the Bag-of-Words method is constructed from features extracted by LBP and SIFT descriptors and then its corresponding parameters are set to improve the recognition accuracy.

As previously mentioned, choosing the closest word in codewords depends on the type of descriptors. To compare histograms of LBP features, we use Hamming distance as a simple and quick distance metric, and for SIFT descriptors we employ Euclidean measurements. Making use of the Bag-of-Words method requires to tune the different parameters. In the following example, LBP and SIFT were extracted in a window size of 8 by 8 around pixels with a distance of 4 along the x-axis and 3 along the y-axis. One feature vector is calculated on the center of each grid. Finding the appropriate size of gridding schemes is another parameter which should be carefully set. We later test different visual words on each block with different grid sizes. In Table 3.9, the results of applying BoW methods over LBP, uLBP and SIFT features in different gridding schemes with 20 number of words for each region is provided:

Table 3.9: The recognition rate of the BoW method on features extracted by LBP, uLBP, and SIFT methods on the LFW database

Methods	Gridding Scheme	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
BoW-LBP	$4 \times 4$	32.78	50.63	58.57	60.83	60	62.5	63.33	62.5	55	53.22
BoW-LBP	$7 \times 7$	40.18	48.96	62.62	64.45	71.3	75	73.3	73.3	65	59.25
BoW-uLBP	$7 \times 7$	40.56	48.75	62.39	63.61	69.7	65.42	71.67	69.17	58.33	57.67
BoW-uLBP	$8 \times 8$	35	40	53.57	59.17	65	63.75	63.33	65	65	51.78
BoW-SIFT	$7 \times 7$	32.7	43.13	52.86	54.17	60	67.5	73.3	67.5	65	51.65

As seen in Table 3.9, BoW on LBP feature with gridding size  $7 \times 7$  performs better than others. But processing the 256-bin histogram is so expensive in comparison with 59-bin histogram in terms of memory and speed.

The results of BoW method over LBP features on four probes of Fb, Fc, Dup I, and Dup II with 20 number of words have been provided in the following table:

Table 3.10: The recognition rate of BoW method over LBP features on the FERET database probe sets

Methods	Fa(Fb)	Fa(Fc)	Fa(Dup I)	Fa(Dup II)
BoW-uLBP	93.05	84.43	46.88	23.94

As shown, it is obvious that the tuning of parameters to optimize a subset of the results is a necessary step in the BoW method. If this step is omitted, results may vary by a large number.

One of the other main configuration in this procedure is face alignment. Since each element should be represented by the correct words, they should be located in the right positions. To clarify this matter, we have done an experiment based on face alignment using different potential locations of eyes. By changing the eyes's locations, unrelated words are employed to represent the eyes recognition accuracy will be reduced. The results of this experiment based on gridding scheme  $7 \times 7$ , 20 number of words, and  $(x_{step}, y_{step}) = (4, 4)$  have been provided in the following table. The second row corresponds to the alignment of faces where the eyes' locations in first row changed only by 5 px; in the third row, they changed by 10 px. These changes are applied in the Y-direction, and the codewords corresponding to each grid have not been changed:

Table 3.11: The recognition rate of the BoW method on features extracted by uLBP with different face alignment on the LFW database

Methods	eyes Y location	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
BoW-uLBP	$(y_e : 114)$	32.78	50.63	58.57	60.83	60	62.5	63.33	62.5	55	53.22
BoW-uLBP	$(y_e : 119)$	28.33	35	42.14	44.17	44	48.75	50	50	50	40.22
BoW-uLBP	$(y_e : 124)$	26.11	34.38	41.42	42.5	49	51.25	46.67	57.5	60	40.44

This demonstrates that a slight change in the locations of a face’s features can change the structure of the BoW model and the system will be less accurate.

It is worth mentioning that all the images used in our tests were aligned based on the location of the eyes and the mouth. Since detection of eyes and mouth might be an expensive task in terms of implementation or speed for some face detection systems, we exploit BoW of LBP features to discover how accurate these models are without using any alignment. Table 3.12 shows the results of the BoW-uLBP method on the same faces from the LFW dataset without any alignment pre-processing. The first row corresponds to the same method with the same codewords and parameters but on aligned versions of faces:

Table 3.12: The recognition rate of BoW-uLBP method on aligned and unaligned faces of the LFW database

Methods	Aligned	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
BoW-uLBP	Yes	32.78	50.63	58.57	60.83	60	62.5	63.33	62.5	55	53.22
BoW-uLBP	No	23.89	33.13	35	39.17	39	46.25	41.67	55	40	35.89

Next we experimented BoW method on uniform LBP features with different numbers of words (number of clusters) from 5 to 120 stepping 5, different distances between pixels along  $x$  and  $y$  direction to extract descriptor, and two gridding schemes with sizes of  $7 \times 7$  and  $8 \times 8$  in order to get better results. All training and recognition was done on the LFW dataset with images aligned and resized to  $100 \times 100$ . Unlike previous results, we have done this experiment on all possible sets of train numbers and test numbers. Figure 3.13 shows the results of experimenting with these different parameters:

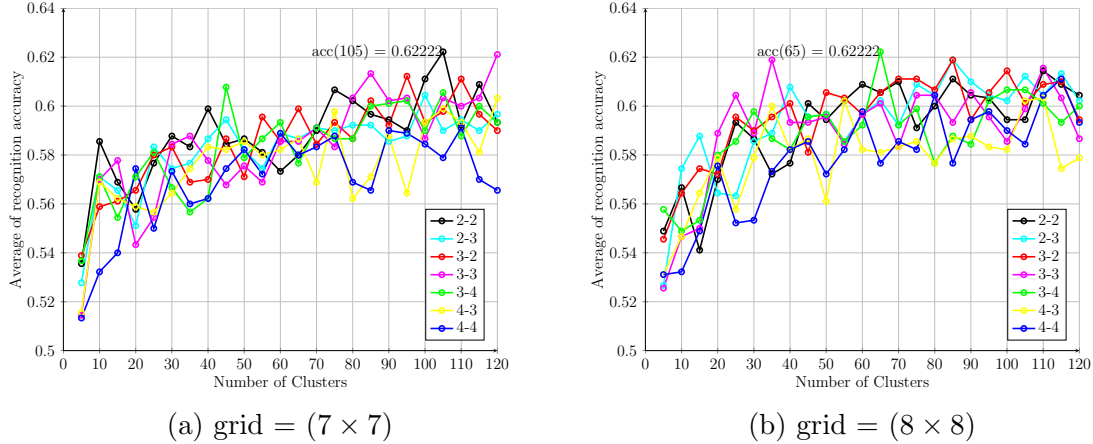


Figure 3.13: Performance evaluation results of the Bag-of-Words method over uLBP features with different number of words , gridding schemes and distances between pixels to extract descriptors

By analyzing all the results, the BoW method with number of clusters= 105,  $(x_{step}, y_{step}) = (2, 2)$ , and  $grid = (7 \times 7)$  provides the best result (62.22%). In addition to this, another configuration with 65 cluster number,  $(x_{step}, y_{step}) = (3, 4)$ , and  $grid = (8 \times 8)$  provided the similar accuracy.

Considering the fact that some processors cannot handle floating point calculations natively, we have provided the best results by making use of a 16-bit integers model as well. These results are shown in the following table:

Table 3.13: The recognition rate of the BoW-uLBP method ( $grid = (8 \times 8)$ ) with two integer and floating point numerical systems on the LFW database

Methods	numerical system	10(90)	20(80)	30(70)	40(60)	50(50)	60(40)	70(30)	80(20)	90(10)	average
BoW-uLBP	float	44.44	53.13	63.57	66.68	72.5	76.73	78.33	77.45	70.44	62.22
BoW-uLBP	integer	35.44	45.54	58.82	61.79	64.2	64.32	65.92	63.21	59.01	53.94

### 3.6.6 Identification of unknown individuals

Once descriptors are computed throughout each face patch, they are concatenated and then forwarded to a brute-force matching model to return a final decision on the person’s identity. While brute-force matching always returns an identity, it is often necessary to set a measurement for unknown faces. For this reason, a simple setup is performed. Once a feature histogram is compared with the codewords, we employ a Local-Threshold parameter to measure how close they are. By applying this threshold on each block we then compute how many regions between the matches are above the threshold. If this number be greater

than  $x\%$  of image's regions we keep the identity as a right person, if not we set it as a new person. This number of regions has been carefully set for the LFW dataset.

In this experiment we added the 50 different faces from LFW dataset as unknown individuals to test set. The results are the average of right recognition based on the recognizing true identity and unknown ones. We experimented with different values of Local-Threshold parameters (5, 10, 11,  $\dots$ , 15, 20), and regions number in the best configuration in gridding schemes of  $7 \times 7$  in order to get better results. All training and recognition was done on the LFW dataset with images aligned and resized to  $100 \times 100$ .

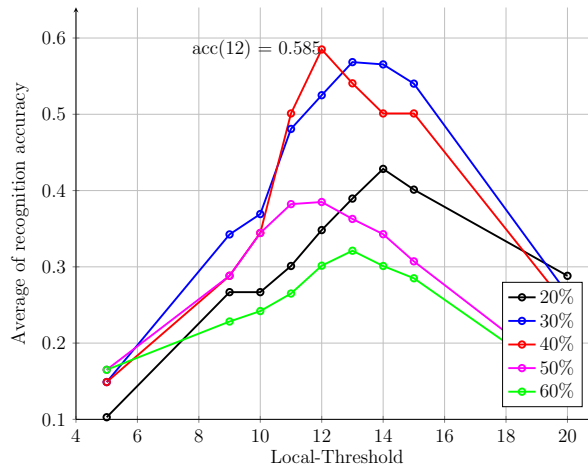


Figure 3.14: Performance evaluation results of the Bag-of-Words method with 50 unknown faces with different threshold and number of regions

By analyzing all the results, the BoW method with Local-Threshold= 12, number of clusters= 115,  $(x_{step}, y_{step}) = (2, 2)$ , matching 40% of regions in  $grid = (7 \times 7)$  provides the best result (57.24%).

### 3.7 Conclusion

In this chapter, different approaches for describing face images were described and implemented. Their performances were empirically tested on two databases: FERET and a restricted version of LFW. Among the described methods, we came up with the BoW framework based on uniform LBP features. For this purpose, we conducted an extensive parameter tuning experiment. The corresponding optimal parameters were provided in the results section.

Overall, we found that employing the Bag-of-Words method for face recognition leads to a significantly better performance when compared to the other tested methods when



used in realistic situations. Furthermore, as the local binary pattern method can be used in face detection algorithms, designing a face recognition system based on this type of feature is beneficial in terms of processing operations and speed. Furthermore, we used the “Local-Threshold” parameter in cases where the detected face is not in our database.

# Chapter 4

## Age and Gender Recognition

Age and gender recognition constitutes an important component for many computer vision applications such as human-robot interaction, visual surveillance and passive demographic data collections. More recently, the advertising industry's growing interest in launching demographic-specific marketing and targeted advertisements in public places has attracted the attention of researchers in the field of computer vision and has focused them on the problem of age and gender recognition.

The main structure of these applications can be explained as follows: when a frame is captured, a face detection technique is employed to detect the face image. After detecting and aligning the face, the information allowing for facial discrimination is extracted and these data are then used to recognize the face's age and gender category. This whole procedure is shown in Figure 4.1:

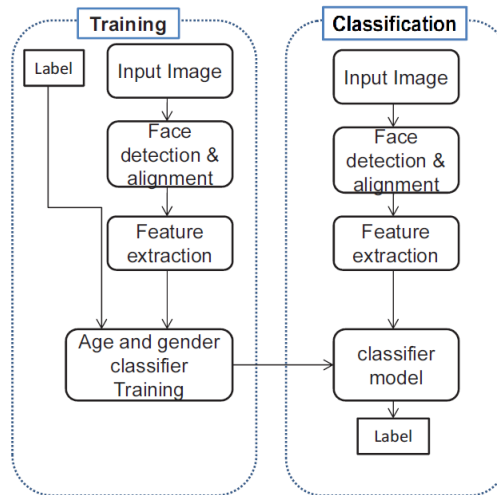


Figure 4.1: The flowchart of a gender and age recognition application

As previously mentioned, a key component in any face processing system is facial representation. While some methods choose to use raw pixels (e.g., [70], [38] and [78]) without any modification, the majority of the existing methods use local visual descriptors to produce stronger and, often, more compact representations of face images. Examples of visual information commonly used for age and/or gender recognition are features related to texture information (e.g., used in [55],[53],[54], [85], [91] and [3]), shape information (e.g., used in [88], [27] and [13]) and color information (e.g., used in [60] and [45]). These methods employ local descriptors, which are often extracted from a dense regular grid, over the entire image and then the face representation is built by concatenating these extracted descriptors into a single vector. A key issue in this framework is to determine the optimal grid parameters (e.g., spacing, size, number of grids in multi-resolution/pyramid approaches, etc.). The majority of methods that were mentioned in section 2.2 used fixed settings and performed trial-and-error heuristics to determine the right grid parameters. However, a better approach would be to use feature selection to allow the most informative image regions (or grid cells) those that can best separate face images that belong to different demographic classes (with respect to age and gender) to contribute to the facial representation. This approach further facilitates the integration of different types of descriptors and allows for more compact representations by preventing redundant features from contributing to the facial representation.

In this thesis, we suggest using feature selection to integrate different types of descriptors (color-based, shape-based, texture-based, etc.) and compact representations by preventing redundant features from contributing to the face representation. The approach demonstrated in [88] also uses feature selection but in the context of gender recognition only. They <sup>1</sup> used LBP, intensity histograms and gradient orientation features, while in this thesis LBP, SIFT and color descriptions are employed. We performed both gender recognition and age classification on two datasets: Gallagher’s and FERET.

The remainder of this chapter is organized as follows: in Section 4.1, we describe the different steps of the proposed facial representation method. Section 4.2 explains Ullman feature selection as a technique to select a set of the most discriminant features. Section 4.3 describes the learning and classification modules and section 4.4 presents the implementation details and experimental results.

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<sup>1</sup><https://codeload.github.com/uricamic/flandmark/zip/master>

## 4.1 Facial Representation

As previously mentioned, extracting the most useful facial information has been the motivation behind most of the research in the field of face processing. Gender and age classifications are among the most important applications of this field, which try to extract information regarding the demographic category of the image of a face. The vast majority of the existing solutions focus on a single visual descriptor which often encodes only a certain characteristic of the image regions (e.g., shape, texture, color, etc.). Unlike these methods, which normally only use a single type of descriptor based on a fixed setting (in terms of grid parameters), in our proposed method, a face image is represented by a collection of different types of local descriptors extracted from various regions across the image. We do this because, though each type of visual descriptor only captures specific information about an image region, they can all be used to complement the information captured by another type of descriptor. For example, while the Local Binary Pattern (LBP) descriptors encode spatial relations between neighboring pixels and are useful to describe the texture of an image patch, a Scale Invariant Feature Transform (SIFT) builds local histograms of gradient orientations and is the best when it comes to capturing the shape of an image patch. Therefore, extracting both SIFT and LBP descriptors from their respective locations in the face image (e.g., cheeks for LBP descriptors to distinguish between faces with and without beards, and the nose and mouth for SIFT descriptors to distinguish between different faces based on the shape characteristics of the facial features) allows the produced face representations to take advantage of both sources of information. This will, in turn, provide better distinctiveness between faces for classification and recognition purposes.

To determine which type of visual descriptors are the most informative at specific regions of the face image, we suggest using feature selection (where a feature is defined by of type of descriptor and an image region) to choose the optimal set of features from a pool of candidate features. In the next two sub-sections, we explain how the pool of candidate features can be generated and how informative features can be selected.

### 4.1.1 Pool of Candidate Features

To generate the pool of candidate features, alignment techniques, which are based on the affine transformation determined from three facial landmarks (left eye, right eye and mouth center) must be used. For each aligned face image in the training set, an image pyramid is built and then different types of visual descriptors are extracted from dense

regular grids (with different sizes and spacing of the pixels) over the image at each level of the pyramid. This results in a large number of descriptors being extracted from various regions of the face images. In this thesis, we consider three such types of features, each encoding a certain characteristic (e.g. texture, shape and color) of an image region.

### 4.1.2 Texture Features

Among the variety of techniques that have been developed for extracting texture features from a face image, the Local Binary Pattern Histogram(LBPH) and the Gabor Wavelet technique number among the most successful ones. In this section, we will go over these methods and briefly describe each of them.

#### The Local Binary Pattern Histogram

LBPH [72] as described in 3.4, is a powerful texture-encoding descriptor based on the occurrence statistics of a set of local binary patterns. These uniform patterns help keep it robust against the rotation and extract the more meaningful textures of the target image. A uniform pattern is a Local Binary Pattern (LBP) with at most, two bitwise transitions (or discontinuities) in the circular presentation of the pattern. When using a  $3 \times 3$  neighborhood, for example, only 58 of the 256 total patterns are uniform. In a 59-dimensional image representation (i.e., a histogram), there is one dimension for each uniform pattern and one dimension for the entirety of the non-uniform patterns. The whole procedure of applying LBPH has been explained in section 3.3.1

#### Gabor Texture Descriptors

The bio-inspired Gabor filter method, proposed by Gabor in 1946[33], is a texture descriptor that is mainly inspired from the structure of the human retina. When observing the cell layers in the retina, one can see that different types of cells exist. Hubel and Wiesel[44] categorized the receptive fields of cells in the visual cortex into three categories: simple cells, complex cells and hyper complex cells. Of these, a simple cell is defined as a cell that responds primarily to oriented edges and gratings (bars of particular orientations). The two-dimensional Gabor function models these types of cells based on their spatial summation properties.

As this filter extracts the frequency and orientation characteristics of a region, it is well suited for the texture analysis of images. In the spatial domain, a 2D-Gabor filter is

defined as a Gaussian kernel function modulated by a sinusoidal plane wave as follows:

$$G_{\vec{k}}(\vec{x}) = \frac{\|\vec{k}\|}{\sigma^2} \cdot e^{-\frac{\|\vec{k}\|^2 \cdot \|\vec{x}\|^2}{2\sigma^2}} \cdot \left[ e^{i\vec{k} \cdot \vec{x}} - e^{-\frac{\sigma^2}{2}} \right] \quad (4.1)$$

$$\vec{k} = k_s e^{i\phi} \qquad k_s = \frac{\pi}{2^{s+1}}$$

where "s" corresponds to the scale of the Gaussian envelop, which takes on the values of 0, 1, ..., 4 and "φ" controls its orientation and takes on the values of 0, 1, ..., 7. By using 5 scales and 8 orientations, a total of 40 Gabor filters are computed. Figure 4.2 represents the section of the real part of the 40 Gabor filters.



Figure 4.2: Representation of the real part of 40 Gabor filters

Since computing Gabor coefficients for all pixels leaves a huge amount of information requiring processing, statistical techniques such as PCA are commonly used to reduce the amount of dimensions in which feature data is found.

### 4.1.3 Shape Features

Since human perception systems can provide a good approximation of age and gender just by considering the shape of the face and its overall structure, descriptors which characterize the shape information of image regions have received considerable attention. Of a variety of descriptors commonly used for this purpose, we can mention different edge operators and the Scale-Invariant Feature Transform (SIFT) as the most performant ones. Note that SIFT can also be categorized as a textural descriptor. The high discriminative power of SIFT descriptors acts as competition against different edge operators, which simply extract gradient orientation features and are not robust against the scale and rotation variations. Thus, to recognize age and gender, we employ SIFT descriptors. The results of this descriptor are found in section 4.4.

#### Scale-Invariant Feature Transform (SIFT)

As previously mentioned in section 3.3.2, SIFT [63] is a powerful description method for characterizing image regions that has been widely used for various computer vision applications. SIFT produces a 128 dimensional representation for each image region using a 3D (2 locations and 1 orientation) histogram of gradient locations and orientations. The contribution of each pixel to the location and orientation bins is weighted by its gradient magnitude. The quantization of gradient locations and orientations makes SIFT descriptors robust to small geometric distortions and certain illumination variations.

### 4.1.4 Color Features

Modeling color distribution can be very useful in characterizing an image region. For this purpose, different types of color descriptors are used to describe image regions and embed color information into an object recognition framework. In this section, two popular techniques to fulfill this purpose - the color histogram and Color CENTRIST - are analyzed and employed in the practice of age and gender recognition. A third color descriptor based on the Local Binary Pattern framework (CLR-LBP) is also proposed and, through extensive experiments, it is shown that our descriptor achieves results comparable with the two other color descriptors.

## Color Histogram

This type of descriptor models color distribution by constructing a histogram with 4 bins per color channel, in the RGB color space[45]. More specifically, the intensity values in each color channel (i.e., red, green and blue) are mapped into 4 values (intensity values between 0 and 63 are mapped to 0, and so on). Then, each of the 64 ( $4^3$ ) bins stores an integer that count the number of times the corresponding color triplet occurred. A histogram is then computed using the corresponding quantized samples per pixel for each region. Since each channel is mapped into 4 values, the histogram is specified by 64 bins. The entire procedure that this descriptor undergoes is presented in the Figure 4.3.

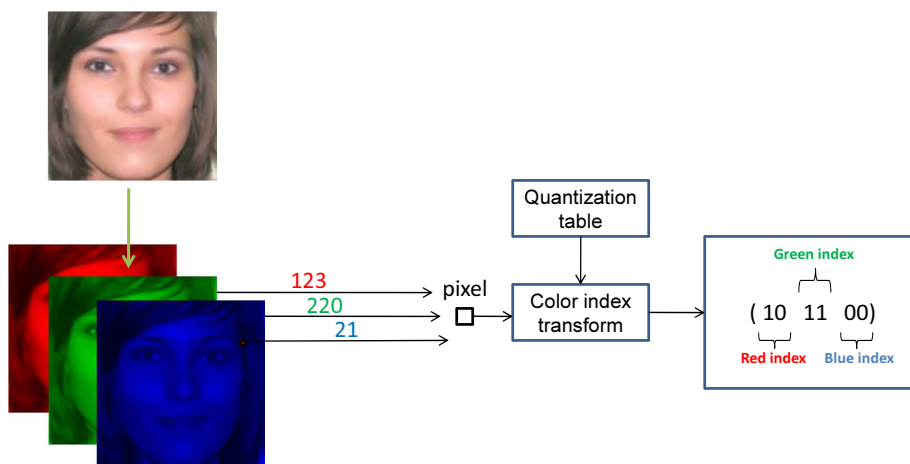


Figure 4.3: Color Histogram descriptor

## Color CENTRIST

Chu et al. [20] developed a new descriptor to categorize image scenes: Color CENTRIST. This descriptor, based on the CENSUS TRANSFORM HISTOGRAM (CENTRIST)[97] framework, employs both intensity gradients values and color variations among image pixels. The goal of the CENTRIST framework is to compensate for two existing issues prevalent in histogram-based descriptors: disappearing spatial information from the histograms during the computation process and a lack of multilevel representation. To tackle these problems. Chu et al. proposed a spatial pyramid scheme, which scales images to different levels. In the  $k$  level, an image is divided into regions with a size of  $\frac{N}{2^k} \times \frac{N}{2^k}$ . Next, they split the image's width and height into  $2^k$  parts and all resultant regions plus the ones centered at the common corners of four neighboring regions are extracted. By this scheme for image level  $k$  we have  $2^{2k+1} - 2^{k+1} + 1$  number of regions.



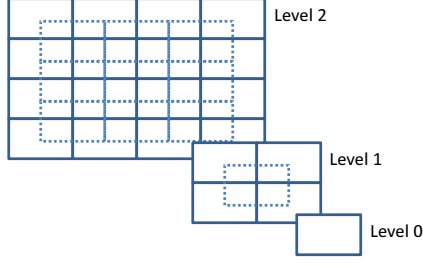


Figure 4.4: Illustration of levels 2, 1, and 0 split of an image

The Color CENTRIST scheme is then applied on all pixels and the histogram corresponding to each image's region is extracted. In this approach, each pixel is represented by 8 bits, computed from the color channel (e.g. RGB or HSV). For example, by allocating  $b_1$ ,  $b_2$  and  $b_3$  bits for the Hue, Saturation, and Value components of the HSV channel (with  $b_1 + b_2 + b_3 = 8$ ), the HSV channels will be quantized into  $2^{b_1}$ ,  $2^{b_2}$  and  $2^{b_3}$  levels. Therefore, for a pixel with HSV value of  $p = (h_p, s_p, v_p)$ , the corresponding color index is equivalent to:

$$p_i = \lfloor \frac{h_p \times 2^{b_1}}{256} \rfloor + \lfloor \frac{s_p \times 2^{b_2}}{256} \rfloor 2^{b_1} + \lfloor \frac{v_p \times 2^{b_3}}{256} \rfloor 2^{b_1+b_2}$$

After representing the images' pixels with a color index, a census transform, similar to that shown in the LBP model, is applied on  $3 \times 3$  blocks around each pixel's value. The color index of each pixel is compared with other ones and, if the center pixel's value is greater than the neighbor's value, we set the neighbor's value as "1". Otherwise, it is set to "0". As we have 8 neighbors in a  $3 \times 3$  block, by following the pixels row by row, we will have an 8-bit binary number. This number will then be converted to a decimal numerical system to obtain a new number between 0 and 255, namely the color Census Transform value (cCT value). The histogram of the cCT values is then extracted for each region, which results in a 256 dimensional descriptor. Finally, their dimensions are reduced using the PCA technique, and by employing the spatial pyramid, the global structure of the image is constructed.

### Color-based Local Binary Pattern (CLR-LBP)

Here, a new color descriptor has been proposed to embed color information based on the Local Binary Pattern (LBP) framework. The focal idea of this descriptor lies in demonstrating the relations between color intensities of each pixel in the  $3 \times 3$  block around it.

First of all, the image is represented in red-blue-green (RGB) color space. The differ-

ences between the green value of the middle pixel and the blue and red values of neighbors' pixels are then compared. If the differences between the green and blue channels is greater than or equal to other green and red ones, we set the neighbor's value as "1". Otherwise, it is set to "0". Similar to LBP, we then follow the pixels along a circle, (be it clockwise or counter-clockwise) to obtain an 8-digit binary number. Afterwards, for comparison purposes, this number (which ranges between 0 and 256) is mapped to 64 bins, all of which fall between 0 and 63 (Figure 4.5). The image is then divided into a number of regions, and the values of the 64-bins histogram of CLR-LBP are extracted from each of said regions. Finally, histograms of all regions are concatenated to build the feature vector for the face image.

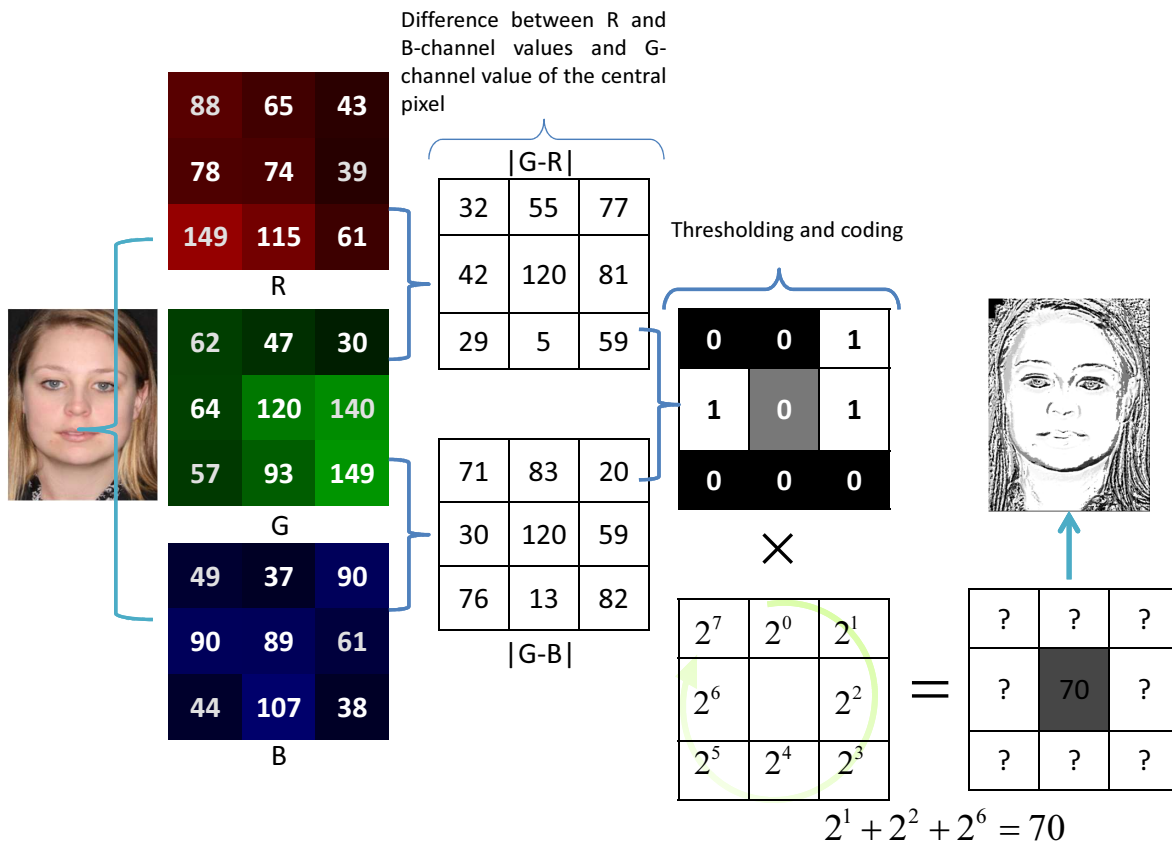


Figure 4.5: The CLR-LBP descriptor

Through an extensive experimental study, this framework will be applied on RGB and HSV channels (all channels are normalized ranging between 0 and 255) while using a different middle channel to serve both gender and age classification purposes.

## 4.2 Feature Selection

Once all candidate features have been extracted from a set of images, feature selection is required to choose the most informative features amongst them. For this purpose, the feature selection technique, proposed by Ullman [94], has been employed in this thesis. This approach tries to select the subset of relevant features by employing two sets of positive and negative data. The procedure relevant to choosing features take into account the fact that the best set of features comprises features which keep positive sets of data close together and separate negative sets as far from their average. Although this approach can easily be extended to the case of multiple classes, the feature selection based on these two sets make it more appropriate for a binary classification.

For each candidate feature,  $X_n$ , a response vector,  $r_n$ , is generated by computing the similarity between different pairs of training faces, using only the descriptor extracted based on the specifications of the candidate feature, namely the location and the size of a region, and a type of descriptor (e.g., LBP, SIFT, or CH) .

Then, an initial binary variable,  $f_n$ , is associated to each  $X_n$  by mapping its response vector  $r_n$  to 0 (if the corresponding element of the response vector is lower than the threshold  $\theta_n$ ) and 1 (if that response is greater than  $\theta_n$ ). The threshold  $\theta_n$ , which presents the minimal similarity between features, is determined in such a way that the mutual information between the resulting binary variable  $f_n$  and the class variable  $C$  is maximum:

$$\theta_i = \arg \max_{\theta} I(X_i(\theta); C) = \arg \max_{\theta} (H(C) - H(C|X_i(\theta))) \quad (4.2)$$

where  $H(x)$  and  $H(x|y)$  correspond to Shannon's entropy and conditional entropy.

Given a collection of binary variables, feature selection then attempts to select the most appropriate features that can, together, best separate the positive training pairs (i.e., pairs with both face images belonging to the same age or gender class) from the negative training pairs (i.e., pairs with both face images belonging to different age or gender class). To this end, a binary variable  $C$  is generated in order to represent the ground-truth classification, where  $C(I) = 1$  if the pair  $I$  is positive and is 0 if otherwise.

The discriminative value of each feature is measured by the amount of mutual information it can deliver about the class:

$$I(f_n; C) = H(C) - H(C|f_n) \quad (4.3)$$

In the above equation,  $I(f_n; C)$  is the mutual information between the binary variable  $f_n$

and classes  $C$  and  $H$  denote entropy. Feature selection begins by identifying the feature whose binary variable generates the highest mutual information score. It then proceeds by iteratively searching for the next informative feature,  $f_r$ , that delivers the maximal amount of additional information with respect to each of the previously selected features:

$$f_r = \arg \max_{f_k \in K_r} \min_{f_j \in S_r} (I(f_k, f_j; C) - I(f_j; C)) \quad (4.4)$$

Here  $K_r$  and  $S_r$  are the set of features not yet selected, and the set of features already selected at iteration  $r$ , respectively.

The feature selection process ends when the increment in mutual information gained by selecting a new feature is less than a certain threshold or until the number of selected features reaches a certain limit. It worth mentioning that selecting more features doesn't necessarily increase the performance of the classification process and can even contribute to a greater degree of mis-classification. Therefore, the number of features should be tuned to let those features with a large contribution go through the classification model and without those having a low discriminative power.

Figures 4.6, 4.7, and 4.8 show the results of applying feature selection on texture and shape features extracted with the purpose of discriminating age and gender classes. Red squares in Figure 4.6 show the regions of interest (ROI's) which the corresponding descriptors have been selected as the most discriminative features for determining gender. Similarly, Green squares in Figure 4.7 and Figure 4.8 represent those ROIs which have been selected for age classification.

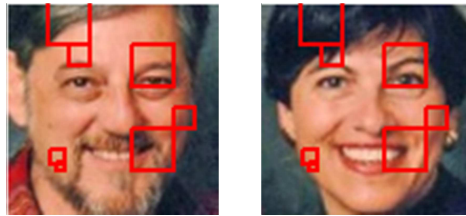


Figure 4.6: The first seven texture features selected by Ullman feature selection technique to classify gender subjects

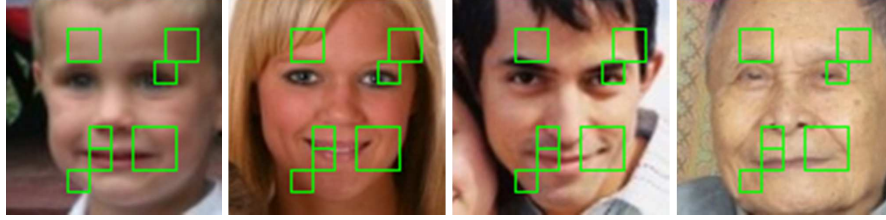


Figure 4.7: The first seven texture features selected by Ullman feature selection technique to classify age subjects

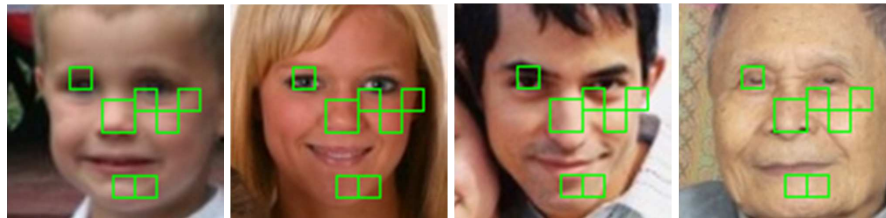


Figure 4.8: The first seven shape features selected by Ullman feature selection technique to classify age subjects

## 4.3 Classification

As explained beforehand, the feature selection process provides us with a set of features that each represent a certain region in the face image and specify a particular descriptor type to be extracted from that region. By concatenating all of regions' descriptors together, a global representation of the face image is produced. A learning method must then be applied to perform the task of classification. This learning method aims to construct a classifier based on extracted descriptors of the training set. Among the existing methods, the Support Vector Machine (SVM) is one of the most popular as it performs extremely well and has an efficient open source implementation[16].

### 4.3.1 Support vector machine (SVM)

The Support Vector Machine(SVM) proposed by Boser et. al[10] is one of the commonly chosen learning techniques in supervised classification processes. The training data set and its label set is fed into the classifier. The SVM classifier then finds an optimal decision boundary to separate the data based on its corresponding labels.

The basic form of the SVM[92] is proposed for two class problems and aims at finding the optimal hyperline with the widest margin possible to better separate classes. This

margin corresponds to the distance between the hyperline and classes' support vectors.

An example would be of Figure 4.9, which presents the two classes' data in  $R^2$ . As it is evident, these data can be separated linearly by a hyperplane with the form of  $\omega \cdot x - b = 0$ , where  $\frac{b}{\|\omega\|}$  indicates the hyperplane's offset.

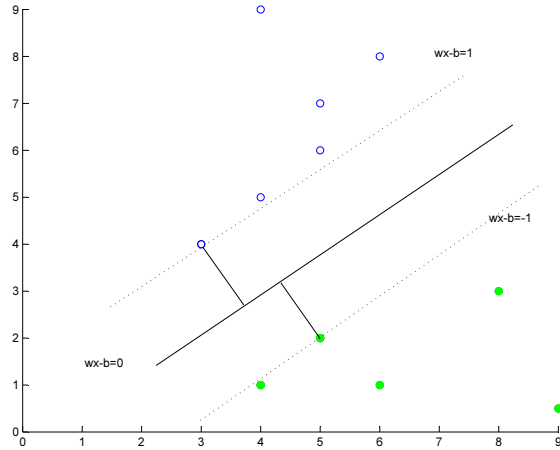


Figure 4.9: Support vector Machine schema

The hyperplanes corresponding the borders of these two classes can be formulated as  $\omega \cdot x - b = 1$  and  $\omega \cdot x - b = -1$ , where the distances between them ("the margin") is equivalent to  $\frac{2}{\|\omega\|}$ . To generalize these hyperplanes so that all classes' points fall into them we can write them in the following form:

$$\begin{cases} \omega \cdot x - b \geq 1 & \forall x_i \in C_1 \\ \omega \cdot x - b \leq -1 & \forall x_i \in C_2 \end{cases} = y_i(\omega \cdot x - b) \geq 1 \forall x_i \quad (4.5)$$

Since we aim to maximize the margin space we can write:

$$\begin{cases} \langle \omega, x_1 \rangle - b \geq 1 \\ \langle \omega, x_2 \rangle - b \leq -1 \end{cases} \Rightarrow \langle \omega, (x_1 - x_2) \rangle = 2 \Rightarrow \langle \frac{\omega}{\|\omega\|}, (x_1 - x_2) \rangle = \frac{2}{\|\omega\|} \quad (4.6)$$

Since the SVM also aims to maximize the margin between these two classes ( $\frac{2}{\|\omega\|}$ ), the term  $\|\omega\|$  should be minimized. What's more, the potential errors that can emerge when mapping classes' data to the hyperplane should be minimized. This means that the problem

of finding the hyperplane can be expressed in the Lagrange multiplier term as follows:

$$\min_{(\omega, b)} \max_{\alpha_i \geq 0} \frac{1}{2} \|\omega\|^2 - \sum_{i=1}^n \alpha_i (y_i (\omega \cdot x_i - b) - 1) \quad (4.7)$$

where parameter  $\alpha$  is the Lagrange multiplier parameter. The solution to this quadratic equation is found as follows [51]:

$$\omega = \sum_{i=1}^n \alpha_i x_i y_i \quad (4.8)$$

where  $x_i$  values that correspond to non-zero values of  $\alpha_i$ , represents the support vectors on the margins (on the lines  $y_i (\omega \cdot x_i - b) = 1$ )

From the arguments seen above, it follows that the basic SVM cannot be applied for non-linearly separable and multi-class cases. Thus, in order to generalize this framework, the Kernel SVM has been proposed. The Kernel SVM tackles this problem by mapping the training data to a feature space of high dimension and then constructs a linear decision model to separate the data classes. This highly-dimensional space is characterized by the inner product between data and is selected in such a way that the data in this space can be separated linearly.

As such, the Representer theorem [50] suggests that, instead of optimizing the  $\omega$  value in high-dimensional space, a set of Kuhn-Tucker coefficients ( $\alpha$ ) can be optimized as follows:

$$\omega = \sum_{i=1}^n \alpha_i \Phi(x_i) \quad (4.9)$$

Thus, the formula to calculate a hyperplane (the decision rule) can now be written as follows:

$$F(x) = \sum_{i=1}^n \alpha_i \Phi(x_i) \cdot \Phi(x) + b \quad (4.10)$$

And the similarity kernel can be expressed as follows:

$$K(x_i, x) = \Phi(x_i) \cdot \Phi(x) \quad (4.11)$$

which formulates our decision rule by:

$$F(x) = \sum_{i=1}^n \alpha_i K(x_i, x) + b \quad (4.12)$$

So the equation (4.7) is expressed as follows:

$$\min_{\alpha} \left\{ \frac{1}{2} \sum_{i,j} \alpha_i \alpha_j \Phi(x_i) \cdot \Phi(x_j) - \sum_i y_i \alpha_i \right\} \quad (4.13)$$

where  $\sum_i \alpha_i = 0$ . Similar the basic SVM, the set of non-zero  $\alpha_i$ s in  $\sum_{i=1}^n \alpha_i y_i = 0$  are called Support Vectors(SV).

To make an appropriate nonlinear feature map, which maps data to a high-dimensional space within which data are best separated, different kernels have been proposed. The polynomial decision surface and Gaussian Radial Basis function (RBF) are among the most popular kernels currently being used to achieve this purpose:

$$\begin{aligned} K_{poly}(x, y) &= (x \cdot y + 1)^d \\ K_{RBF}(x, y) &= \beta e^{-\gamma \|x-y\|^2} \end{aligned} \quad (4.14)$$

It worth mentioning that the parameters regarding each kernels should be tuned for each classification process.

## 4.4 Experimental Results

This section provides the results of the methods described earlier on two bench mark databases. All codes are implemented in C++ using the two most popular libraries: OpenCV 2.4.5 library (used as an open source library specialized for computer vision applications), and LIBSVM (used as a library for Support Vector Machines)[16].

### 4.4.1 Dataset

The number of databases can be used for the purpose of age and gender recognition are limited due to their number of images and the age and gender range distribution. In general, collecting a face database which can fit to different face processing problem is not easy due to the multiple aspects regarding the subject that should be considered. Regarding the fact that the faces can be collected automatically or manually, different issues are being faced. In automatic approaches, which a set of available images are being used in constructing the database, detecting face images and labeling them is not an easy task to do. As an example, providing some meta information or informative tags such as age, gender, spectacles, smile, etc involves a manual and precise tagging system. Moreover,



data privacy policies for these images are sensitive subjects and it becomes a bigger issue for companies who want to use them in their products. On the other hand, creating a database manually requires a set of setups and configurations, which for some applications like investigation of aging affect can be quite expensive. Here, the performance of the different descriptors explained before has been evaluated with two standard benchmark databases for age and gender recognition: the Facial Recognition Technology (FERET) database (as was described in section 3.6.1) and the Gallagher Collection Person Dataset (GROUPS).

### **The Facial Recognition Technology (FERET) database**

The Color FERET is a commonly used database in the field of face processing, as it provides information concerning, the age, the ethnicity, and gender of its faces. As previously mentioned, this database contains faces in different poses, expressions and lightening conditions. In this section the techniques described are tested on the protocol proposed by [6] over 1,689 frontal face images of 969 male subjects and 720 female subject (their age and gender information were provided) taken from Fa and Fb probes. 845 face images(360 female and 485 male) were used for training purposes and 844 face test images (484 males and 360 female) were used to put our methods through classifier tests to ensure their validity.

### **The Gallagher Collection Person Dataset (GROUPS)**

The Gallagher’s database[34], which is publicly available, is composed of 28,231 faces collected from Flickr images taken under unconstrained conditions. Images were gathered based on the search for four subjects: wedding, bride, groom and portrait. 86 percent of database’s faces were detected using a face detection algorithm and other faces were added manually. Furthermore, they have been manually labeled with the corresponding gender and age where the age labels assigned to one of seven categories: 0-2, 3-7, 8-12, 13-19, 20-36, 37-65, and 66+. The faces are labeled based on their gender and their association to one of seven age groups (covering from 0 to +75 years). As there was no common and defined protocol for the experiments on this dataset, Dago-Casas et al. [3], suggested a folding protocol using 14,760 of the higher resolution faces and distributed them into five folds, with an equal number of males and females in each fold. To obtain this result, they[24] employed a face detection technique as well as an alignment method and removed the low resolution faces. Then, they randomly removed some of the male faces so as to

have an equal number of male and female faces in each fold. Finally, they came up with a framework within which each fold contains the images of 2952 people under various changes of illumination, camera poses and image quality. It bears mentioning that Dago-Casas et al. [24] obtained a gender classification accuracy of 86.61% by using Gabor jets (described in 4.1.2) on this framework. Gallagher and Chen[35] had previously reported 42.9% and 74.1% accuracy for age and gender classification by using a combination of appearance and context information. Similarly, Shan[81] had reached 50.3% and 75.7% for age and gender classification by boosted Gabor features on this database without a common framework. However, only Dago-Casas et al. obtained such a high level of accuracy, which was caused by their protocols and better feature types. It worth mentioning that the age classification results reported for this dataset are not obtained in a common framework and, therefore we are not able to make fair comparisons.

The age and gender distribution of the whole database and the proposed framework by Dago-Casas et al. [24] has been shown in the Table 4.1.

Table 4.1: Gender and age distribution in Groups dataset

Gender and age groups	Original Gallagher’s dataset	Dago-Casas et al.’s framework [3]
Male	13672	7380
Female	14559	7380
(0-2)	954	534
(3-7)	1595	906
(8-12)	872	417
(13-19)	1692	899
(20-36)	15048	7921
(37-65)	6817	3463
(66+)	1253	620

## 4.4.2 Results

In this experiment, results concerning gender and age recognition have been gathered based on three different types of descriptors. In the Gallagher dataset, the results are averaged over five folds of each method for both gender and age recognition rates in percentages (i.e. the rate of correct decisions to the number of overall decisions, which can be interpreted as the Rank 1 identification rate). Each fold contains the images of 2952 people under various changes of illumination, camera poses and image qualities. In addition to this, these methods are tested on 1200 face images in the FERET dataset and consist of images taken under a variety of lightings and illustrating various expressions. Texture, shape and color features were extracted for every image in each dataset and then concatenated into a single feature vector. The 200 most informative feature bins amongst all resulting vectors were selected in the Gallagher dataset. These selected features later were applied for face representation on both Gallagher and FERET datasets. Furthermore, it was found that applying an SVM with a RBF kernel to the database representing the selected feature vectors begets outperformances of all other strategies [24] in terms of accuracy. The results of Gabor Jets, raw pixel values and LBP combined with PCA are provided in last three rows of table 4.2.

In each rows of Tables 4.2 and 4.3, CLR-LBP(XYZ) refers to the differences between the  $Y$  value of the center of each patch and its neighboring  $X$  and  $Z$  values such that if  $|Y - X|$  is greater than or equal to  $|Y - Z|$ , we set the neighbor's value as "1". Otherwise, it is set to "0".

Table 4.2 shows comparative results of gender recognition when results obtained with different methods on FERET and Gallagher's datasets. In all experiment the most 200 informative feature bins have been selected.

Table 4.2: Comparative results of the gender recognition systems on the FERET and Gallagher’s datasets.

Method	gender recognition	
	Gallagher	FERET
LBP	90.43	100
CH	82.82	76.45
Color CENTRIST	87.74	96.90
CLR-LBP(RGB)	87.95	96.90
CLR-LBP(GBR)	62.17	96.90
CLR-LBP(BRG)	61.60	51.45
CLR-LBP(HSV)	52.64	57.85
CLR-LBP(SVH)	51.65	60.12
CLR-LBP(VHS)	52.66	92.98
SIFT	89.61	100
LBP+CH+SIFT	91.59	100
LBP+CLR-LBP(RGB)+SIFT	<b>91.94</b>	<b>100</b>
Pixels+PCA	80.11[24]	96.62[70]
Gabor Jets+PCA	86.61[24]	98 [56]
LBP <sub>s</sub> +PCA	86.69[24]	95.8[57]
Appearance+context	74.1[35]	N/A
boosted Gabor	75.7[81]	85[64]

To experiment with the methods for age classification described, we divided the Gallagher’s dataset into three age groups, having three, five and seven age categories, respectively. Similarly, we divided the FERET database into four age categories. Table 4.3 shows comparative age recognition results for these age categories with different methods tested on Gallagher’s dataset. In all experiment the most 200 informative feature bins have been selected.

Table 4.3: Comparative results of the age recognition systems on the FERET and Gallagher’s datasets.

Method	age recognition accuracy			
	Gallagher			FERET
	3 groups	5 groups	7 groups	
LBP	75.15	60.25	54.65	99.94
CH	57.72	43.06	40.77	52.16
Color CENTRIST	59.82	41.73	35.34	95.05
CLR-LBP(RGB)	68.46	53.61	49.15	95.07
CLR-LBP(GBR)	45.46	24.14	21.06	47.56
CLR-LBP(BRG)	40.44	25.68	17.42	30.19
CLR-LBP(HSV)	40.69	25.19	20.10	51.67
CLR-LBP(SVH)	40.75	24.61	15.83	28.14
CLR-LBP(VHS)	38.65	24.48	17.83	94.08
SIFT	74.08	58.34	53.14	100
LBP+CH+SIFT	79.87	62.02	56.75	100
LBP+CLR-LBP(RGB)+SIFT	<b>80.04</b>	<b>62.69</b>	<b>57.63</b>	<b>100</b>

As shown above, the CLR-LBP based on the RGB color space (with the green-channel as being the center from which other channels’ distances are computed) out-performed other color descriptors in terms of its recognition rate. In addition to this, in Table 4.2, the gender recognition rate reached 91.94% by using 130 LBP, 55 SIFT and 15 CLR-LBP bins. Similarly, in Table 4.3, the age recognition rate succeeded 80.04% for three age categories when the number of features that were selected for age recognition on Gallagher’s dataset was at 110, 60, and 30 for the uniform LBP, SIFT and CH respectively. Consequently, the combination of the uniform LBP with SIFT and Color Histogram methods shows the superiority of texture over shape and color information. Adding shape and color information to the texture descriptor improves the level of gender recognition rate by 1.51% and the level of age recognition by 4.89% with respect to pure LBP on three age categories.

Tables 4.4, 4.5, and 4.6 present the confusion matrices for three, five and seven age classes on Gallagher’s database based on our proposed method to achieve optimal results illustrated in Table 4.3. As expected, most of the confusion occurs between adjacent

classes. For instance, it is clear from the last rows of Tables 4.6 that mature adults are often misclassified as young adult or senior classes, which is a commonly made mistake.

Table 4.4: Confusion matrix for three age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized).

Prediction \ Actual	(0-2)	(3-7)	(8-12)	(13-19)	(20-36)	(37-65)	(66+)
(0-2)	<b>87.5752</b>	9.8138	1.4749	0	0.3739	0.1887	0.5735
(3-7)	18.9652	<b>50.350</b>	22.8436	4.2735	1.5571	0.4082	1.6024
(8-12)	2.3331	25.4017	<b>49.5909</b>	11.4253	6.4858	3.3447	1.4184
(13-19)	0.6856	5.6479	15.8349	<b>43.5546</b>	25.0426	6.5393	2.6952
(20-36)	0.6289	2.0510	4.6446	22.7848	<b>44.9055</b>	19.9257	5.0595
(37-65)	0.5169	1.2761	2.3047	7.9813	21.1957	<b>42.1779</b>	24.5473
(66+)	0.4803	0.1575	0.6661	1.1222	2.6093	9.7136	<b>85.2511</b>

Table 4.5: Confusion matrix for five age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized).

Prediction \ Actual	(0-12)	(13-19)	(20-36)	(37-65)	(66+)
(0-12)	<b>84.5187</b>	10.4980	2.5590	1.4549	0.9694
(13-19)	13.1562	<b>54.4231</b>	23.8387	6.8705	1.7116
(20-36)	3.5302	25.8553	<b>46.4744</b>	19.6832	4.4569
(37-65)	1.8250	9.5284	21.0849	<b>44.3041</b>	23.2575
(66+)	0.5023	1.5804	2.1552	10.4260	<b>85.3361</b>

Table 4.6: Confusion matrix for seven age classes employing feature selection on a set of LBP, CLR-LBP(RGB) and SIFT (numbers are normalized).

Prediction \ Actual	(0-19)	(20-65)	(66+)
(0-19)	<b>77.5159</b>	20.1424	2.3416
(20-65)	15.2422	<b>73.0572</b>	16.0605
(66+)	1.6039	8.8490	<b>89.5470</b>

In addition to the previous tests, we performed another experiment to demonstrate that increasing the number of features would not necessarily increase recognition rate. This experiment has been conducted on a set of features extracted by LBP for gender recognition on Gallagher’s dataset. Result of this experiment is shown in Figure 4.10.

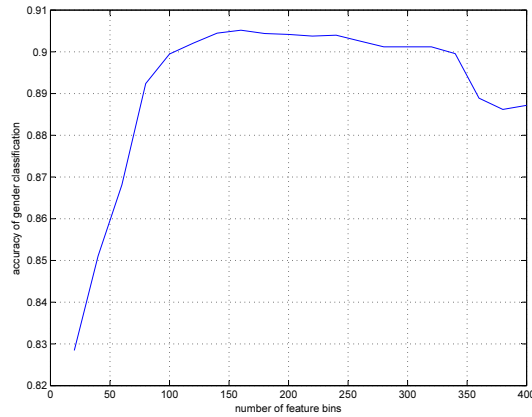


Figure 4.10: Effect of the number of features selected

## 4.5 Conclusion

In this chapter, a novel gender and age classification method was reported. Unlike the vast majority of the existing solutions that focus on a single visual descriptor (and, therefore, limit the face representations by encoding only a certain characteristic of the image regions such as shape, texture or color), this new method facilitates the integration of multiple feature types. This allows for the taking advantage of various sources of visual information. The proposed framework, based on the selection of informative features, only allows the regions that can best separate face images of different demographic classes (with respect to age and gender) to contribute to the face representations. This, in turn, improves classification and recognition accuracies. In addition to this, a new color descriptor (CLR-LBP) was proposed inspired by the local binary pattern schemes that was found to obtain results comparable with those of other existing color descriptors in object recognition. A set of experiments conducted on the challenging Gallagher’s and FERET database validated the effectiveness of the proposed solution with regards to accurately classifying the age and gender of face images taken under unconstrained conditions.

# Chapter 5

## Conclusion

In this thesis, we investigated two problems of the face processing field, face recognition, and age and gender classification. We reviewed recent developments in these two fields and our survey demonstrated that many of the existing methods suffer from difficulties in analyzing data collected from uncontrolled environments. These difficulties stem from the fact that, in face, gender and age recognition problems, proposing a model that allows for an accurate recognition that can be generalized so as to apply to everyone is not an easy task.

The first part of our research proposes a model for face recognition that employs features extracted from sample images of uncontrolled environments to represent a face image. We investigated different approaches such as dimension reduction techniques, edge detection operators and texture and shape feature extractors to represent the face image. Afterwards, these methods were evaluated on two popular databases: the FERET database and the collected version of LFW. After evaluating these aforementioned methods on the FERET database and the collected version of LFW, we were inspired to use the bag-of-words method basing it on the uniform LBP features. Furthermore, we used the "Local-Threshold" parameter in cases where the detected face is not in our database. Experiments on a challenging dataset showed that our approach achieved a better accuracy in comparison with the other popular methods such as the PCA, LDA, LBPH, SIFT, BRIEF and FREAK methods. To tune the parameters, we conducted an extensive experiment for which the results are provided in Section 3.6.

In the other part of our research, we presented a novel age and gender classification method. The vast majority of the existing methods focus on a single visual descriptor, which limits the face representations by encoding only a certain characteristic of the image



regions such as shape, texture or color. In contrast to this, our system facilitates the integration of multiple feature types and allows us to take advantage of various sources of visual information. By integrating the proposed age and gender classifier with a reliable tracker and, possibly, a face quality assessment measure (e.g. [[31]]), a real-time demographics visual system can be built.

Additionally, a new color descriptor (CLR-LBP) was proposed, inspired by the local binary pattern schemes [73], and was found to produce results comparable with those of other existing color descriptors in object recognition. A set of experiments conducted on the FERET [75] and Gallagher’s [35] database validated the effectiveness of our proposed solution by accurately classifying the age and gender of examined subjects. Experiments on Gallagher’s dataset, which contains images captured under various levels of changes of illumination, camera poses and quality showed that we are able to achieve a 80.04% and 91.94% accuracy in age and gender classification - respectively - by employing different visual features extracted from a face image.

## 5.1 Future Work

In light of the good results obtained by applying the feature selection method on age and gender recognition problems, it follows that similar efforts can be employed to improve face recognition problem. Thus, instead of using a single visual descriptor, a possible solution would be to apply feature selection scheme on different regions of the face image. The features that would be selected would be those that offer the most distinctive information. This would allow us to integrate different visual feature types to represent each region of face images.

Another limitation of the face, age and gender recognition systems is that they are all sensitive to pose changes. Therefore, applying pose estimation to the detected faces would give us a good sense of how each face elements corresponds to the overall face positioning. These information can help us to better represent the face image as a whole.

Another potential future direction is to explore the possibility of using a multi-class feature selection method rather than a binary one in order to study the level of improvement it brings to the current accuracy of age classification approach. Building a database from images of people captured in real-world scenarios (e.g., images from people watching a public TV display) would be a good idea to generalize the age and gender model for real-world applications.

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